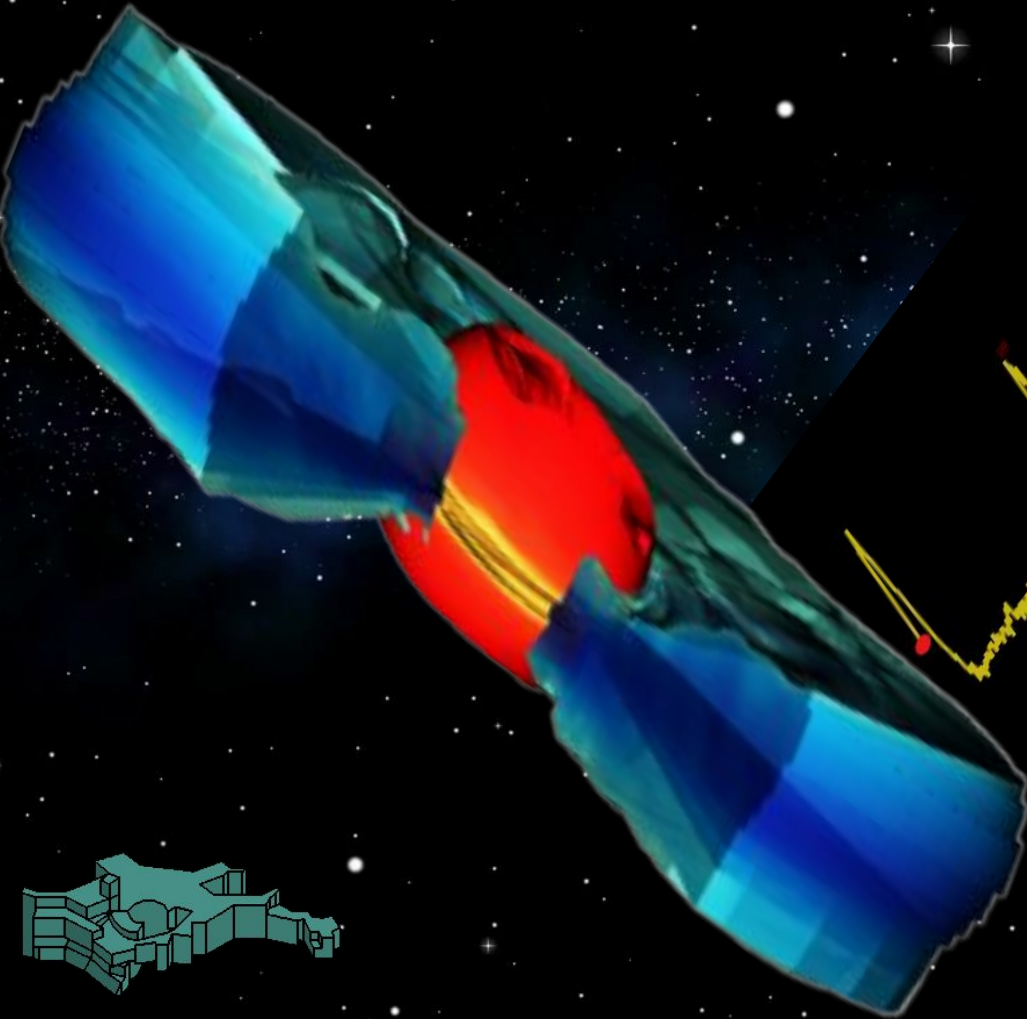


Variability in discs around black holes : Broadband variability & QPOs



Deepika Bollimpalli

Collaborators:

P. C. Fragile (CofC, USA)

W. Kluzniak (CAMK, Poland)

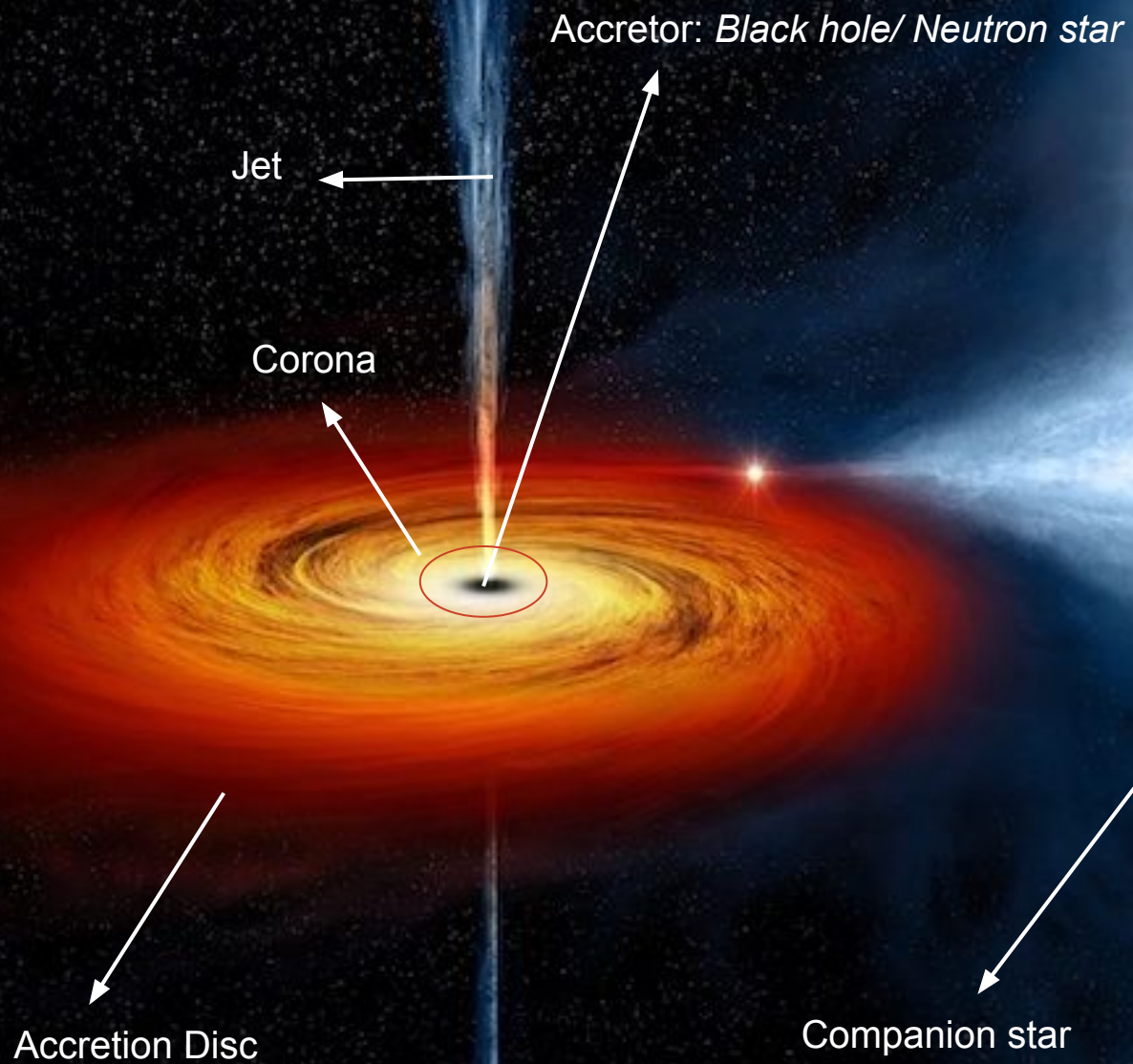
M. Gilfanov (MPA, Germany)

A. Beloborodov (Columbia Univ., USA)

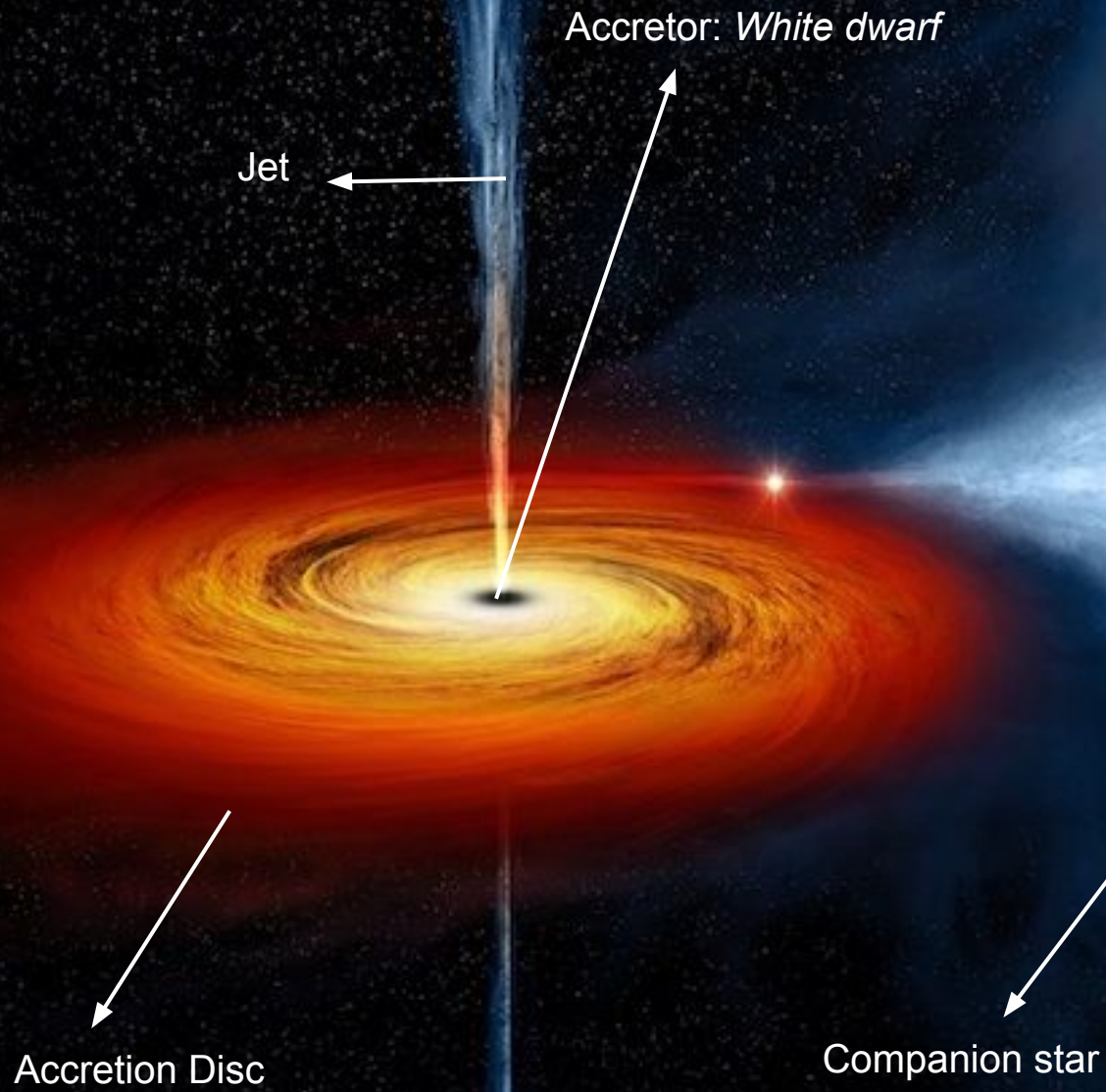


May 17, 2022

X-ray binary



*Cataclysmic
variables*

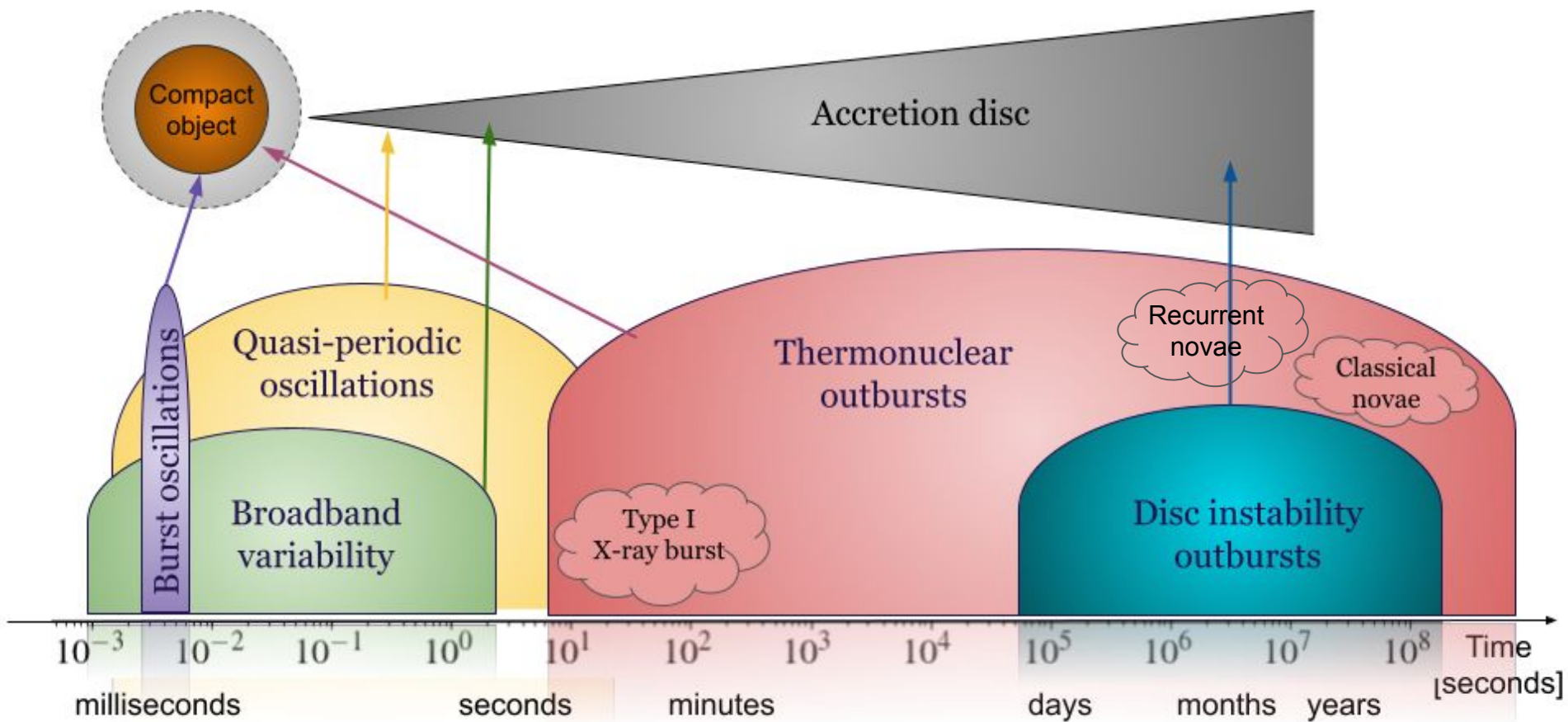


Accretion discs 101



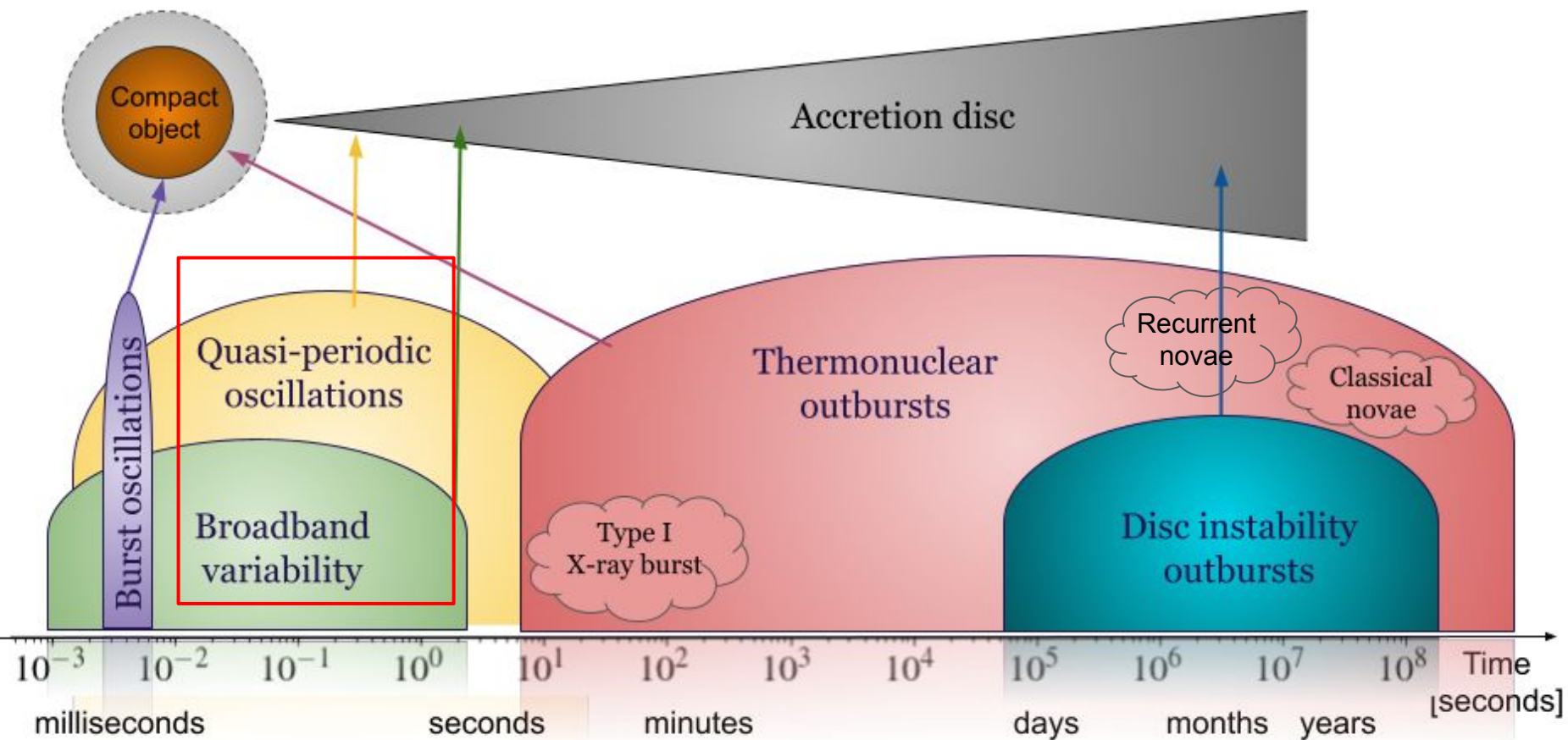
Important variability phenomena - instabilities, oscillations

! Magnetic fields of the compact object are not considered

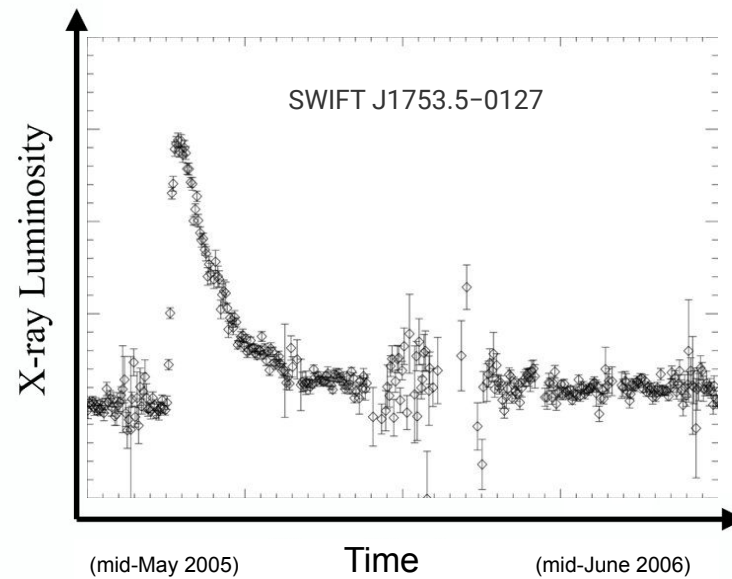


Important variability phenomena - instabilities, oscillations

! Magnetic fields of the compact object are not considered



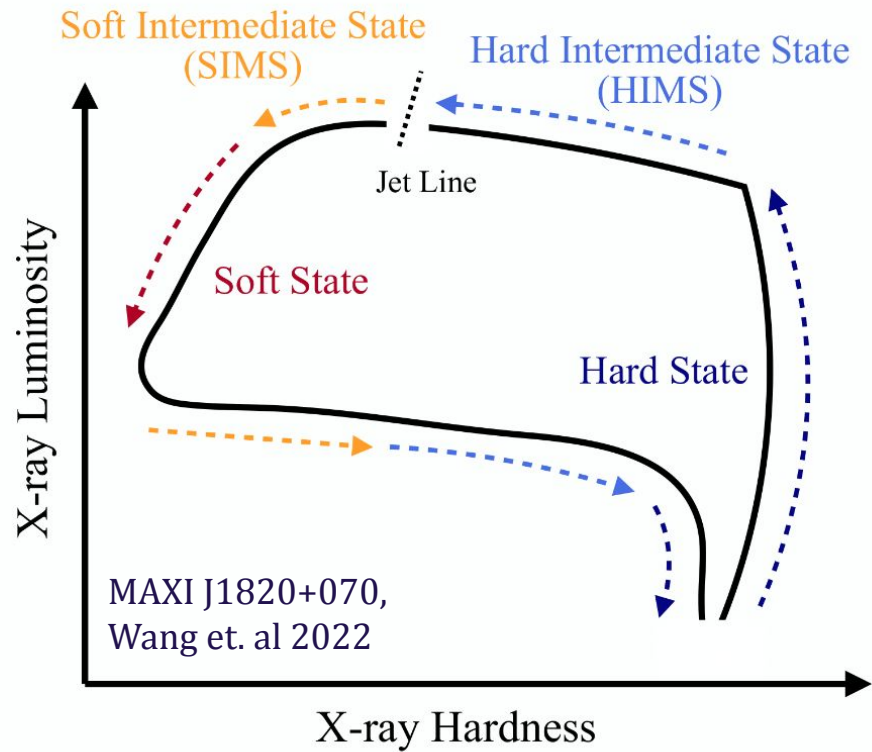
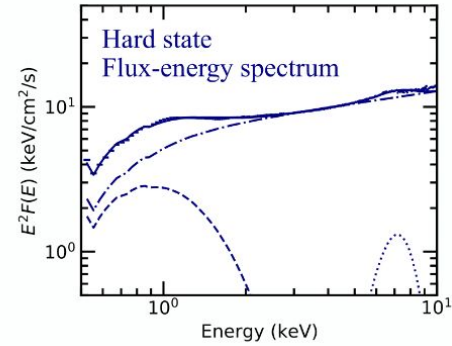
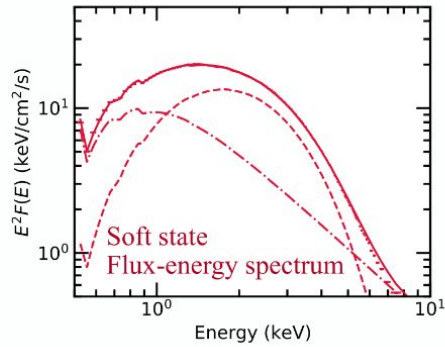
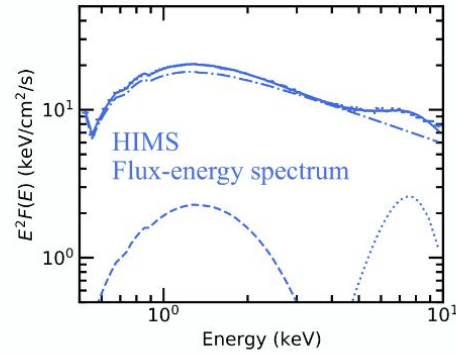
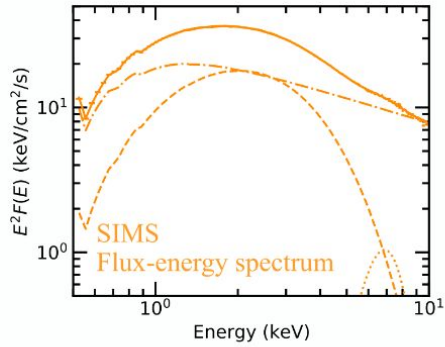
These systems are quite variable



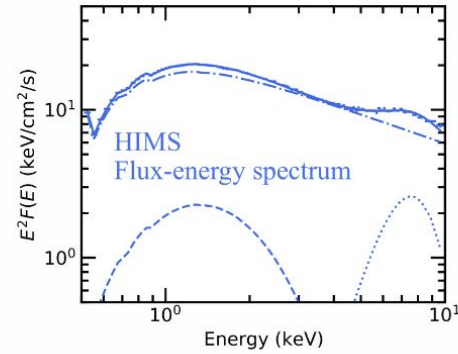
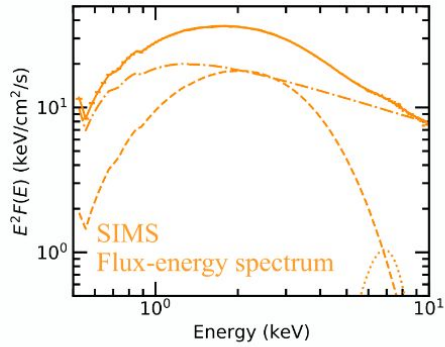
Cadolle Bel, M. et. al 2007

Spectral variability in X-ray binaries

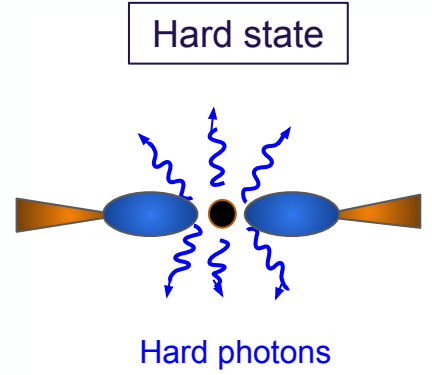
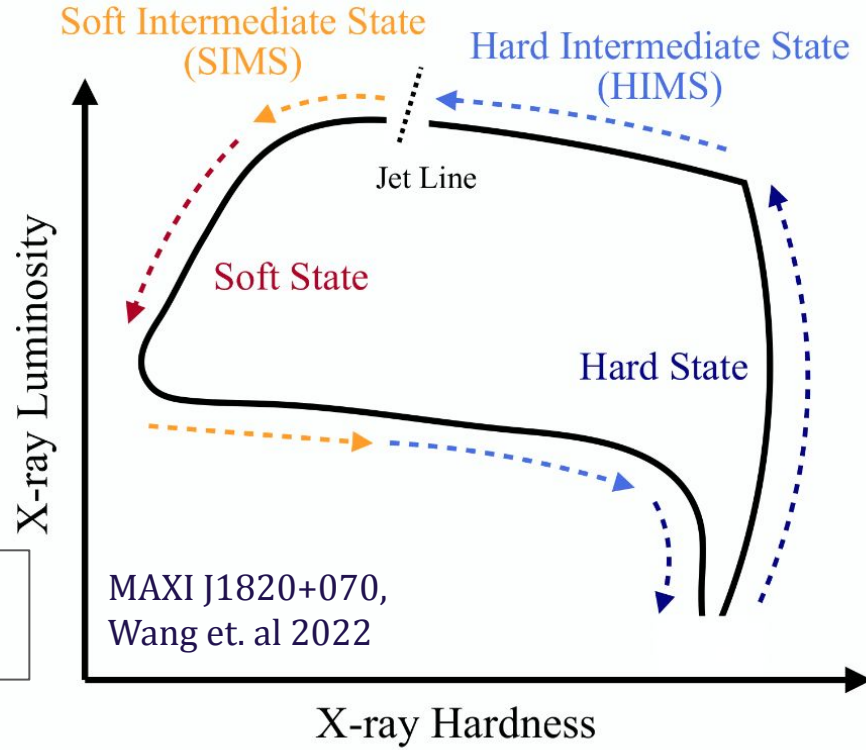
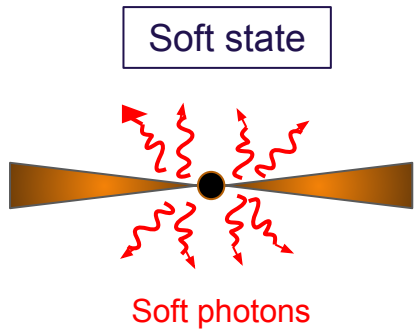
Martin Ward's talk
(in context of AGNs)



Spectral variability in X-ray binaries



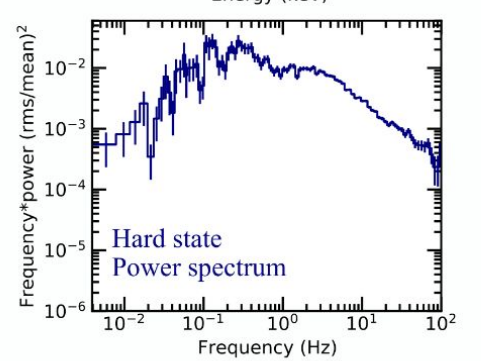
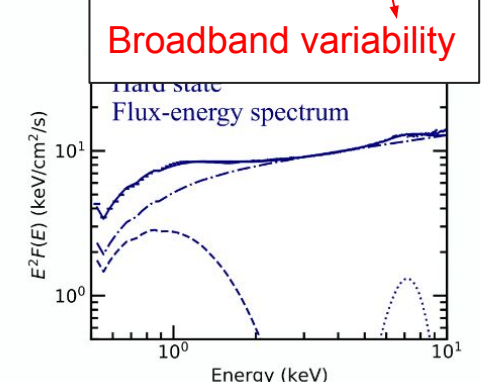
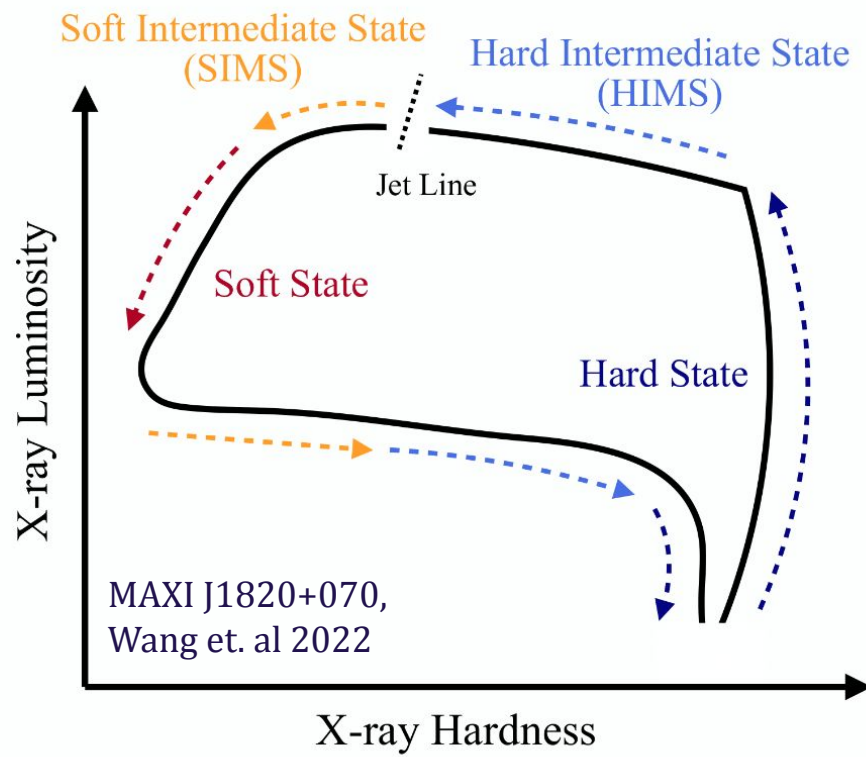
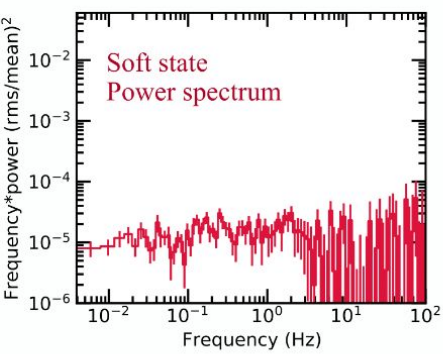
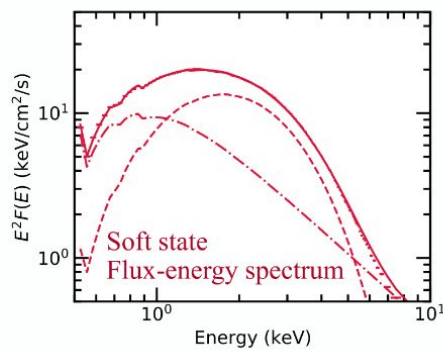
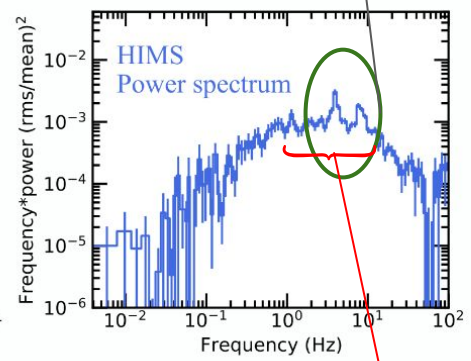
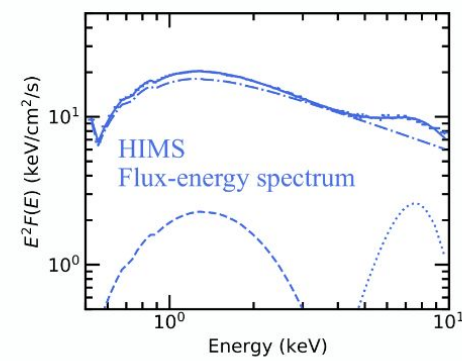
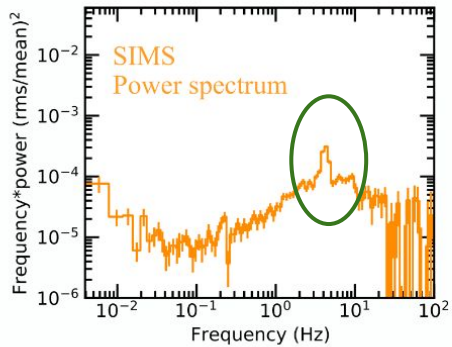
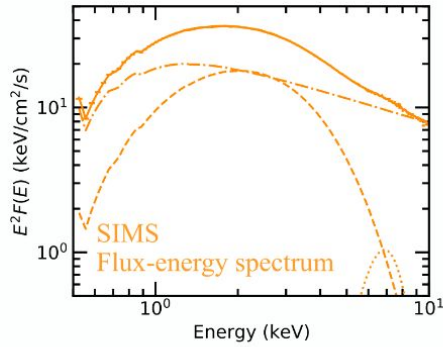
Andrzej Niedźwiecki's talk



State of corona is debatable

Sneha Prakash Mudambi's talk

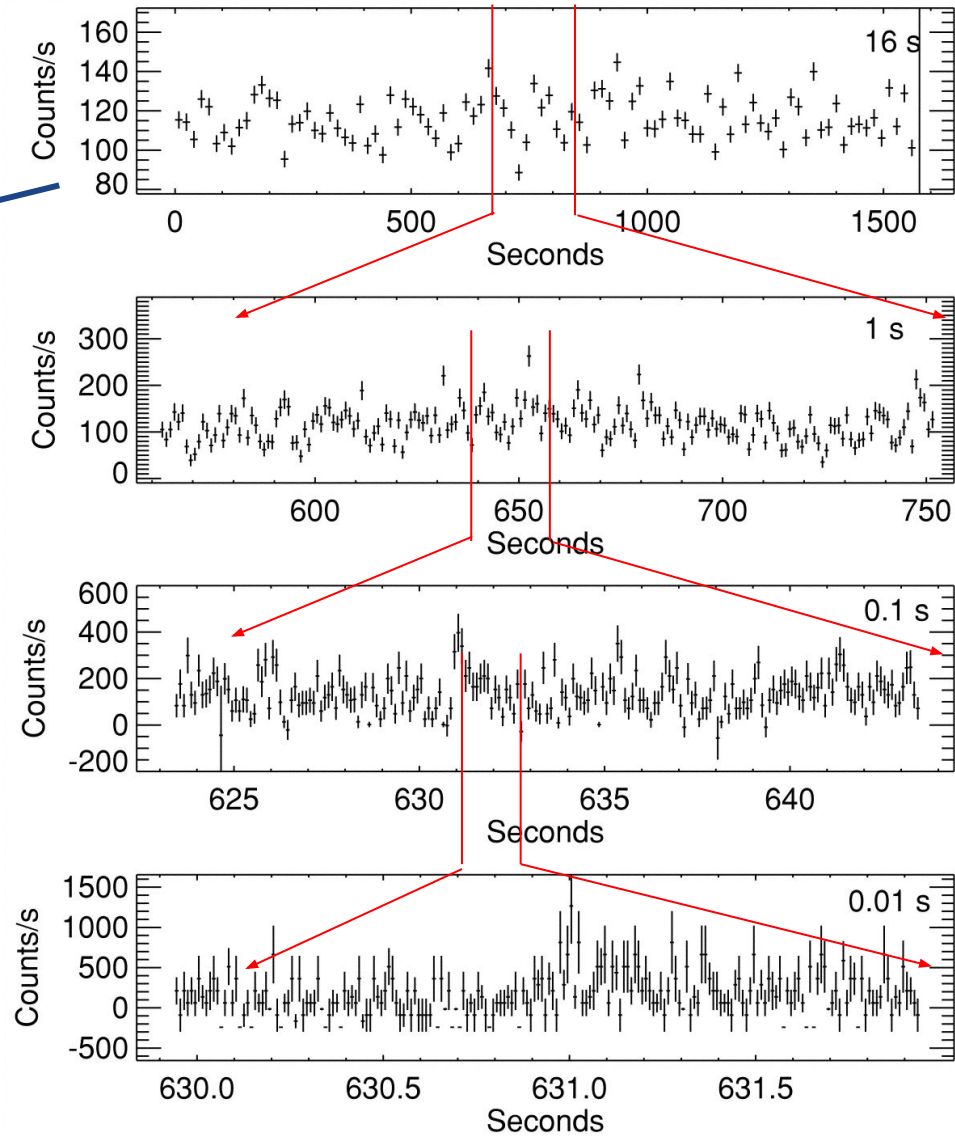
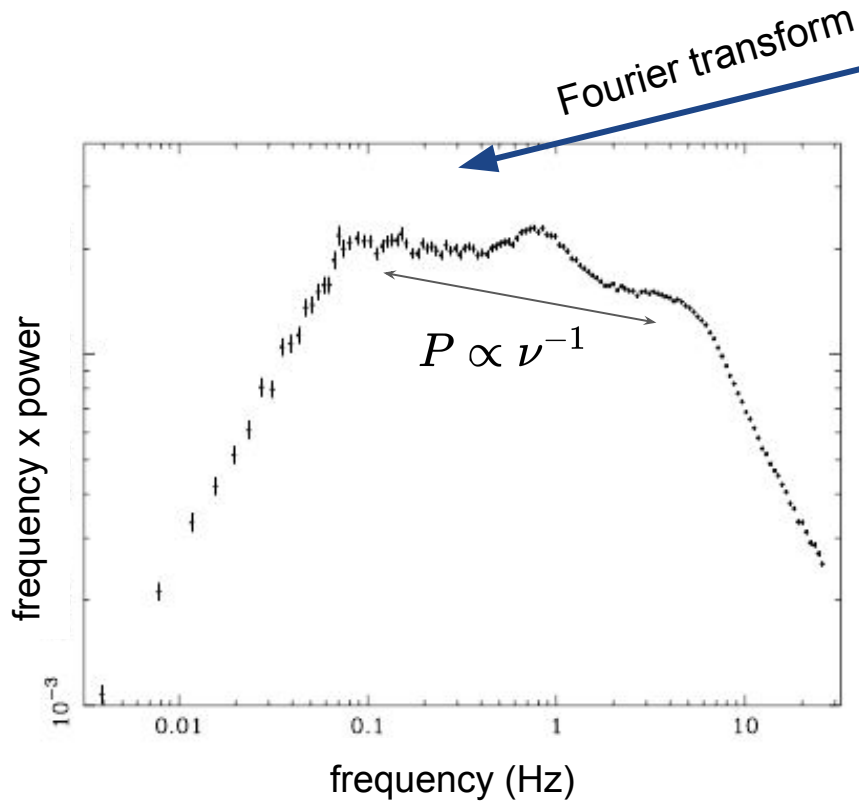
Spectral-temporal variability in X-ray binaries



Broadband variability

GRS 1758-258 (Lin et. al 2000)

- *Variability on broad timescales* - a few seconds to milliseconds.



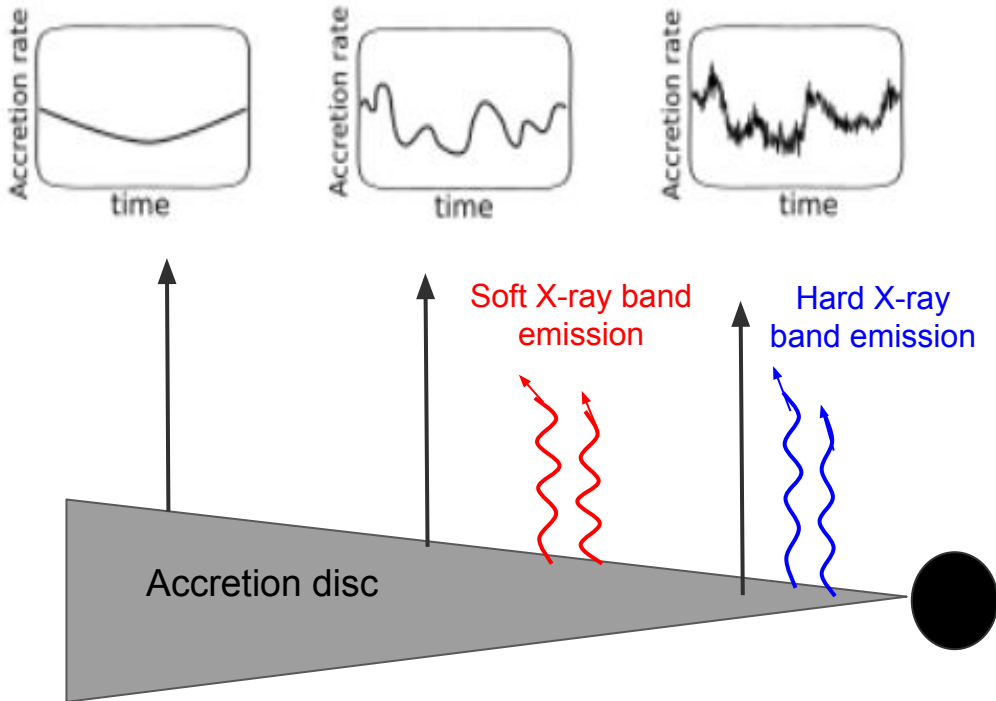
- *Characteristic features*: Strong coherence, frequency-dependent time lags, log-normal distribution, linear rms-flux relation.

What causes the broadband variability?

Propagating fluctuations

Viscous fluctuations rising on **local viscous time scales** at different radii drive fluctuations in accretion rate, which propagate inwards and couple together to produce the multiplicative behaviour in the accretion rate; thus the observed flux.

Accretion rate fluctuations



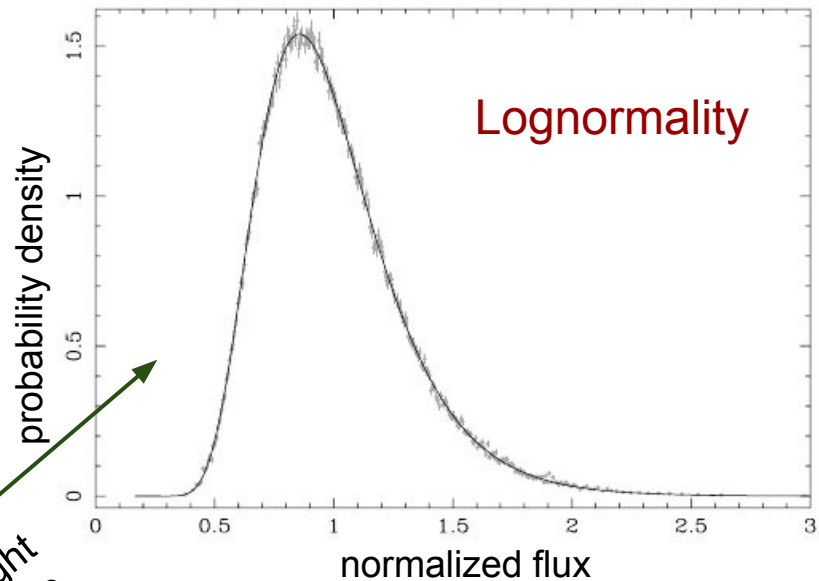
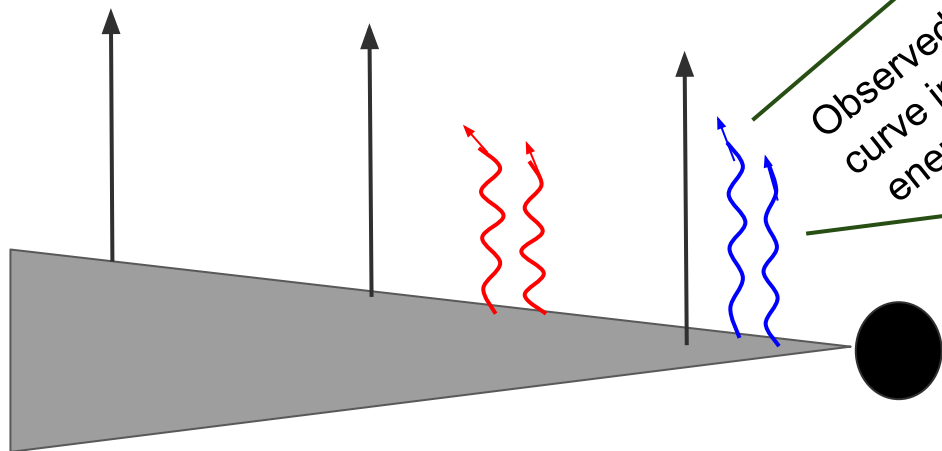
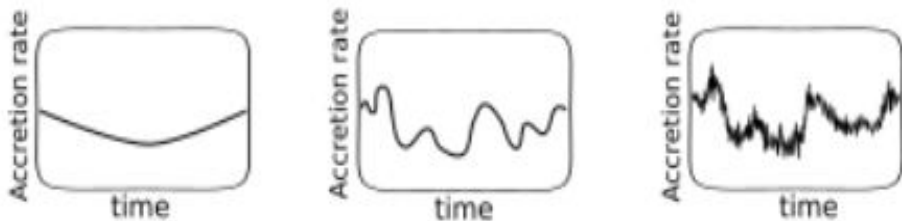
Lynden-Bell & Pringle 1974, Lyubarskii 1997, Kotov et. al 2001, Done 2007

Viscous timescale longer at larger radii

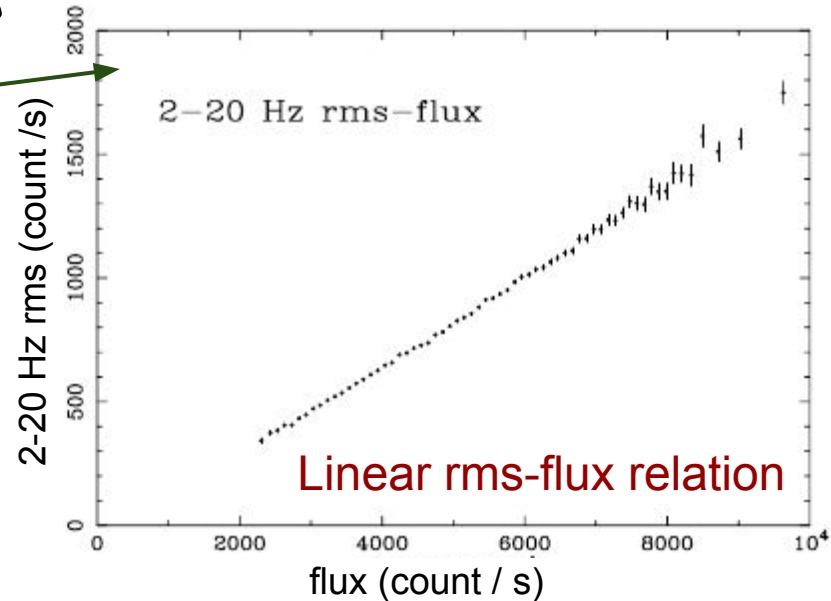
Simple picture: homogeneous disc/corona

Propagating fluctuations

Accretion rate fluctuations

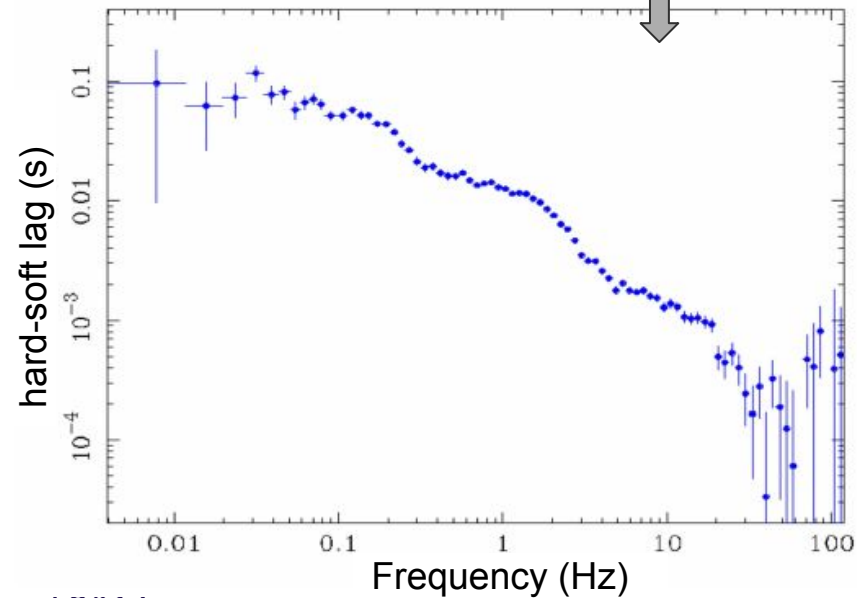
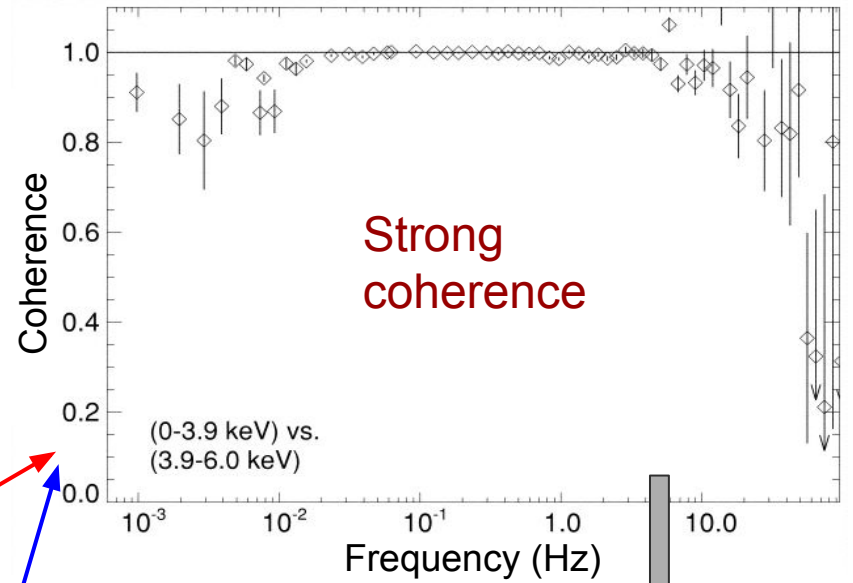
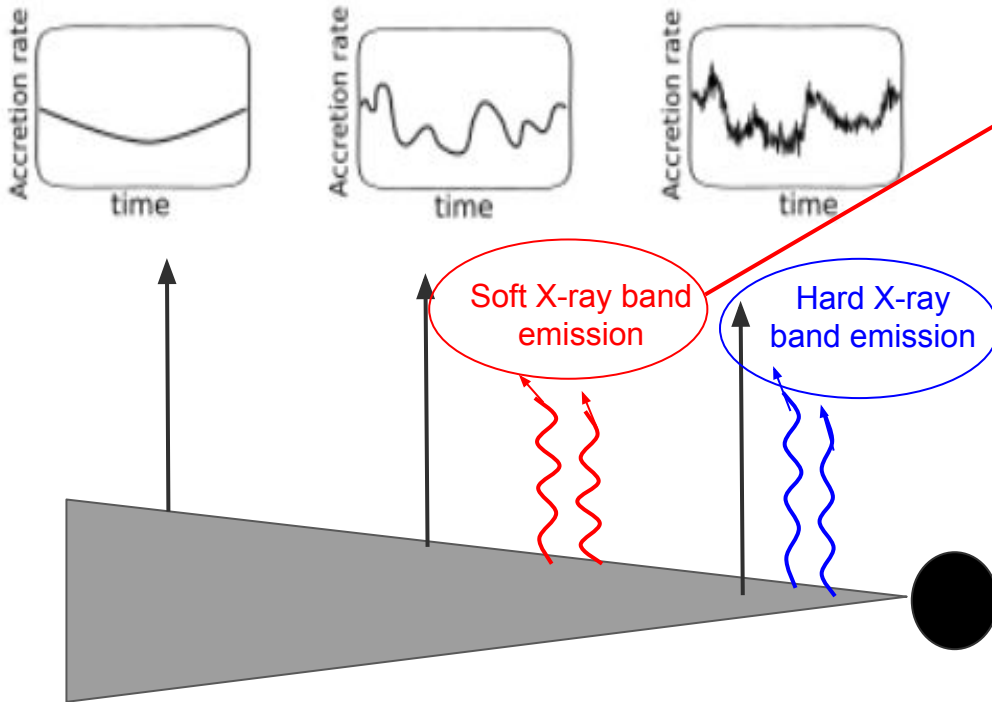


Observed light curve in single energy band



Propagating fluctuations

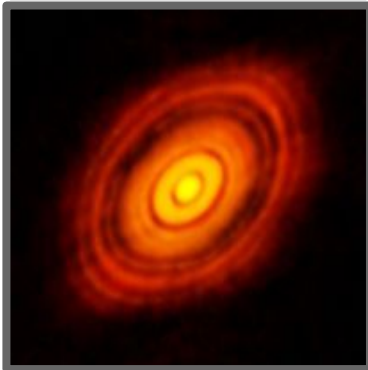
Accretion rate fluctuations



Quick note

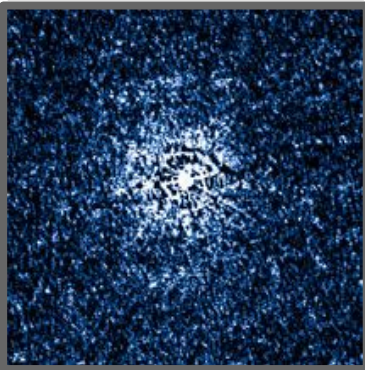
Gopal Bhatta's talk

proto-star
systems



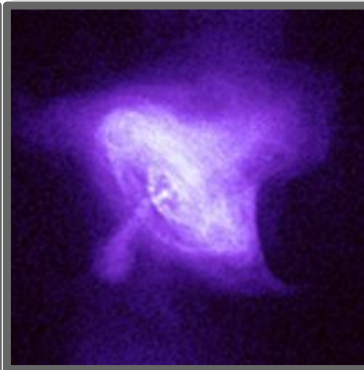
Scaringi et al 2015b

white dwarfs (WD)
in cataclysmic
binaries



Scaringi 2013,
Van de Sande 2015

black hole (BH) or
neutron star (NS)
binaries



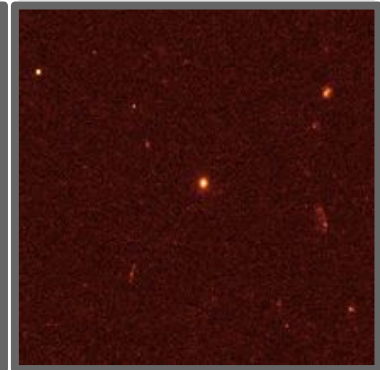
Wijnands & Van der
Klis 1999

AGN



Gaskell 2004

gamma ray burst
(GRB) sources

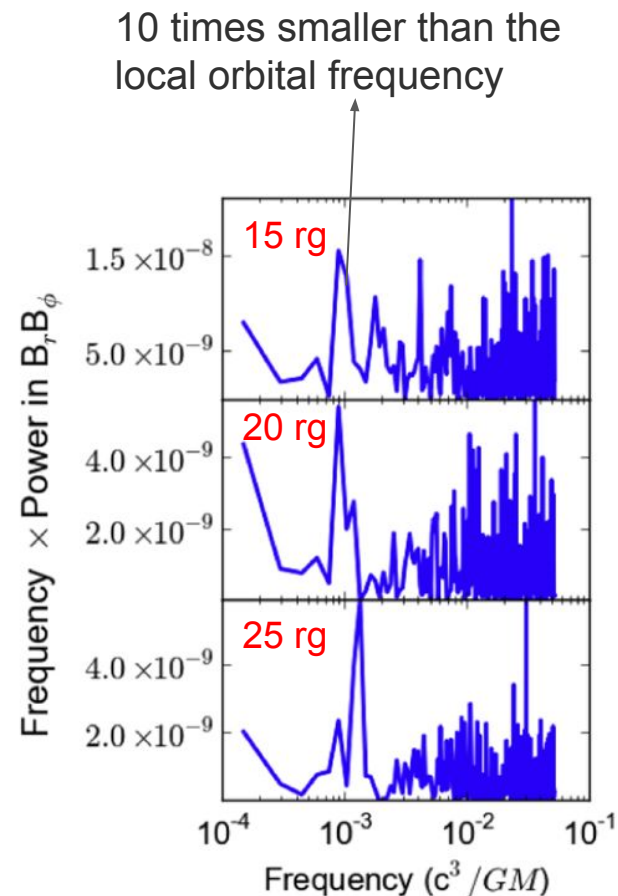
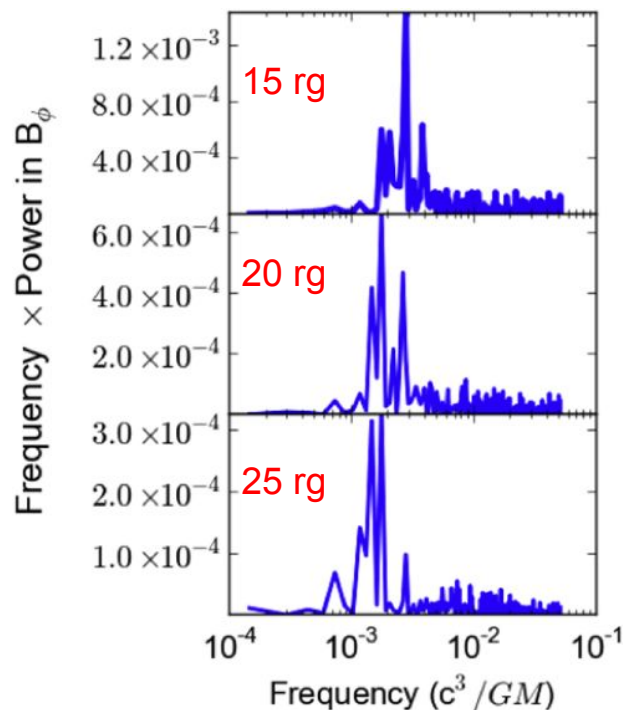


H.E.S.S.
Collaboration,
Rieger F. M., 2019

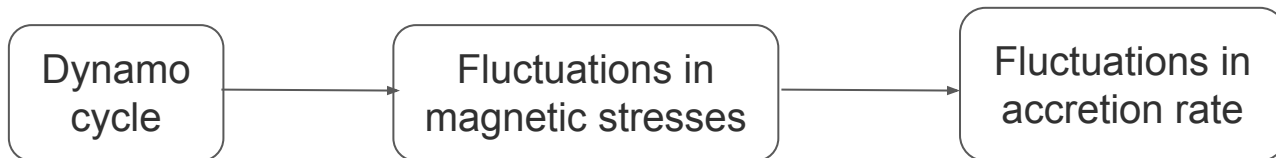
These variability features are observed in other accreting systems as well
- *variability must be related to accretion discs*

What drives these fluctuations?

Turbulent viscosity
↑
Magnetorotational instability



MHD simulations of **geometrically thin discs** (Hogg & Reynolds 2016)



What drives these fluctuations?

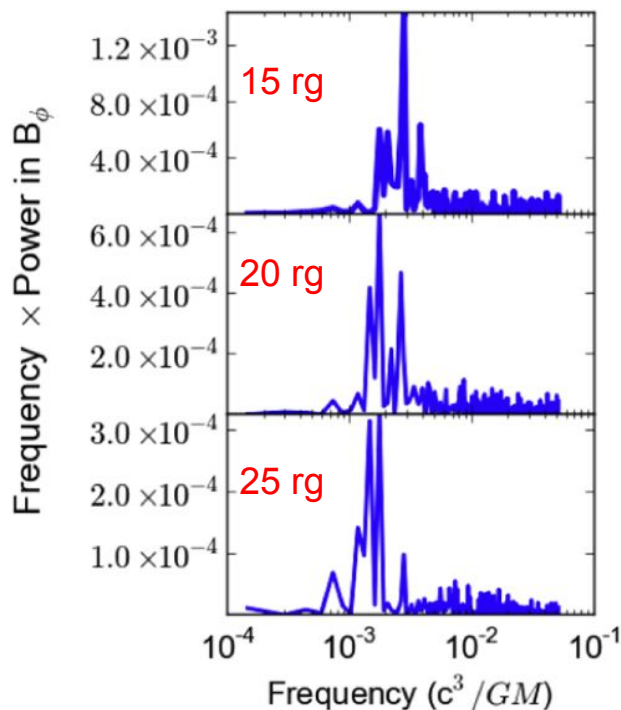
Turbulent viscosity



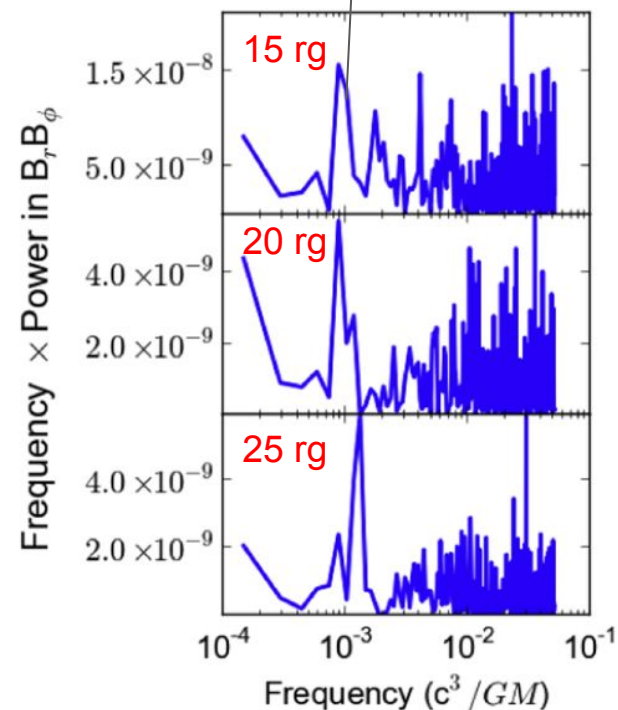
Magnetorotational instability

High frequency variability require **geometrically thick, optically thin accretion flows**

(Churazov et al. 2001; Arévalo & Uttley 2006; Ingram & Done 2011; Mahmoud & Done 2018a)



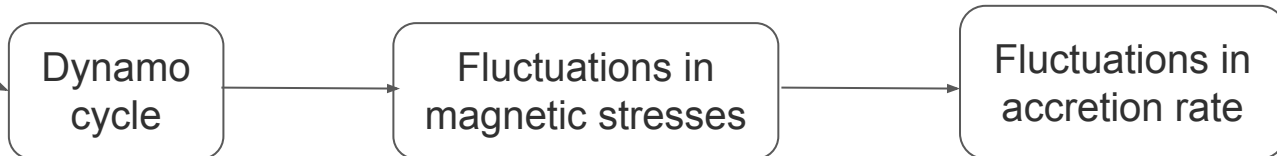
10 times smaller than the local orbital frequency



MHD simulations of **geometrically thin discs** (Hogg & Reynolds 2016)

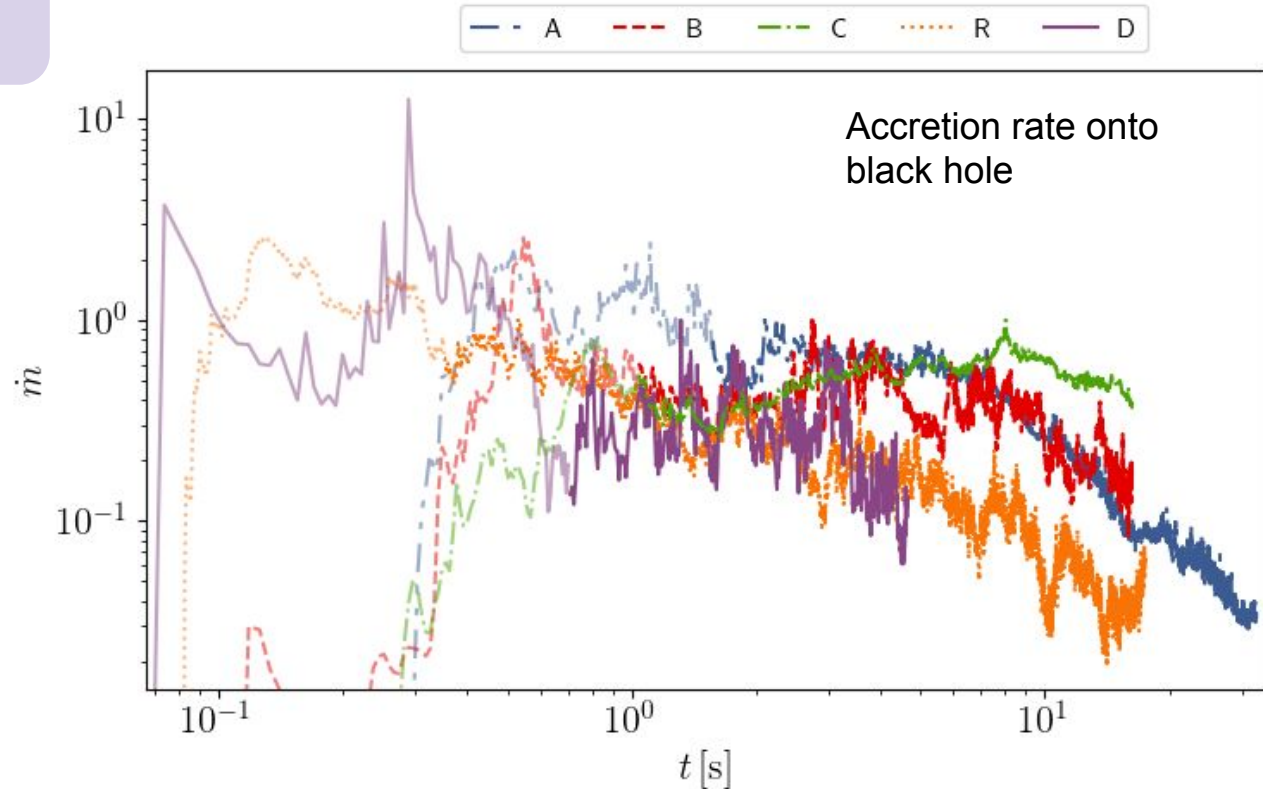
Unordered

(Hogg & Reynolds 2018)



Mass accretion rate as proxy for luminosity

- Non-radiative GRMHD simulations
- How well does the mass accretion rate from the numerical simulations reproduce the observed variability features in black hole binaries?



Bollimpalli et. al 2020

Simulations **A**, **B**, and **C** using **Athena++** (White et. al 2020)

Simulation **R** using **HARM** (Narayan et. al 2012)

Simulation **D** using **Cosmos++** (Bollimpalli et. al 2020)

**Strong evidence :
Radial coherence**

Fourier
transform

$$\dot{m}(r_1, t) \longrightarrow H(f)$$

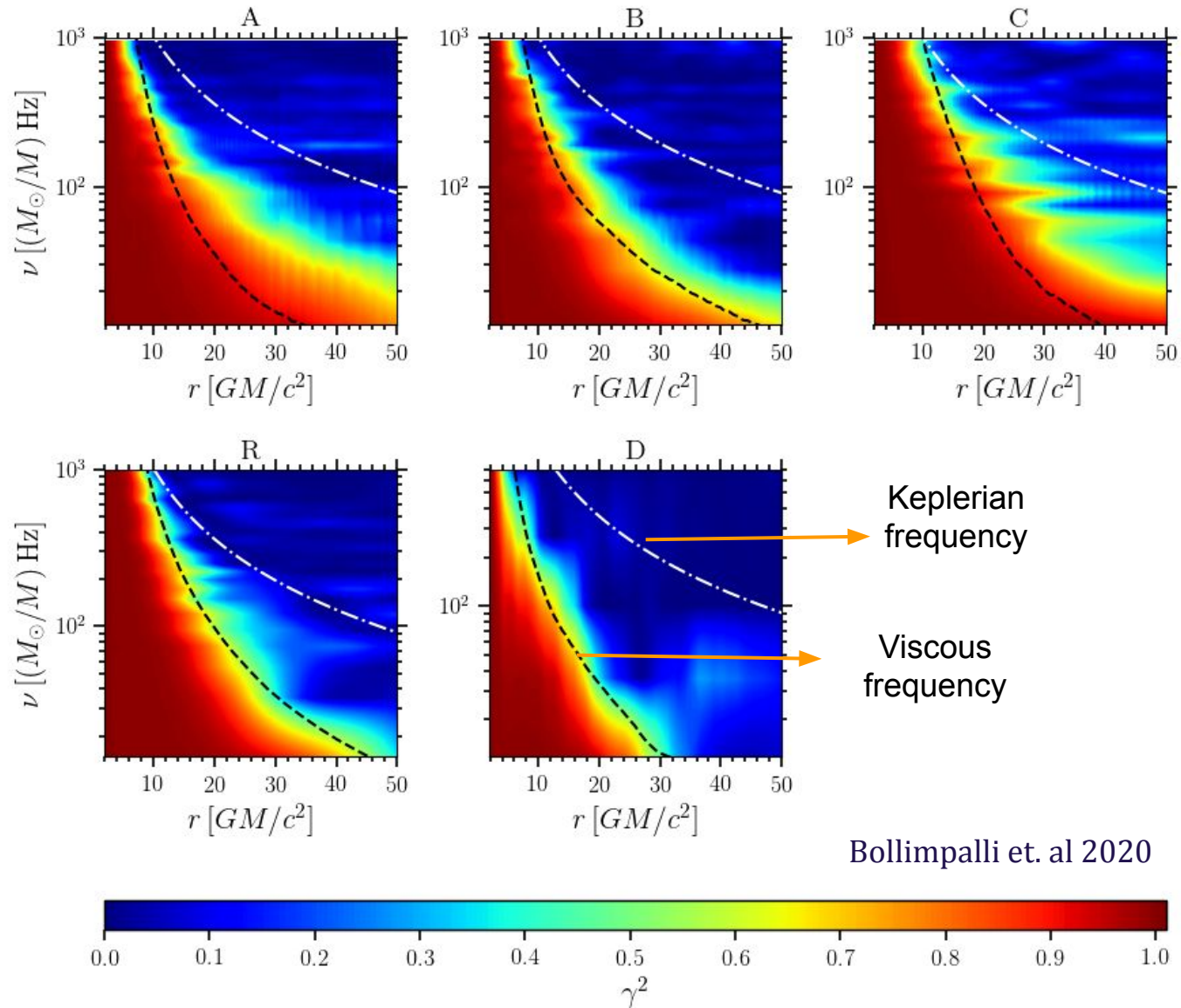
$$\dot{m}(r_2, t) \longrightarrow S(f)$$

$$\gamma^2 = \frac{\langle |H^*(f)S(f)|^2 \rangle}{\langle |H(f)|^2 \rangle \langle |S(f)|^2 \rangle}$$

1, if $\dot{m}(r_1, t)$ and $\dot{m}(r_2, t)$
are **linearly related**.

Here, we take

$$r_1 = 2r_g, r_2 > r_1$$



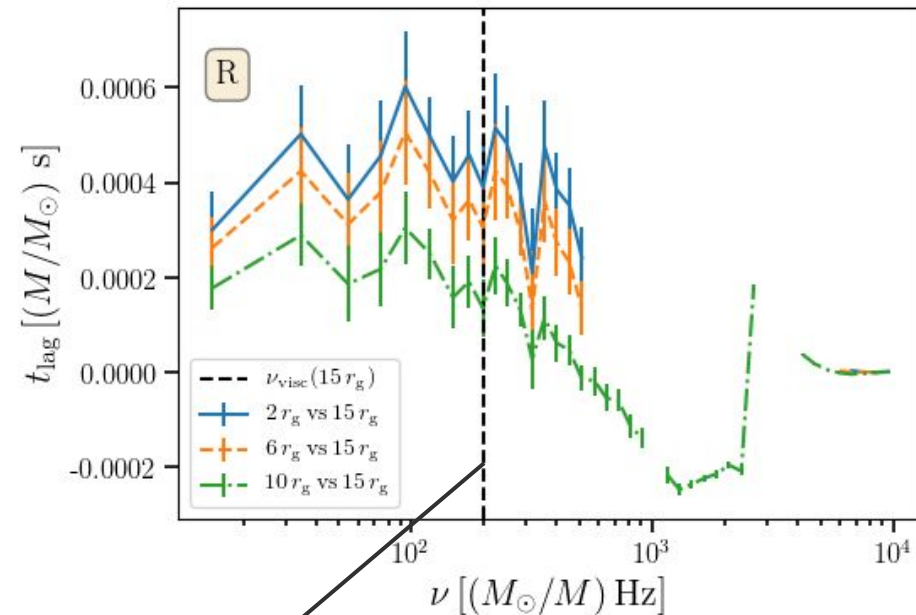
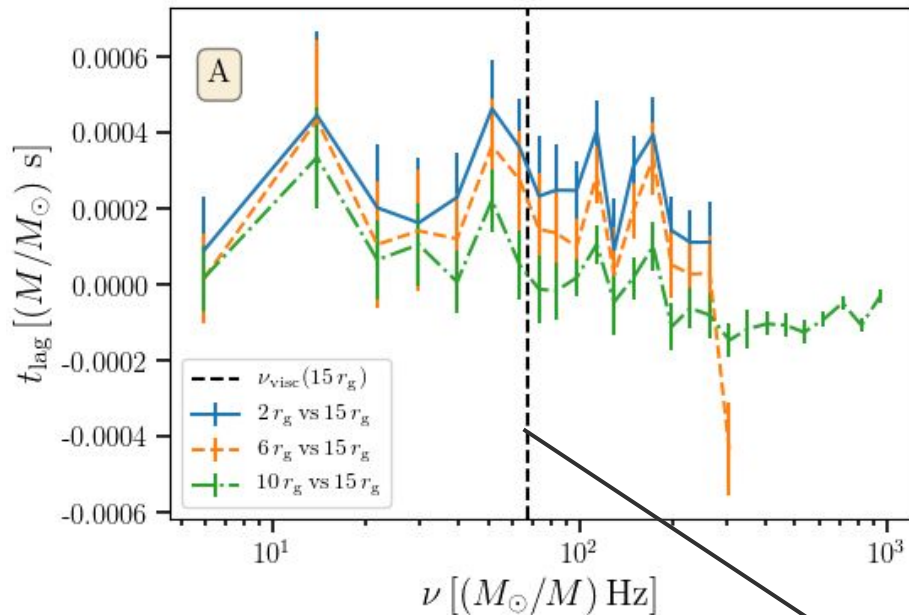
Bollimpalli et. al 2020

Remarkable coherence below the viscous frequency - *propagating fluctuations*

Time lags in fluctuations

- Positive lags - why frequency independent?
fluctuations are propagating inward
- Variability at smaller radii lags variability at larger radii
 - *Propagating timescales are independent of the Fourier frequencies.*
 - Maybe dissipative processes are responsible?

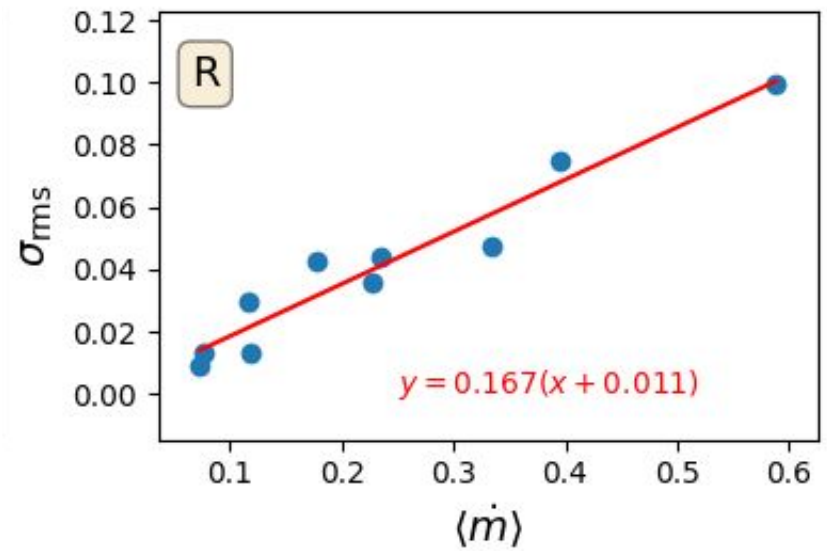
Bollimpalli et al 2020



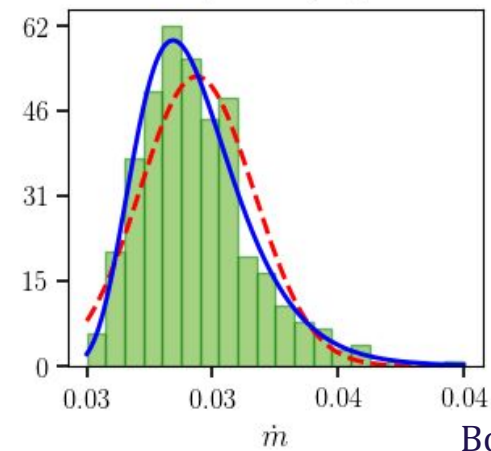
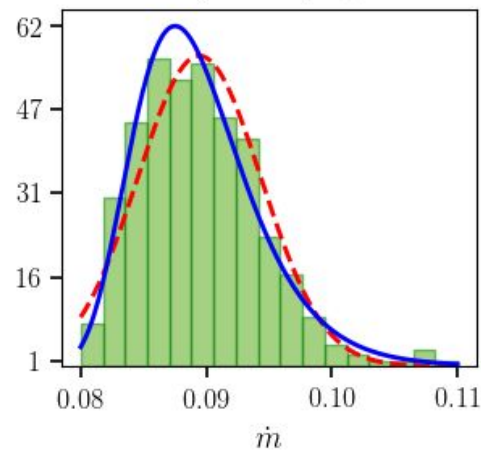
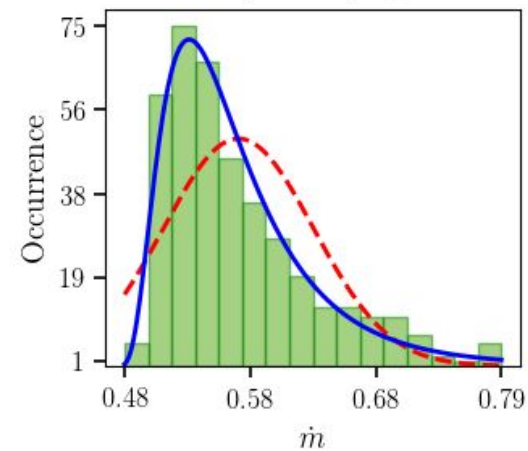
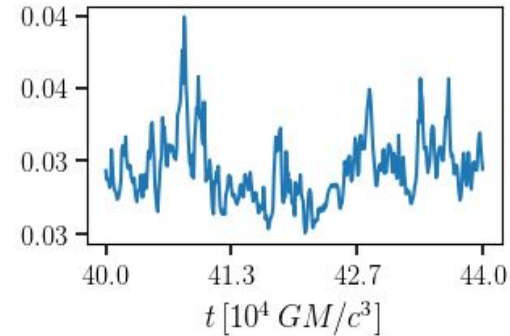
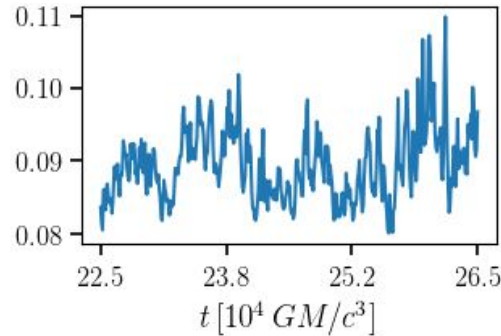
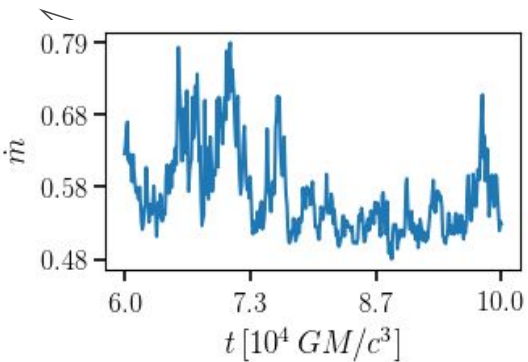
Viscous frequency
at $15 r_g$

Distribution of mass accretion rate

- Log-normal distribution - underlying variability process is *multiplicative* in nature.
- RMS-mean relation - All simulations exhibit *linear* relation - the higher the accretion rate, larger the variability.



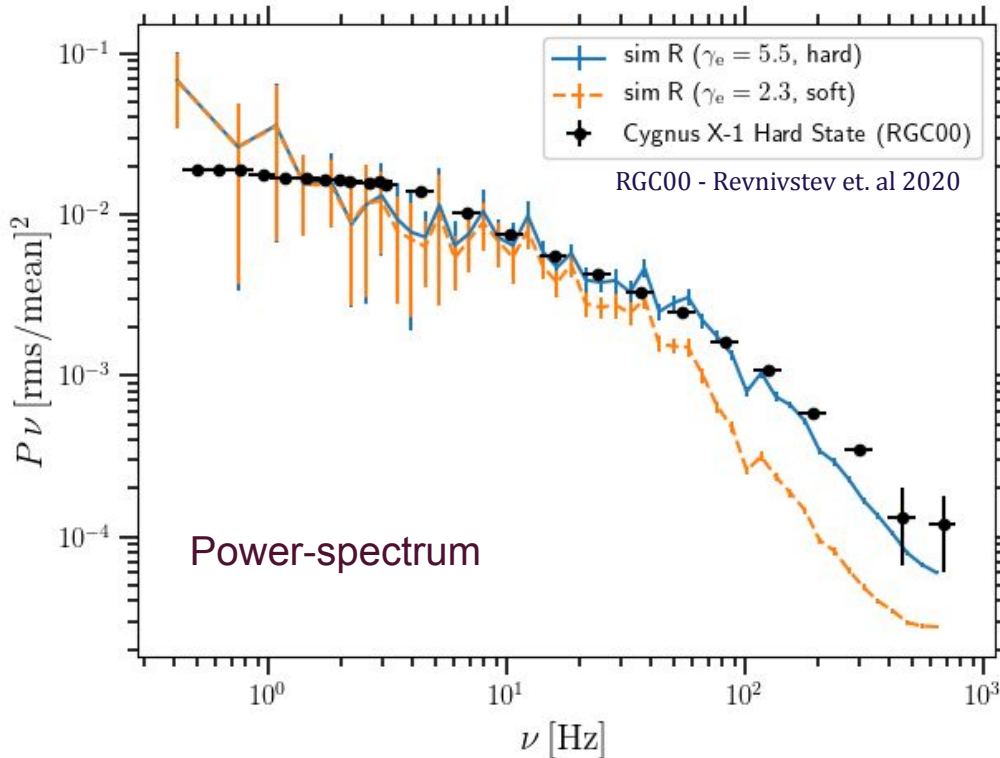
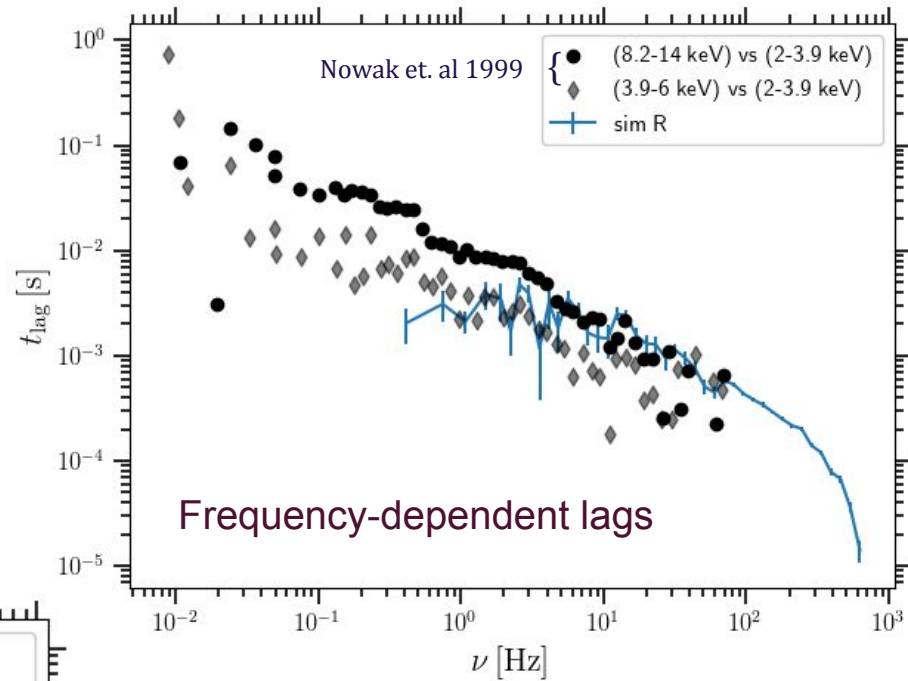
— Log-normal - - - Normal/Gaussian



Comparison with observations

➤ Synthetic light curves generated from the simulations using an emissivity profile - $\epsilon \propto r^{2-\gamma}$

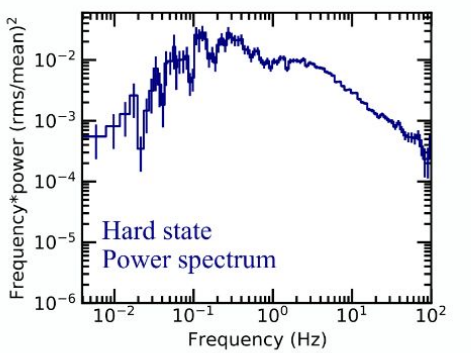
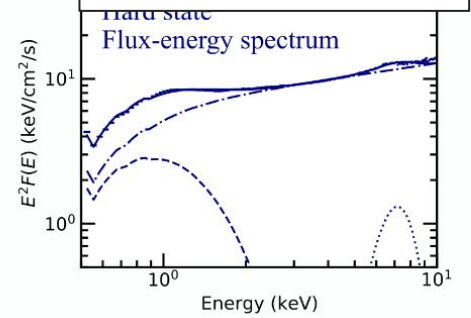
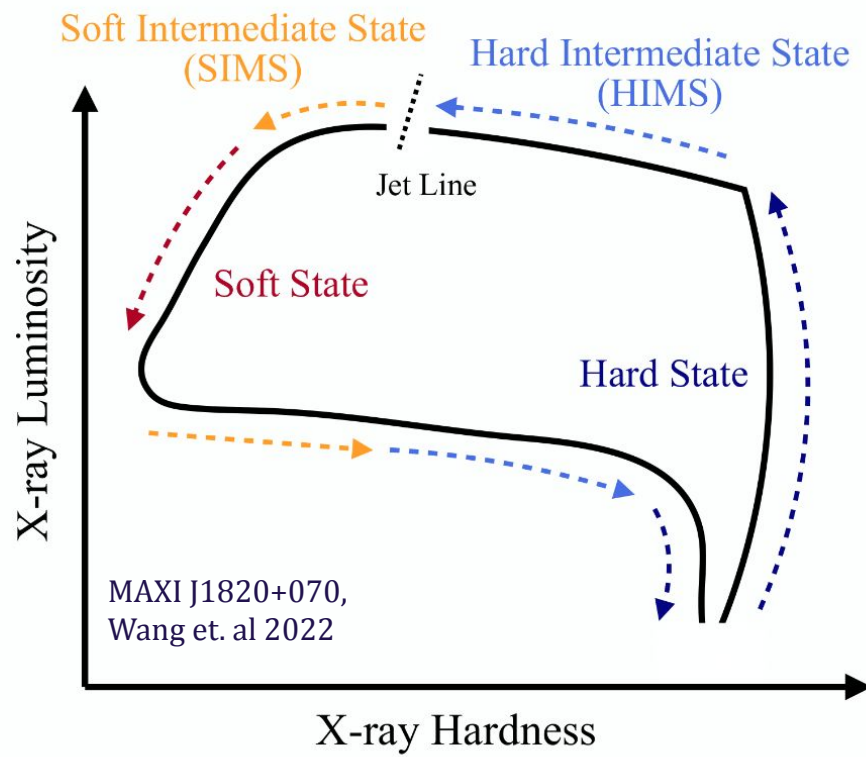
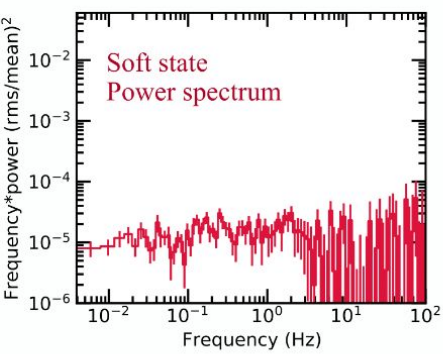
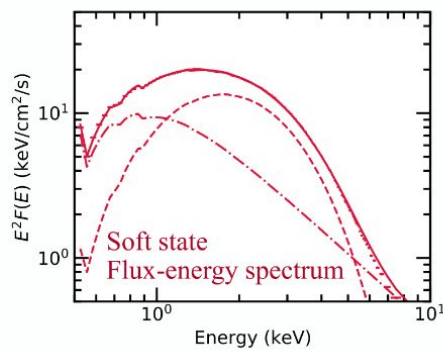
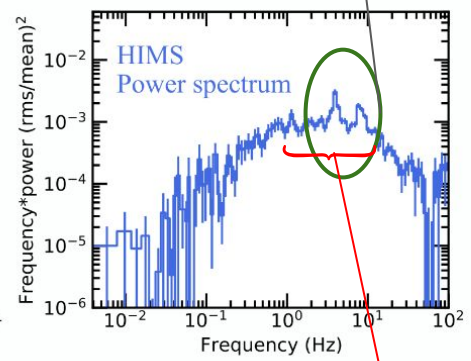
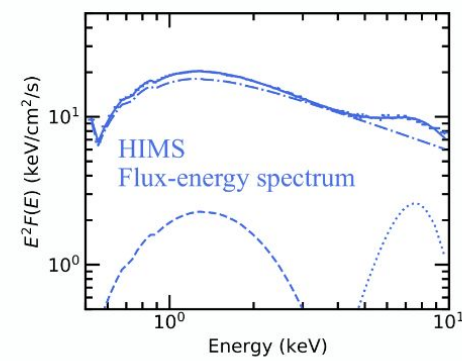
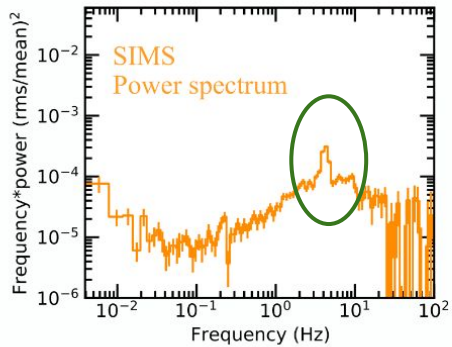
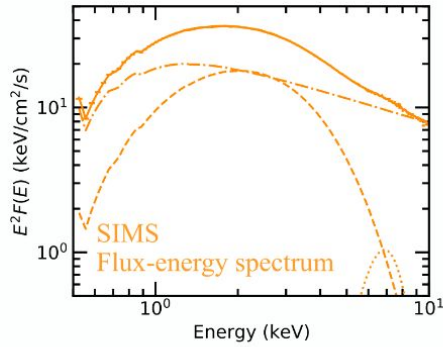
$$f(t) = \sum_{r=2r_g}^{25r_g} \epsilon(r) \dot{m}(r, t)$$



Bollimpalli et. al 2020

Simulations agree well with the observations of the low/hard state of *Cygnus X-1*.

Spectral-temporal variability in X-ray binaries

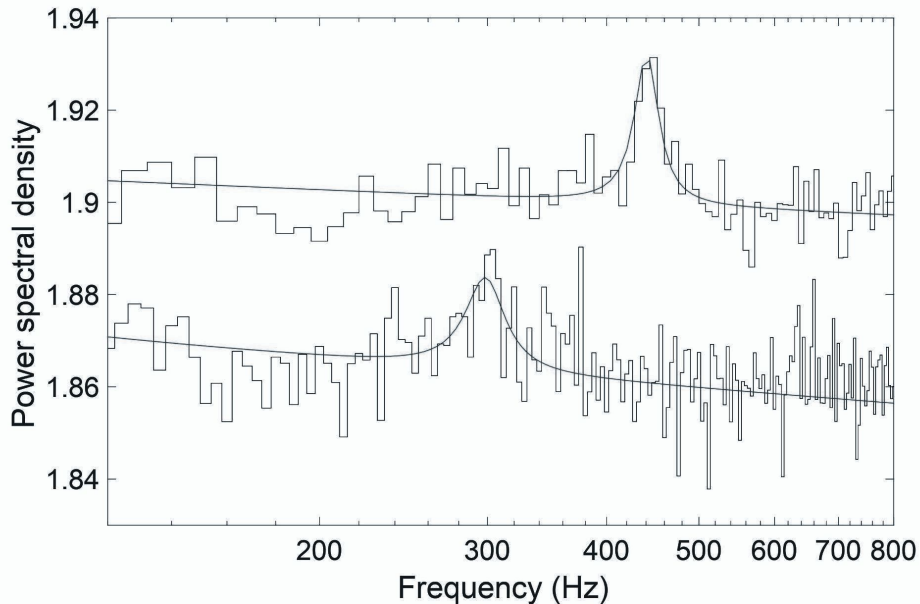


Broadband variability

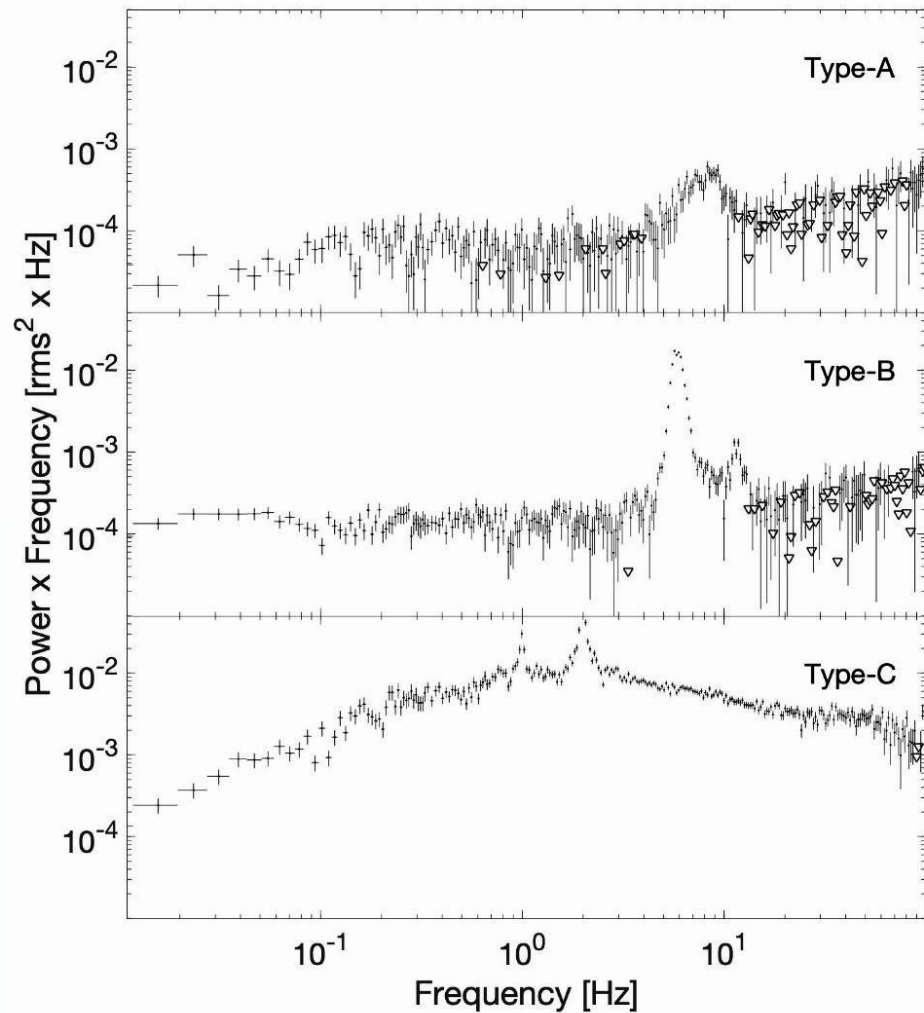
Quasi-periodic oscillations (QPOs)

- Rapid variability; Frequency modulates.
- Low-frequency QPOs (mHz to $< \sim 30$ Hz)
- High-frequency QPOs ($> \sim 60$ Hz)
- Probes for strong gravity, accretion disc geometry e.t.c.

High-frequency QPOs



Low-frequency QPOs



See reviews by van der Klis 2006, Remillard & McClintock 2006, Ingram & Motta 2020

High frequency QPOs in black hole binaries

HF QPOs - detected only in a handful of sources.

Potential models:

1. Oscillations in discs (discoseismic modes)

p-modes are commonly observed in the simulations (Reynolds & Miller 2009, Mishra et. al 2018, Bollimpalli et. al 2020)

g-modes are damped by MHD turbulence (Reynolds & Miller 2009)

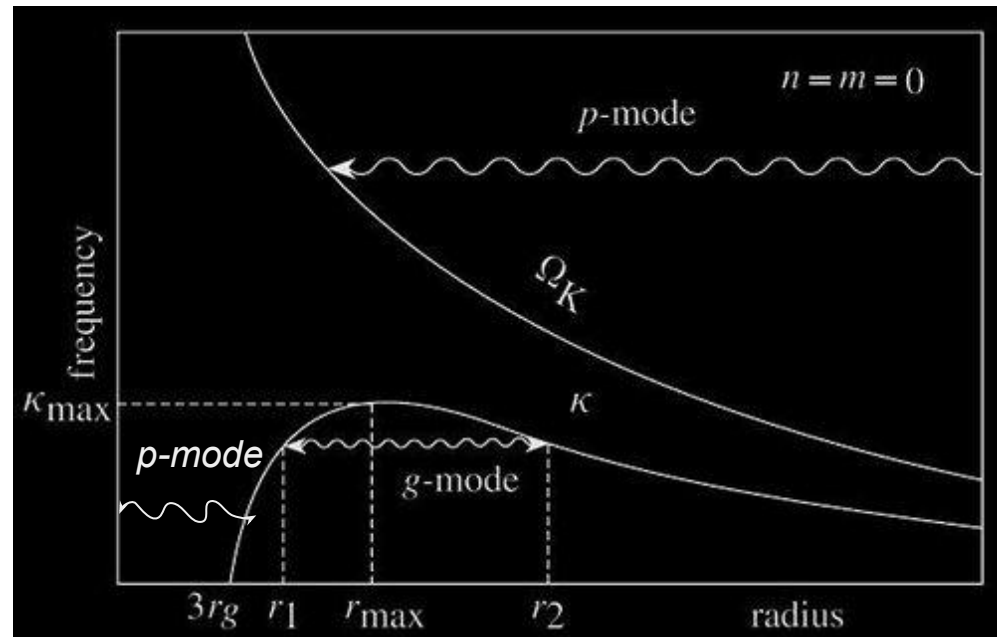
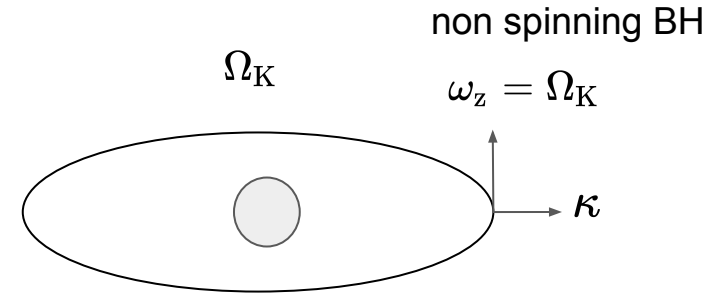
Eccentricity (>0.03) in warped discs can excite inertial g-modes (Dewberry et. al 2020a, 2020b)

2. Parametric resonance model

(Abramowicz & Kluźniak 2001,2003; Abramowicz et. al 2002, 2003)

Resonance between modes at particular radius

Hard to reproduce in the simulations.

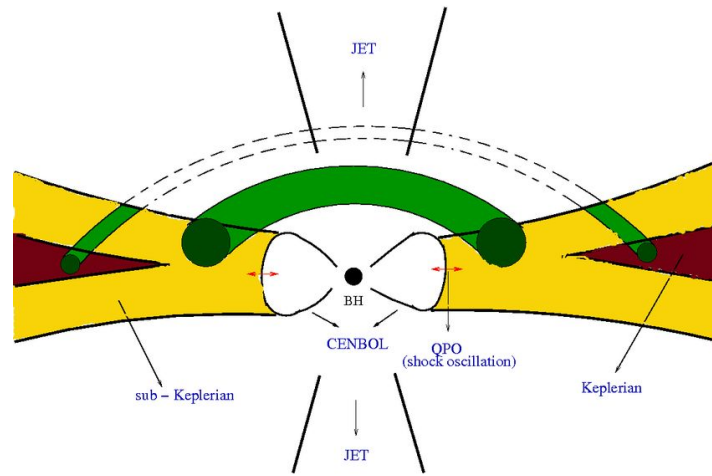


Propagation diagram for axisymmetric modes.
(Kato et. al 1998)

Continuation...

3. Oscillating shocks

(Chakrabarti & Titarchuk 1995)



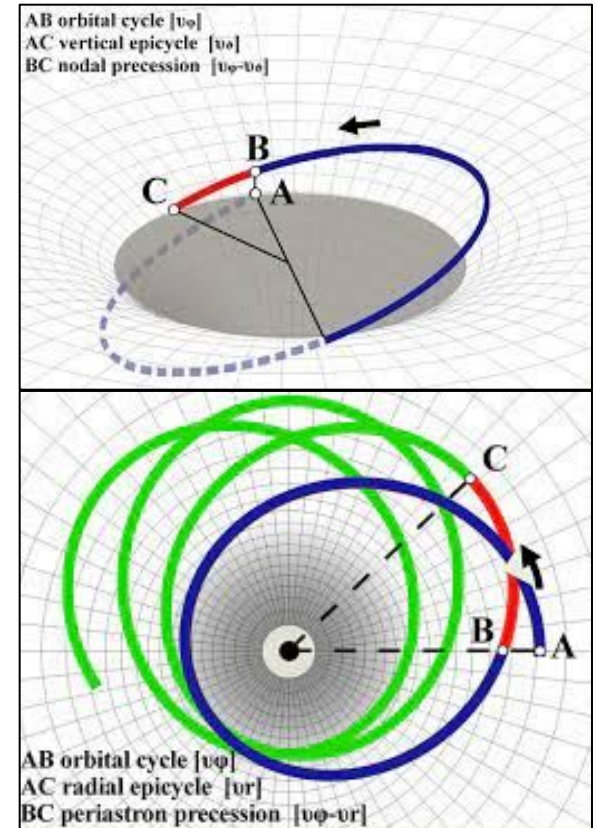
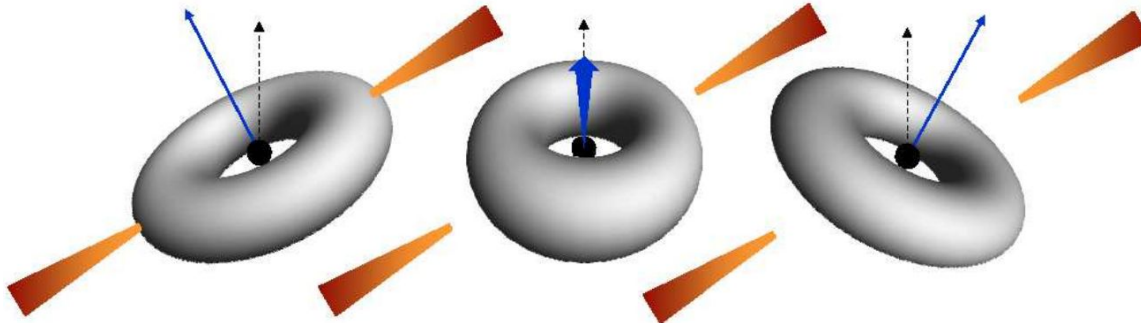
(Radhika et. al 2013)

4. Relativistic precession model

Upper HF QPO - Orbital frequency; Lower HF QPO - periastron precession frequency; Low-frequency QPO - nodal precession frequency (Stella & Vietri 1998; Stella et. al 1999)

3:2 HF QPOs - breathing and vertical epicyclic frequencies of globally oscillating hot, thick flow (Fragile et. al 2016)

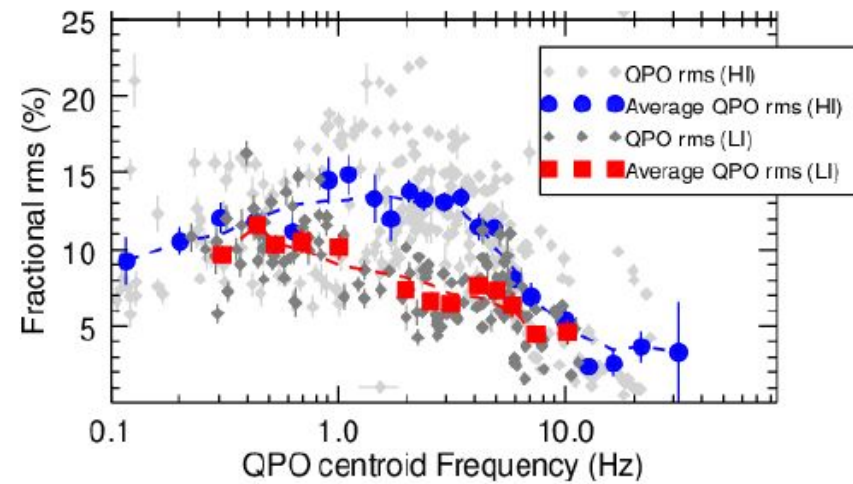
Low-frequency Type-C QPO - Precessing hot flow in a truncated disc geometry (Ingram et. al 2009; Ingram & Done 2011)



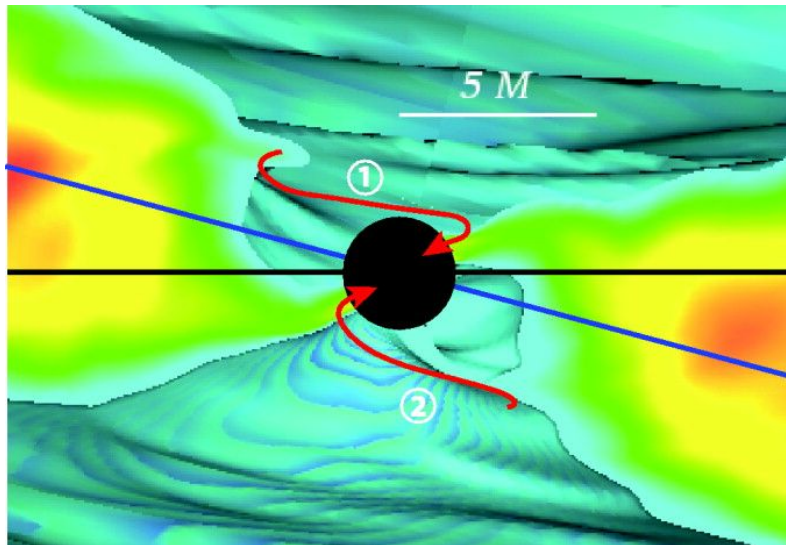
Courtesy: Sara E. Motta

Type - C Low frequency QPO

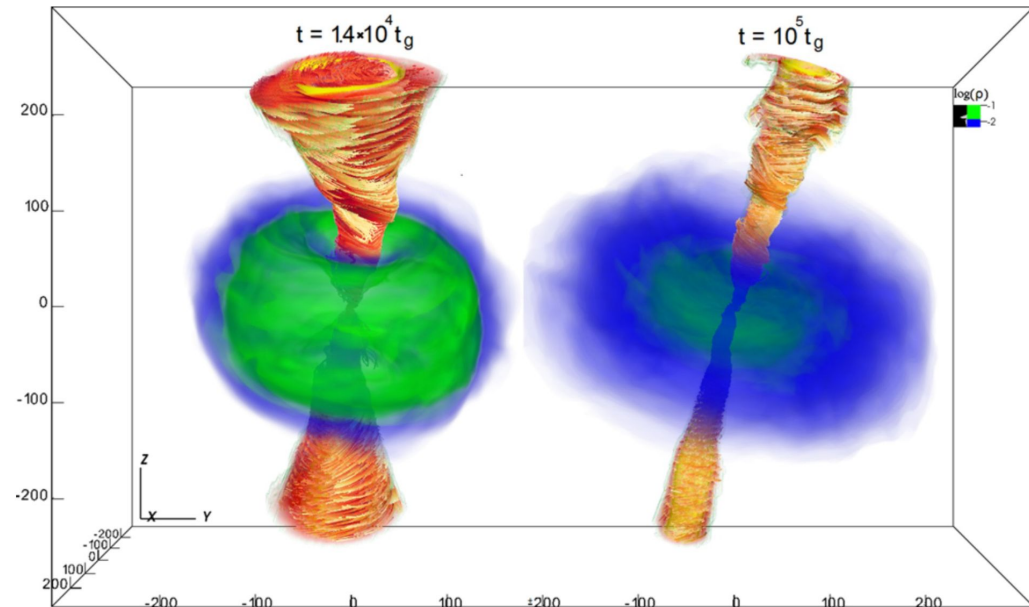
- Centroid frequency is tightly correlated with the spectral state (a few mHz in the hard state to ~ 10 Hz in the intermediate states).
- Strong inclination dependence of the QPO amplitude and phase lag suggests that it is likely a **geometrical effect**.
- Other models: accretion-ejection instability ; pressure or accretion rate modes - all require a moving inner radius.



Ingram & Motta 2020



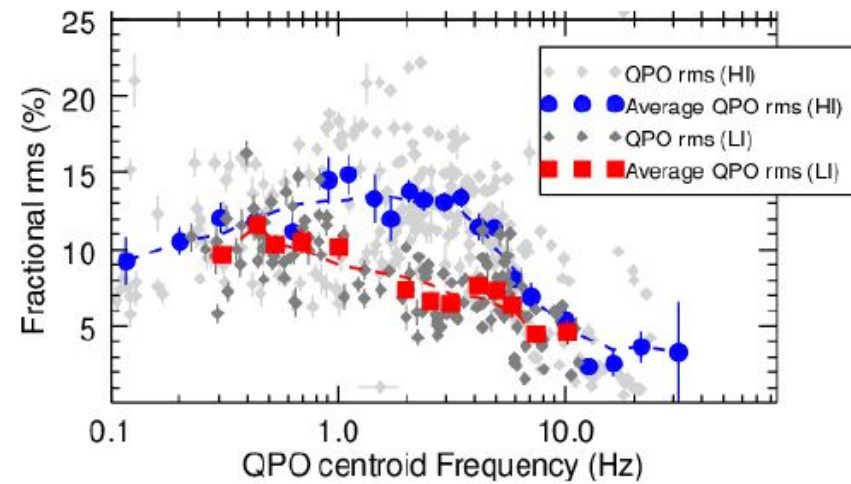
Fragile et. al 2007



Liska et. al 2018

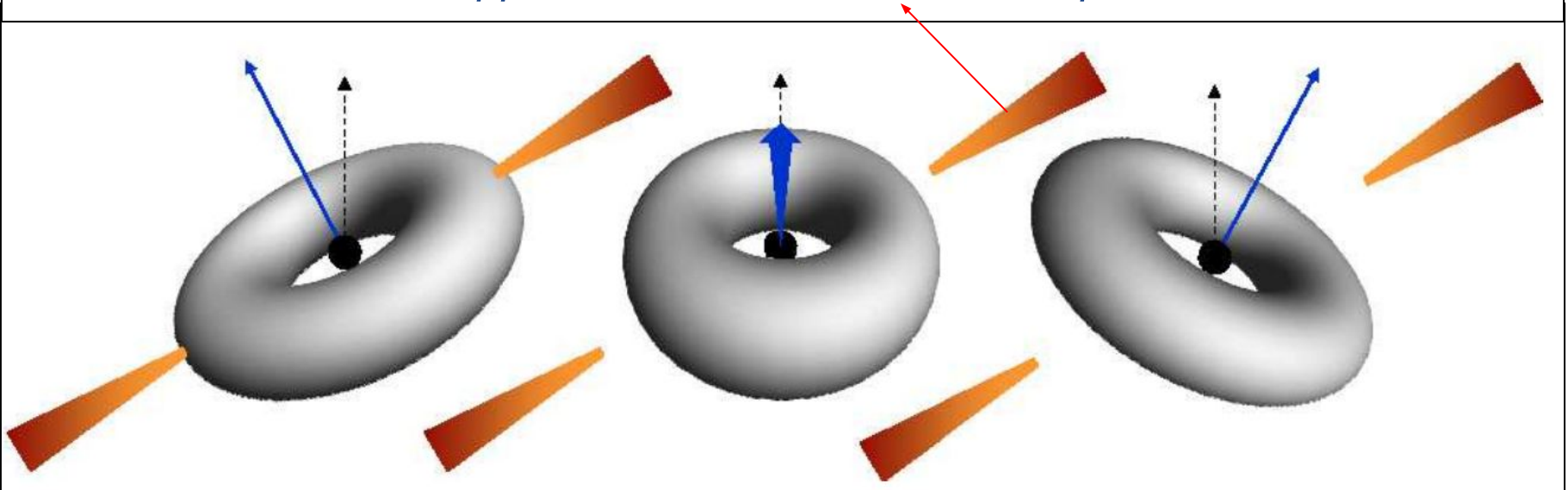
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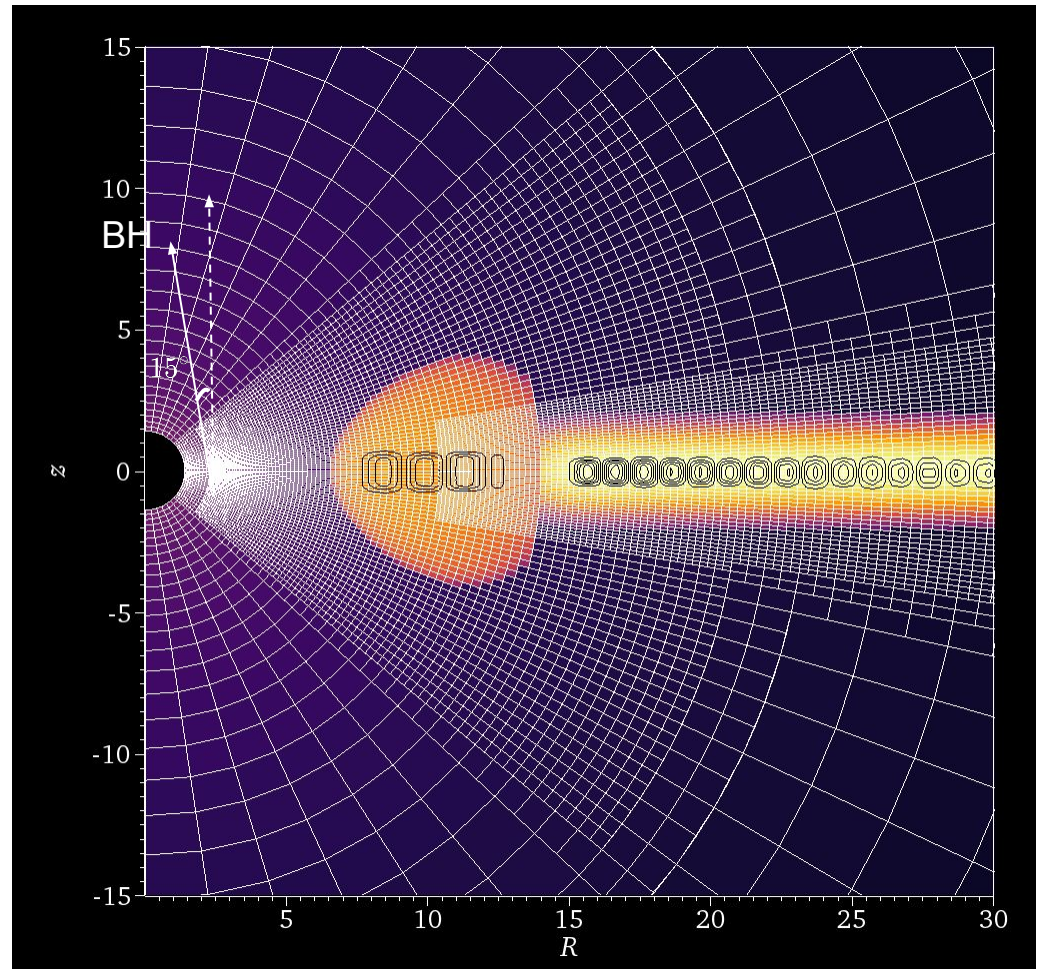
Ingram & Motta 2020

What happens when the outer thin disc present?



GRMHD simulations of Tilted & Truncated accretion disc

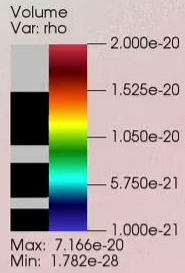
- Using GRMHD code *Cosmos++* (Anninos et al. 2005; Fragile et al. 2012, 2014)
- Initial setup
 - Torus surrounded by a thin slab at 15 gravitational radii
 - Artificial cooling implemented to maintain the slab structure with $H/r = 0.05$
 - Spinning black hole ($a = 0.9$) at a tilt of 15 degrees with respect to the disc.



Bollimpalli et. al (in preparation)

GRMHD simulations of Tilted & Truncated accretion disc

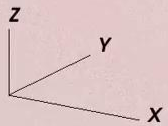
Volume
Var: rho



2.000e-20
1.525e-20
1.050e-20
5.750e-21
1.000e-21

Max: 7.166e-20
Min: 1.782e-28

The color scale shows a gradient from dark blue at the bottom (1.000e-21) to dark red at the top (2.000e-20). Intermediate values are marked at 5.750e-21, 1.050e-20, and 1.525e-20. The maximum value is 7.166e-20 and the minimum is 1.782e-28.



Time=0



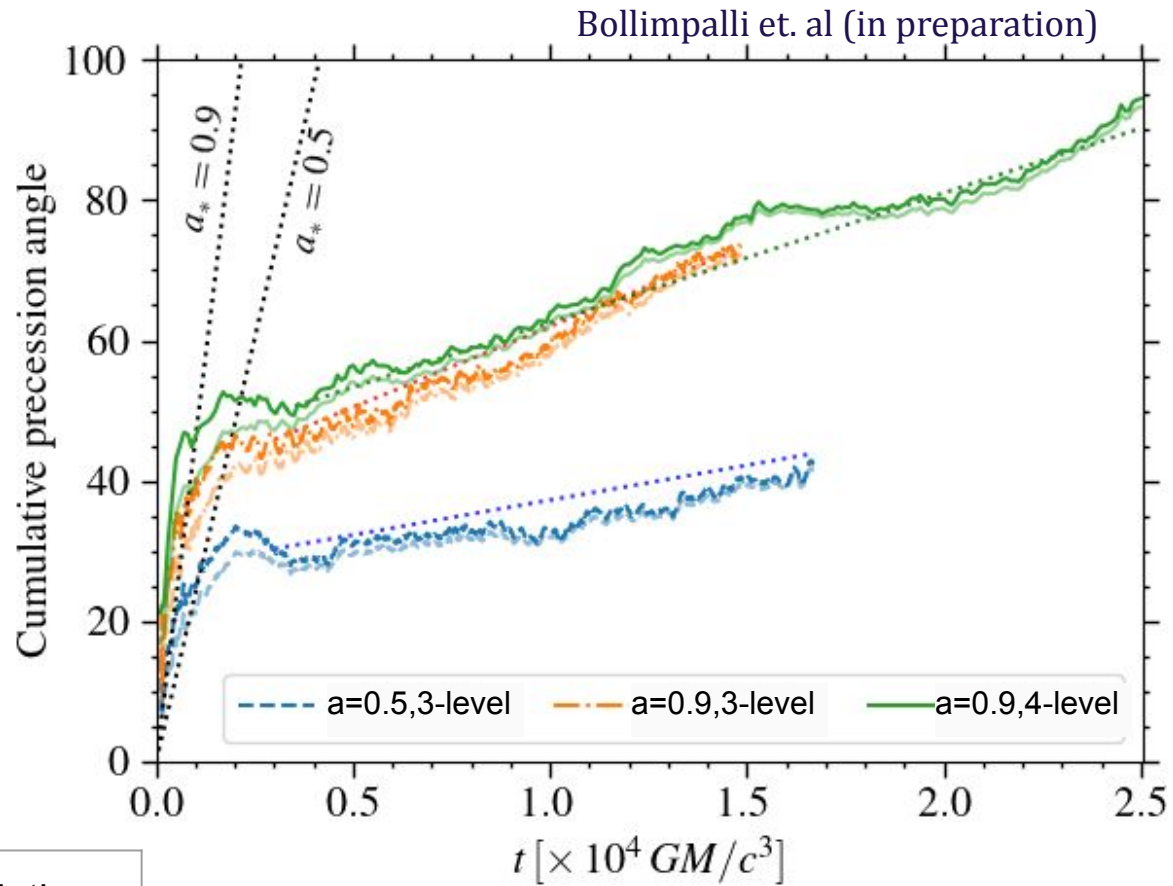
A horizontal, rounded rectangular bar representing the simulation domain at Time=0.

What is the effect of the outer disc?

➤ Expected precession rate
(Fragile et. al 2007; Ingram et. al 2009)

$$\Omega_{\text{prec}} = \frac{\int_{R_{\text{in}}}^{R_{\text{out}}} \Omega_{\text{LT}}(R) L(R) R dR}{\int_{R_{\text{in}}}^{R_{\text{out}}} L(R) R dR}$$

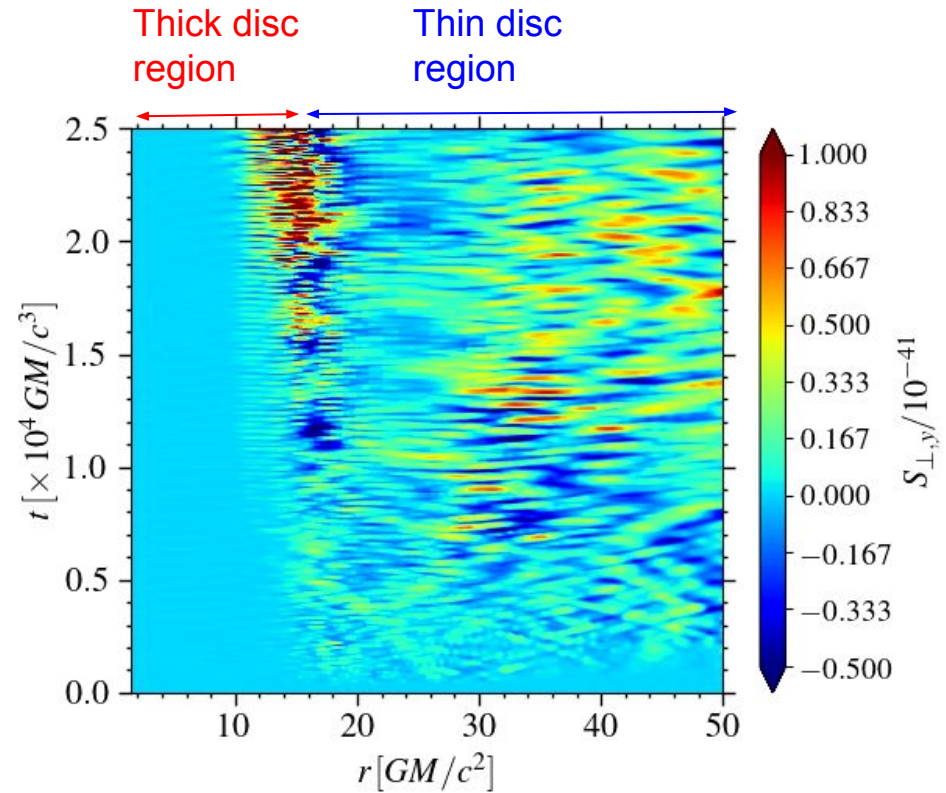
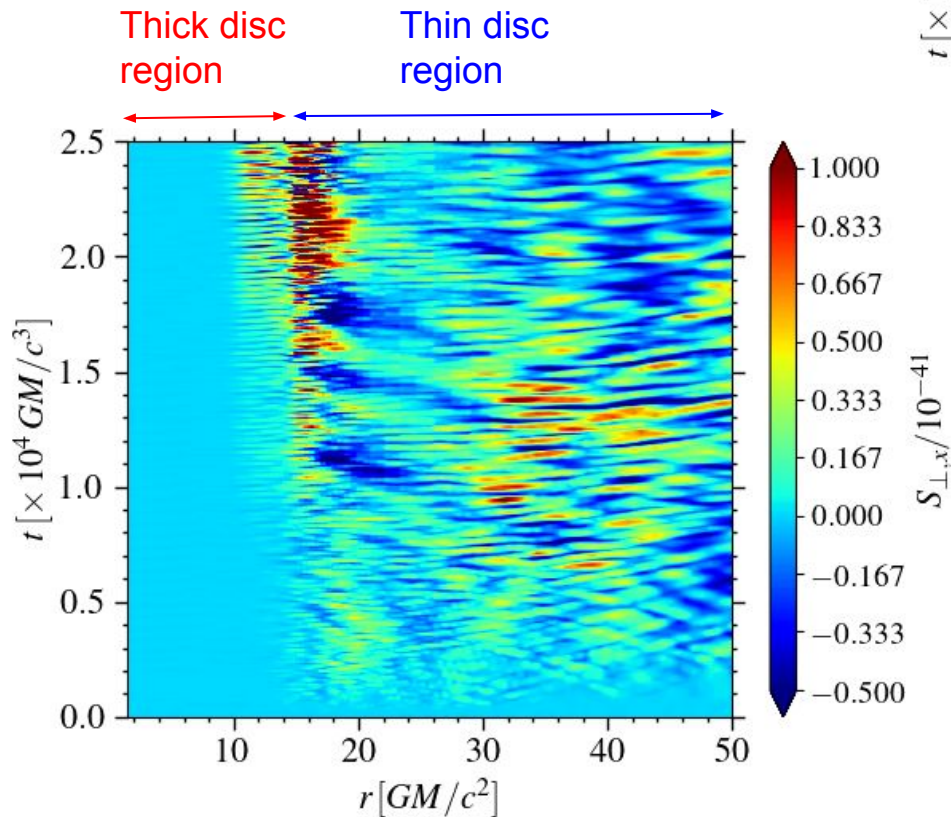
	Spin	Isolated torus (in Hz)	Simulation (in Hz)
3-level	0.5	8.5	0.3
	0.9	16.3	0.85
	0.9	16.7	0.74



Relative decrease in the precession rate is roughly 95 percent.

How is the outer thin disc affecting the precession rate?

Well, if the applied Lense-Thirring torque is used to transport the angular momentum outwards (Sorathia et. al 2013)

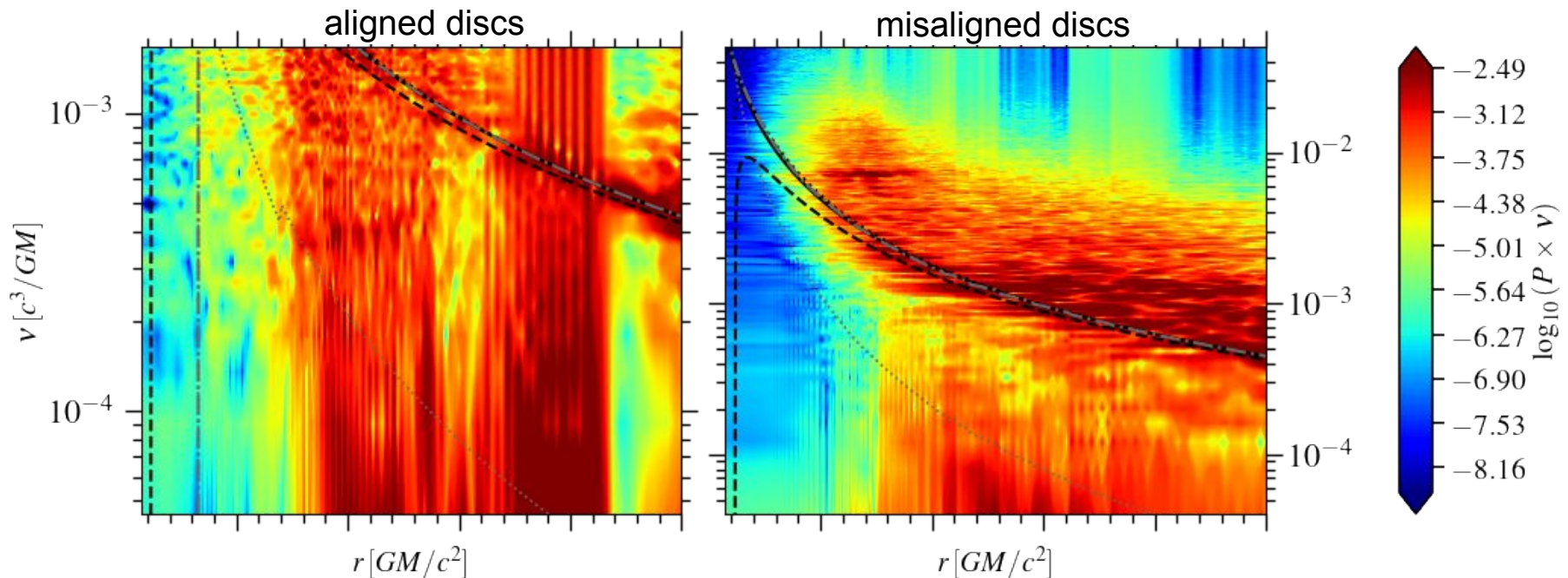


Increased angular momentum flux computed in the precessing plane.

Variability in misaligned accretion discs

- The accretion rate in the torus region is orders of magnitude lower when compared to the outer thin disc - *variability along the radial epicyclic frequency/ Keplerian frequency.*

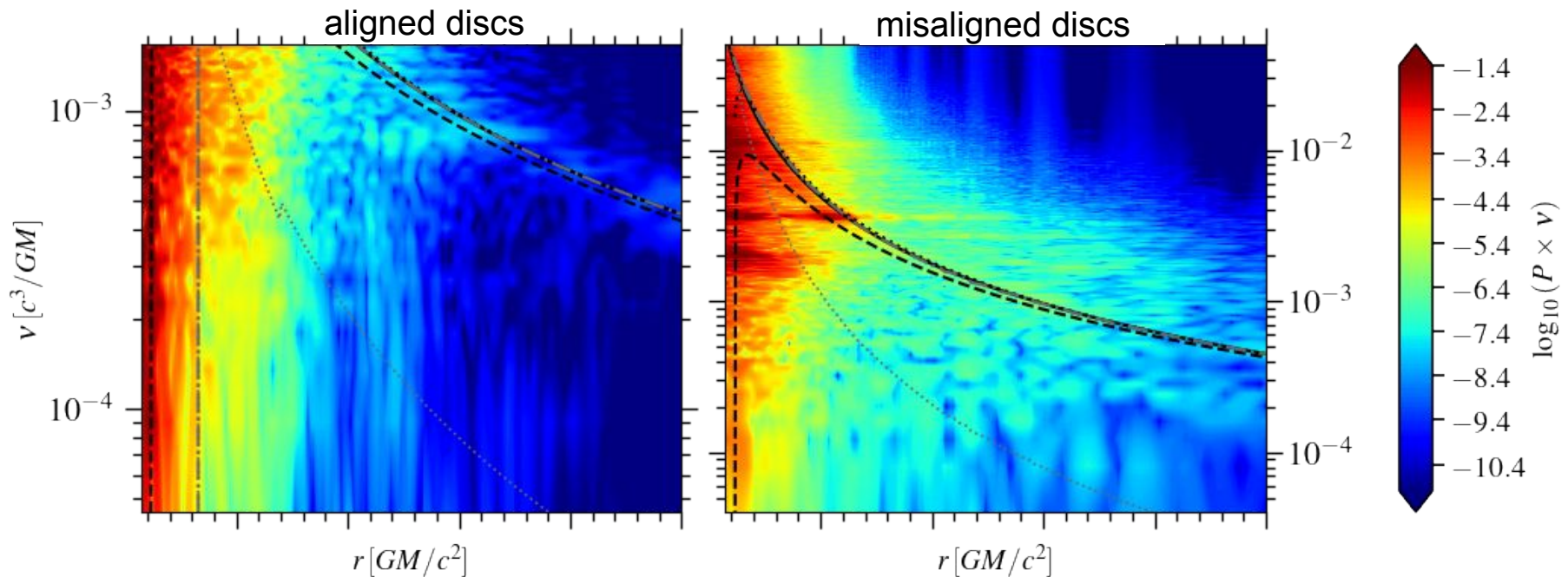
Power density spectra of accretion rate



Variability in misaligned accretion discs

- The accretion rate in the torus region is orders of magnitude lower when compared to the outer thin disc - *variability along the radial epicyclic frequency/ Keplerian frequency*.
- QPO-like features noted in misaligned discs; disc undergoing vertical oscillations. 40 Hz for a 10 solar mass BH.

Power density spectra of vertical velocity



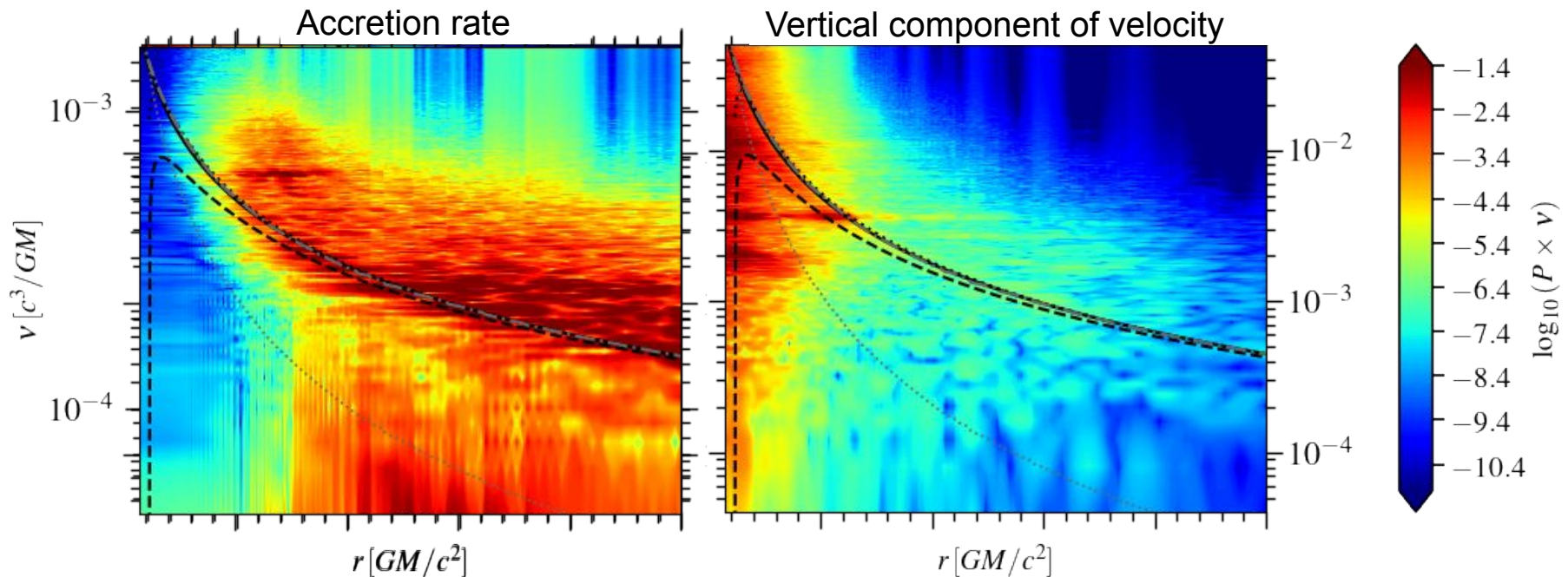
Variability in misaligned accretion discs

- The accretion rate in the torus region is orders of magnitude lower when compared to the outer thin disc - *variability along the radial epicyclic frequency/ Keplerian frequency*.
- QPO-like features noted in misaligned discs; disc undergoing vertical oscillations. 40 Hz for a 10 solar mass BH.

Are these trapped modes? Inertial or acoustic?

Are these oscillations related to the variability in accretion rate?

Power density spectra



- Mass accretion rate from non-radiative GRMHD simulations do show the evidence for *propagating fluctuations* theory.
 - Absorption mechanisms can also cause some variability; Radiative simulations
 - Disc-jet connection?
 - Understanding the frequency breaks in the power spectrum
- Simulations suggest that presence of **outer thin disc reduces the expected precession rate by nearly 95 percent.**
 - Could solve the problem of requirement of larger precessing, corona in systems like GRS 1915+105, MAXI J1535-571.
 - Does the outer thin disc break into rings? (Nixon et. al 2012, Liska et. al 2019)

Theory Simulations

Super-computing
power

Advanced numerical
techniques



Current & Future missions

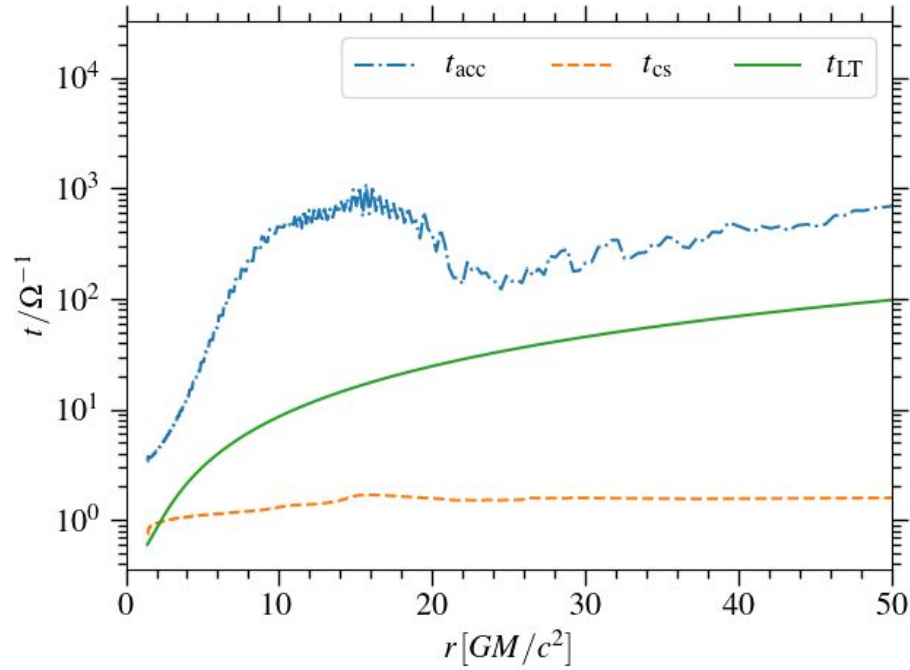
eXTP, HMXT

**Andrea
Santangelo's talk**

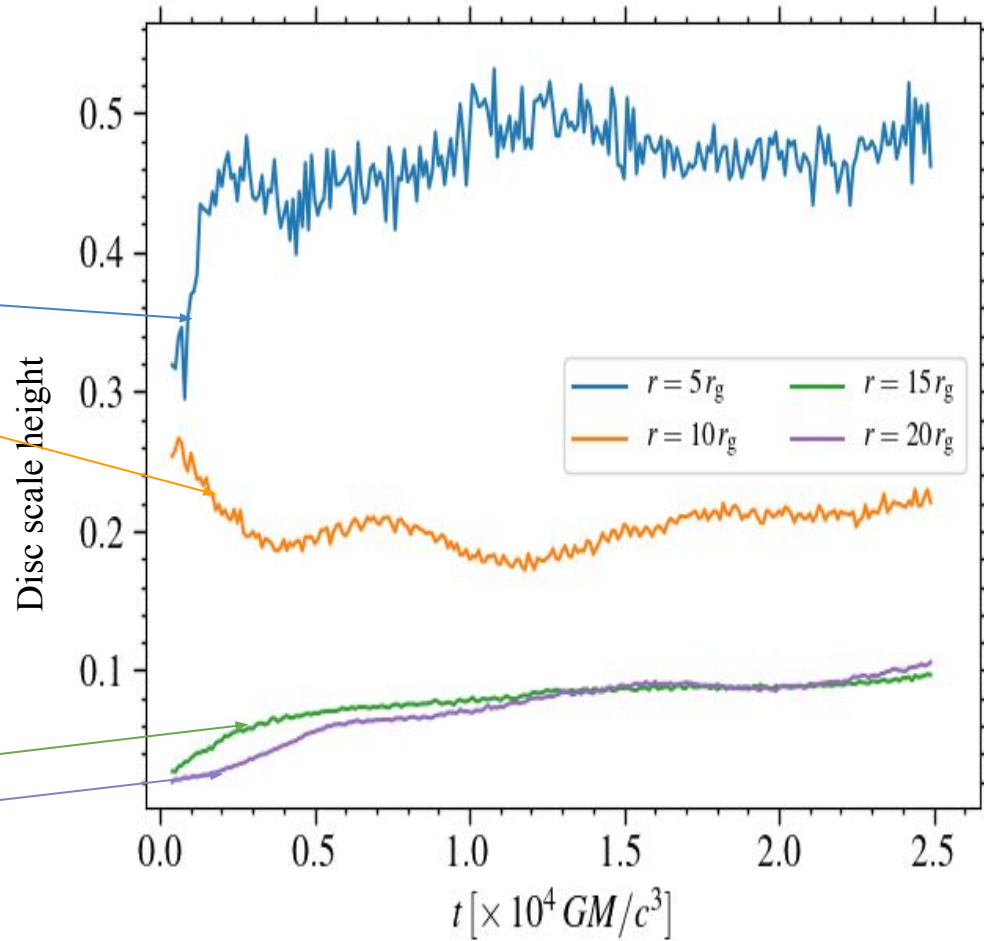
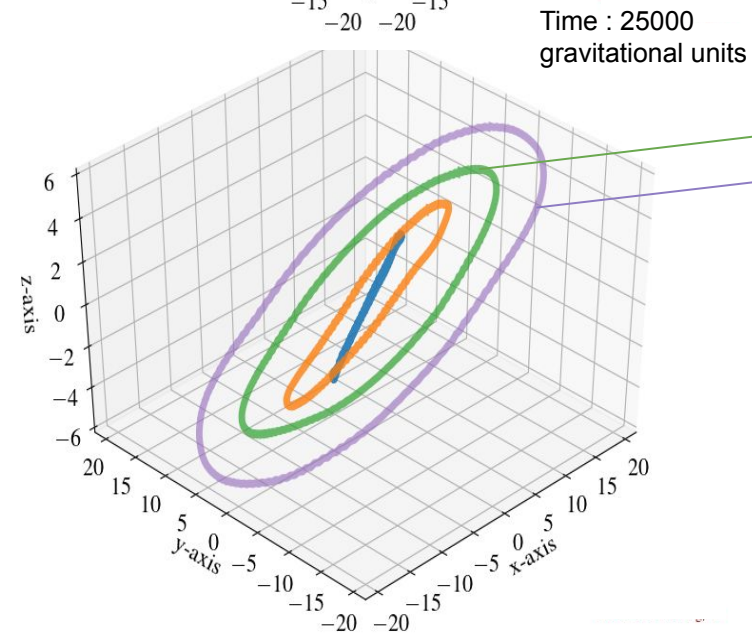
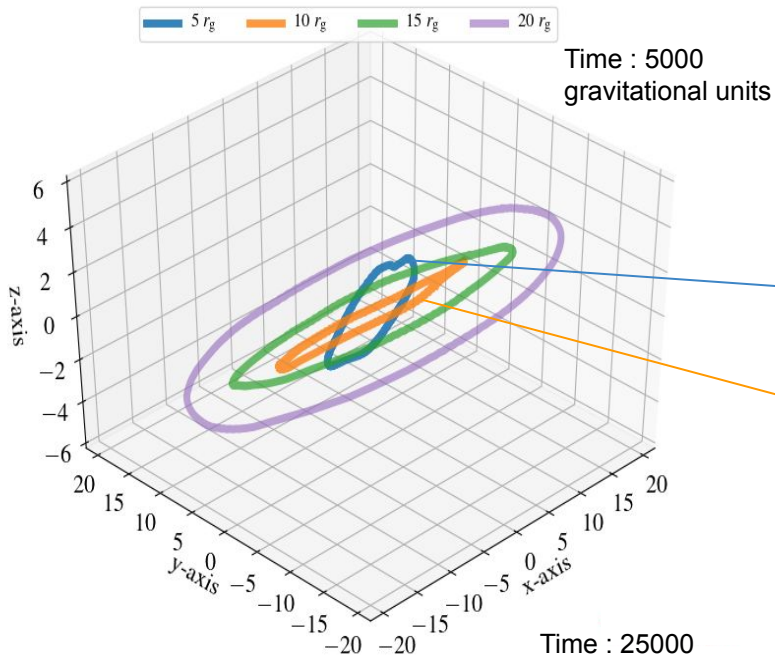
NICER, IXPE,
Astrosat

ATHENA,

Backup slides:



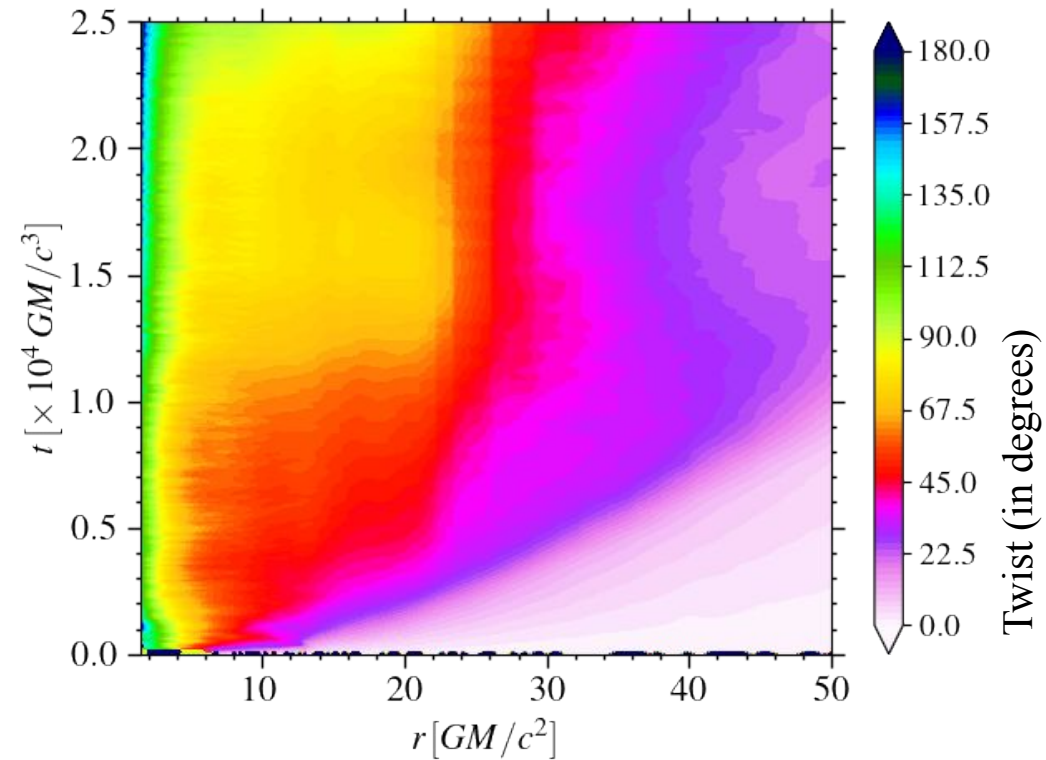
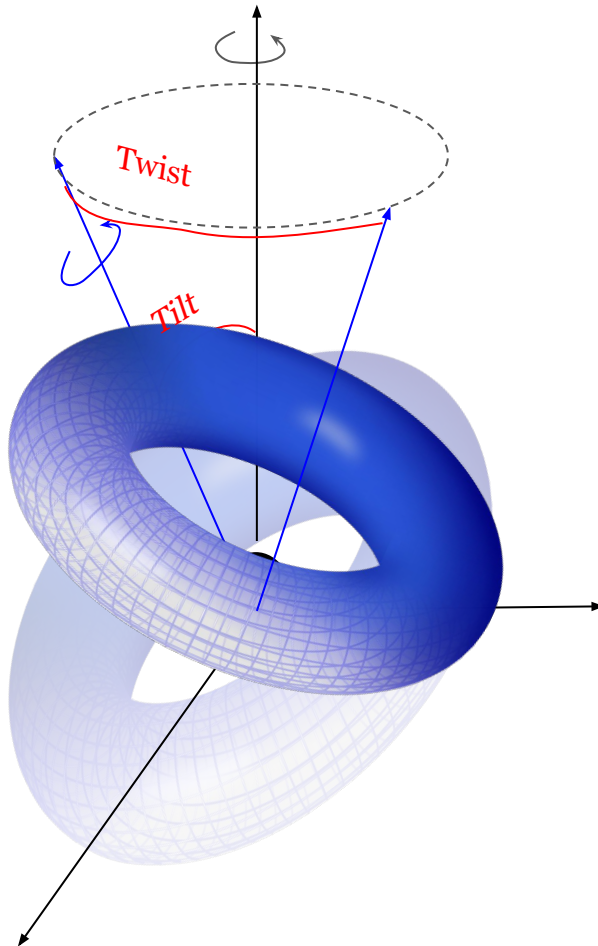
Does the flow really have truncated disc geometry?



➤ The two-component structure is maintained

Measuring precession : Twist angle

- Solid body precession in the torus region.
- The outer disc also undergoes precession, but at comparatively small rates.



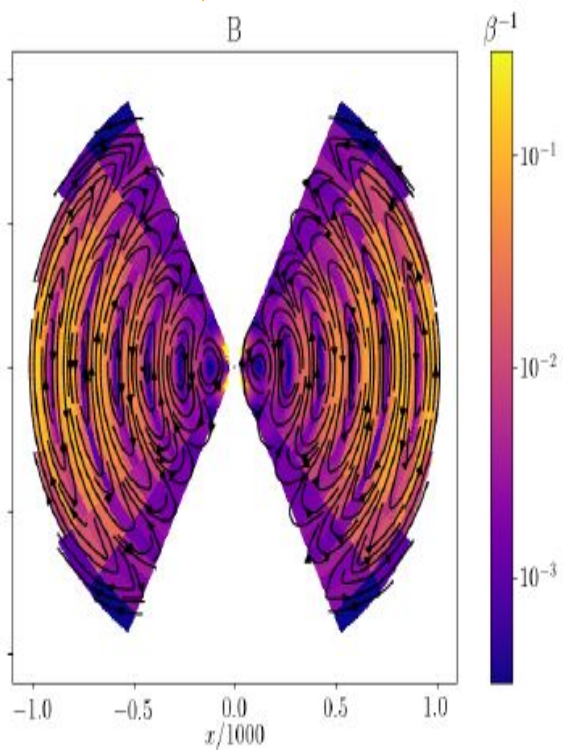
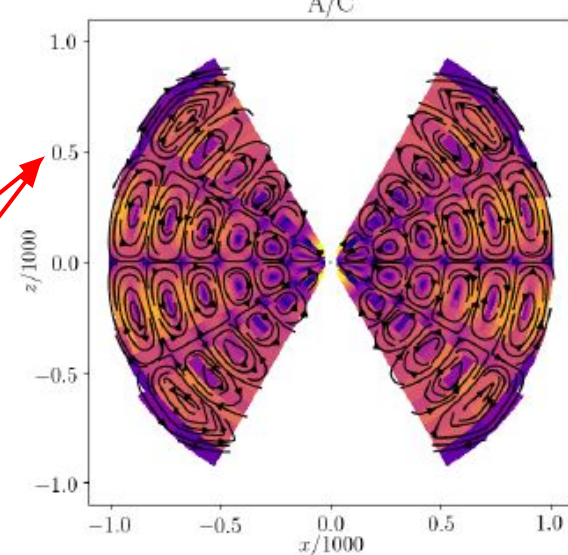
Numerical simulations

Athena++
(White et. al 2020)

HARM
(Narayan et. al 2012)

Cosmos++
(Bollimpalli et. al 2020)

Simulation	run length (GM/c^3)	r_{\max} (GM/c^2)	B field
Sim A	440,000	52	$N_r = 6, N_\theta = 4$
Sim B	220,000	52	$N_r = 6, N_\theta = 1$
Sim C	220,000	52	$N_r = 6, N_\theta = 4$
Sim R	200,000	20	$N_r = 8, N_\theta = 1$
Sim D	50,700	40	$N_r = 1, N_\theta = 1$



- The initial setups are different for all these simulations
- The resulting radiatively inefficient accretion flows are also different, particularly simulations A & C which have polar inflows and equatorial outflows.