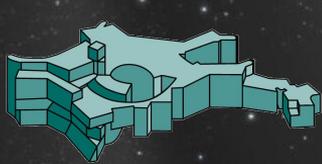


# Gravitational waves from quadruple stars - quadruple the fun! (?)

...



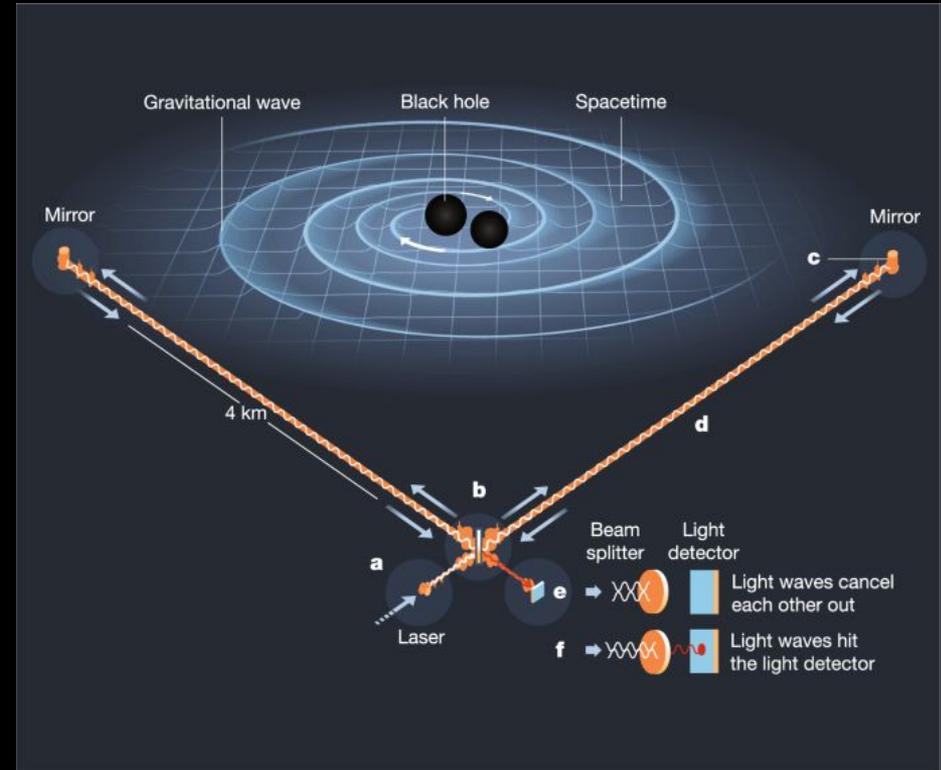
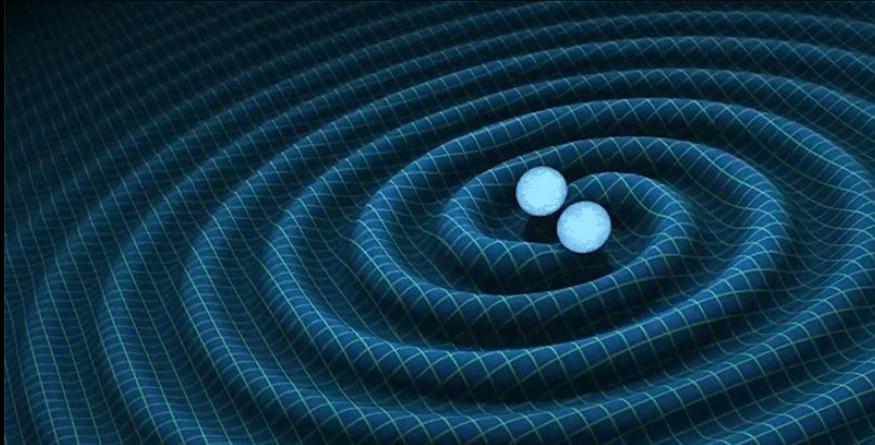
MAX PLANCK INSTITUTE  
FOR ASTROPHYSICS

Pavan Vynatheya  
MPA Garching, Germany

*Supervisor:* Dr. Adrian Hamers  
Multiple Stellar Evolution (MSE) group

# Gravitational waves (GWs)

- Ripples in spacetime
- Inspiral of **compact objects**
- Compact objects - black holes (BH), neutron stars (NS) are **remnants of massive stars**





# Compact object merger channels



Isolated binaries

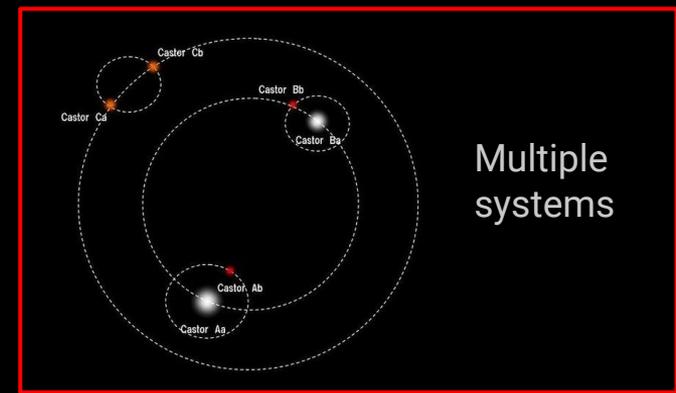


AGN disks



Clusters and stuff

Dynamical formation



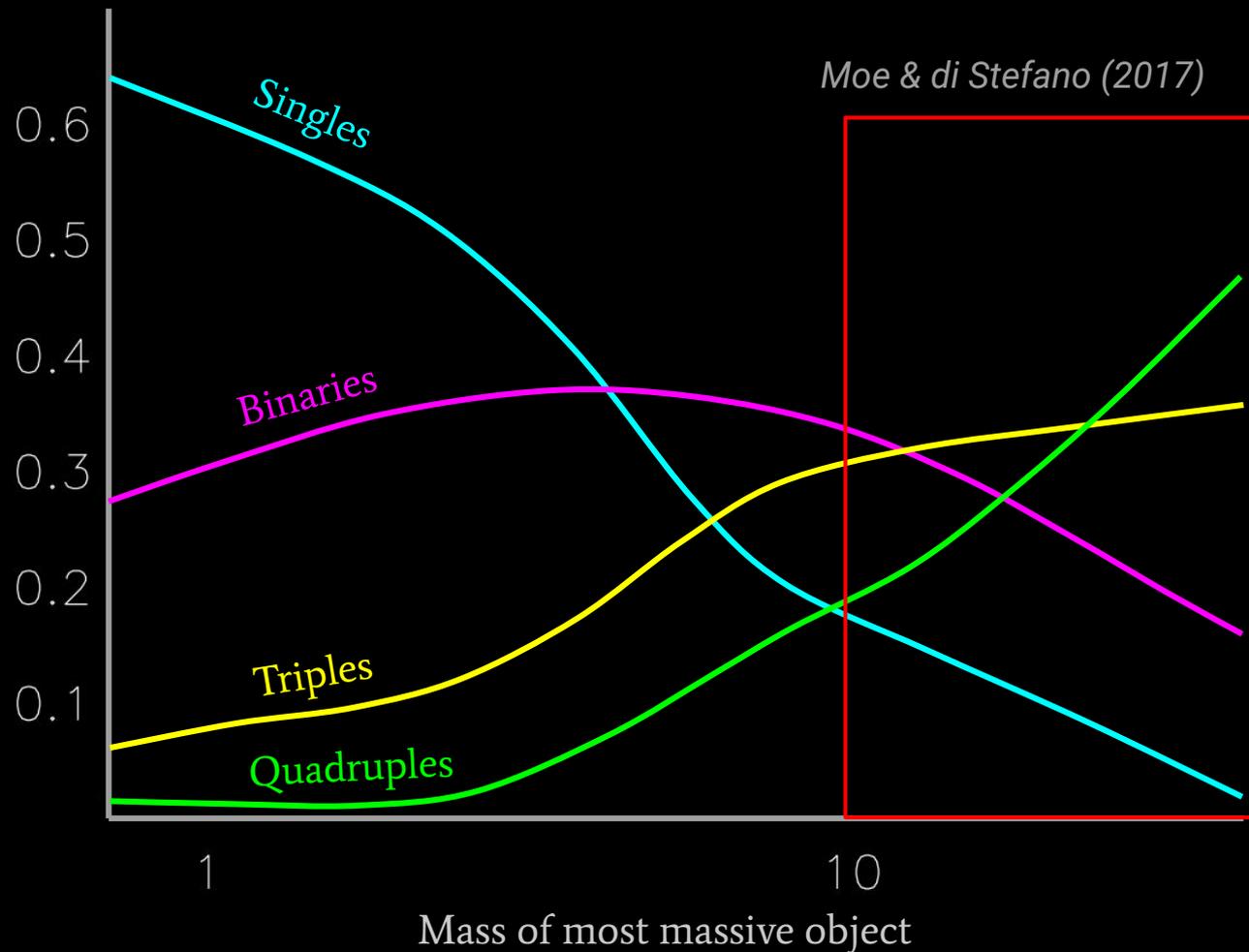
Multiple systems

# Why multiple-star systems (quadruples specifically)?

1. Massive stars are found mostly in multiple systems (triples and quadruples)

# 1. High multiple fraction

Multiplicity fraction

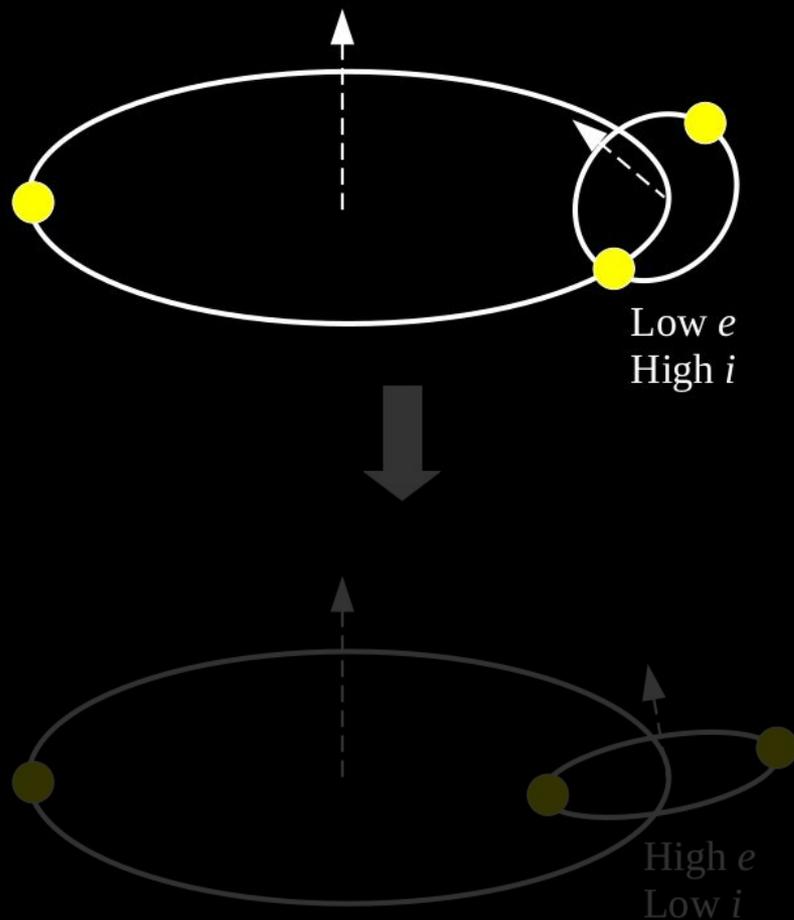


# Why multiple-star systems (quadruples specifically)?

1. Massive stars are found mostly in multiple systems (triples and quadruples)
2. Possible eccentricity enhancements due to interactions → closer approaches for mergers

## 2. Eccentricity enhancement

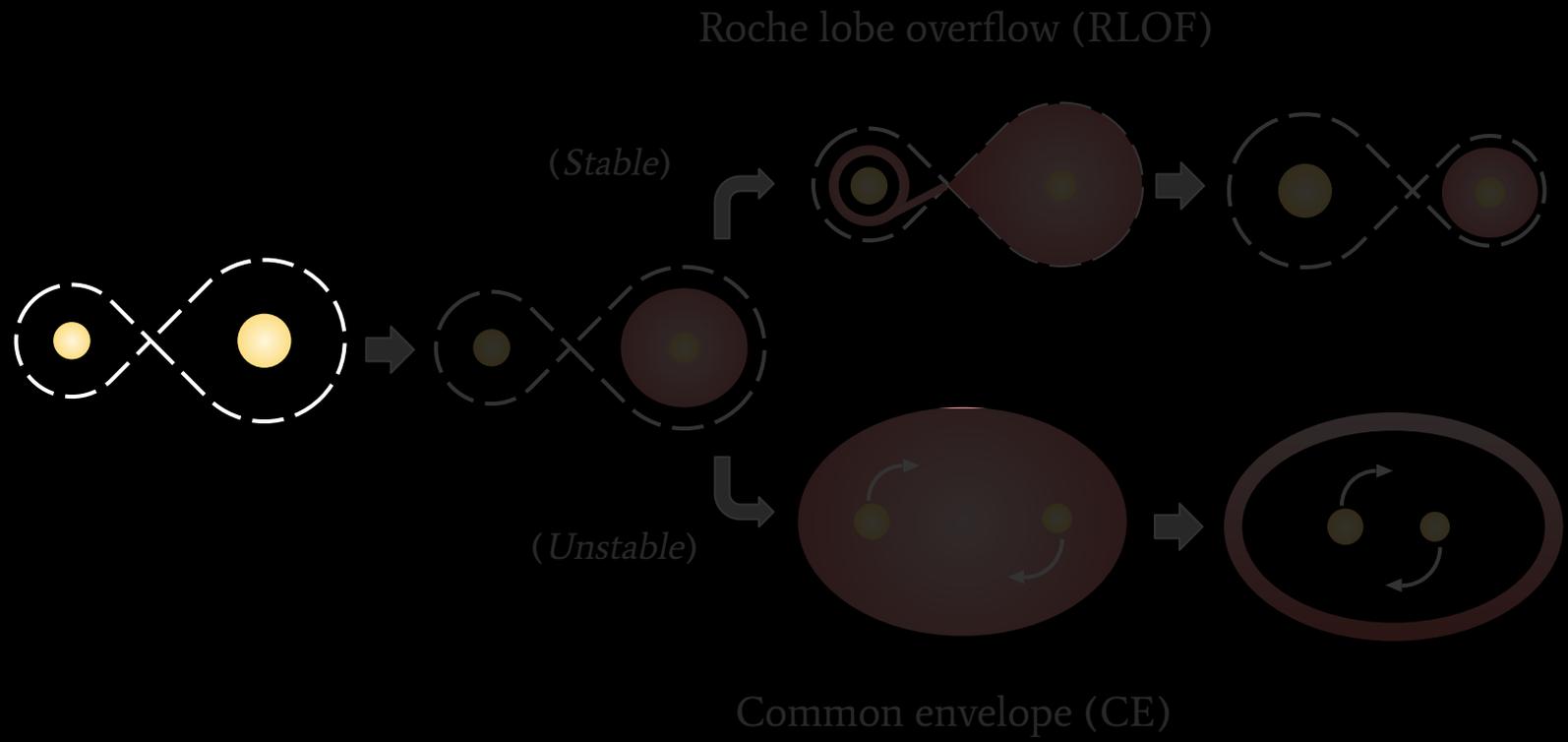
- **Secular evolution**
- **von Zeipel-Lidov-Kozai (ZLK) oscillations**
- Maximum eccentricity depends on initial mutual inclination
- Larger parameter space for secular effects in quadruples (*Hamers & Lai 2018*)



# Why multiple-star systems (quadruples specifically)?

1. Massive stars are found mostly in multiple systems (triples and quadruples)
2. Possible eccentricity enhancements due to interactions → closer approaches for mergers
3. Binary evolution plays an important role as well

# 3. Binary evolution

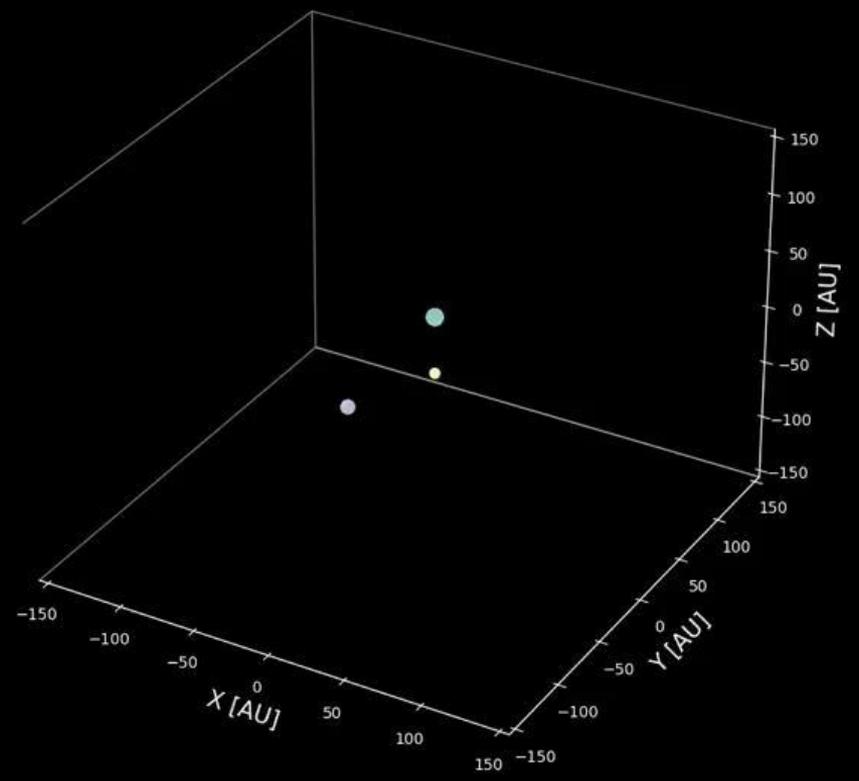


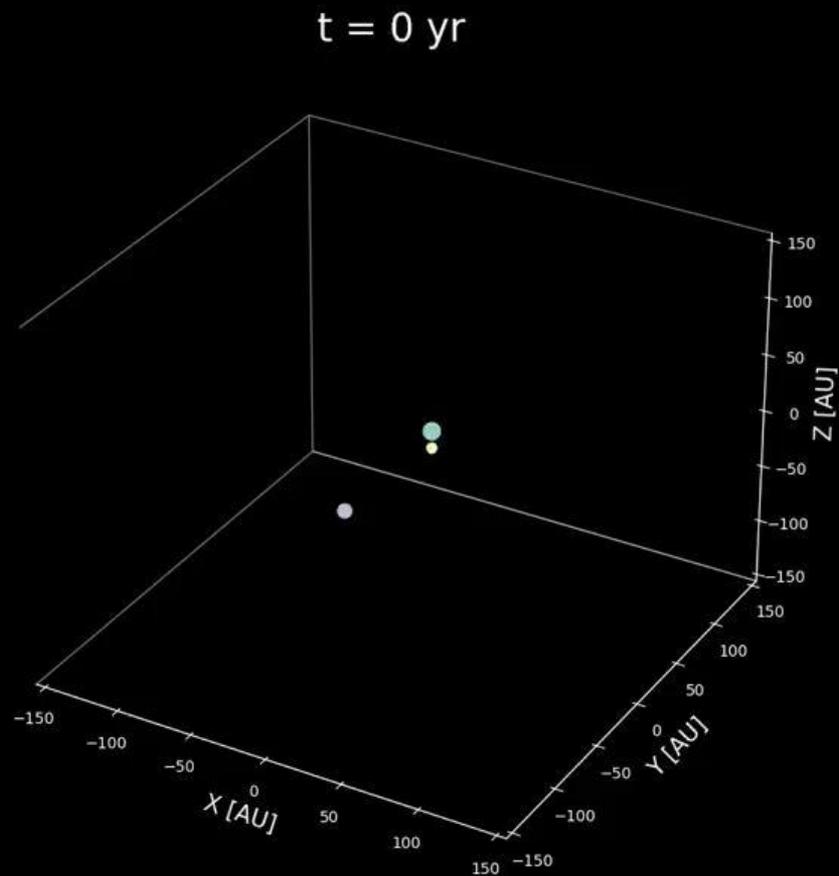
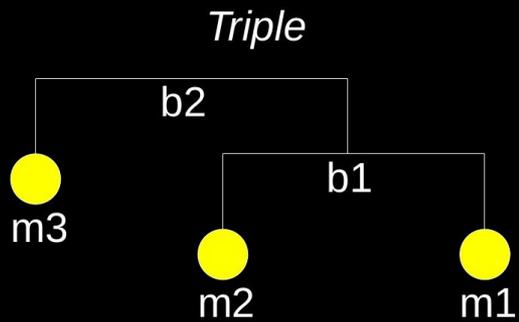
# Why multiple-star systems (quadruples specifically)?

1. Massive stars are found mostly in multiple systems (triples and quadruples)
2. Possible eccentricity enhancements due to interactions → closer approaches for mergers
3. Binary evolution plays an important role as well
4. The more, the merrier!

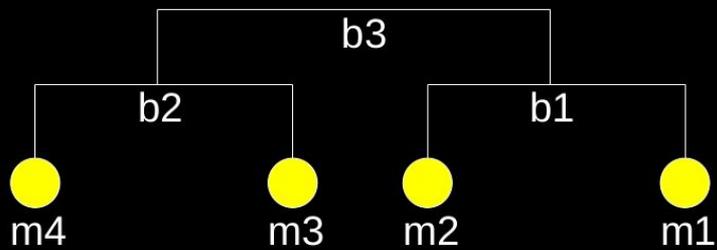
t = 0 yr

*Non-hierarchical  
Triple (unstable)*

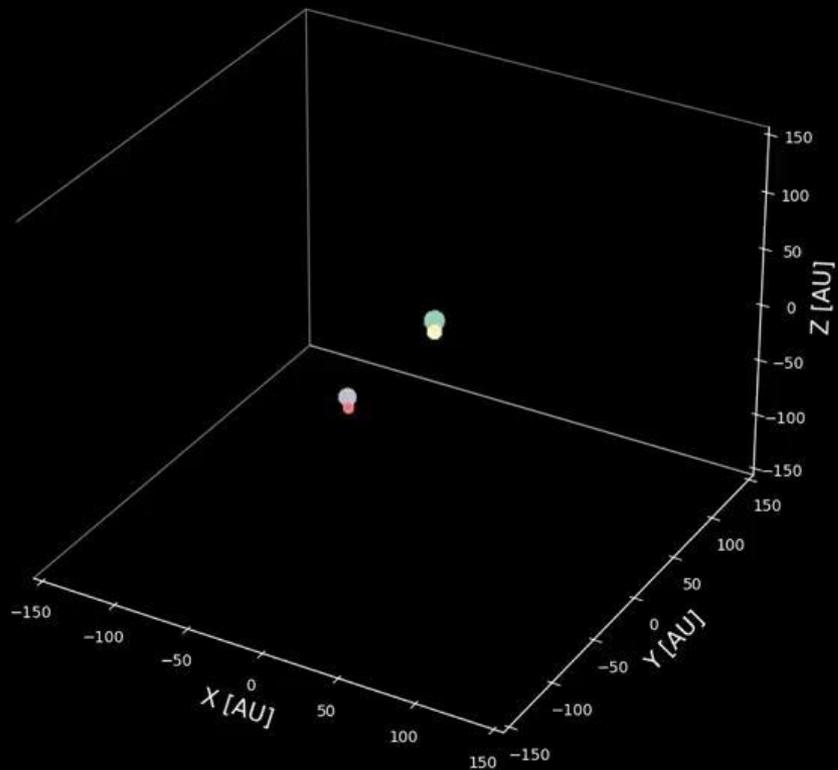


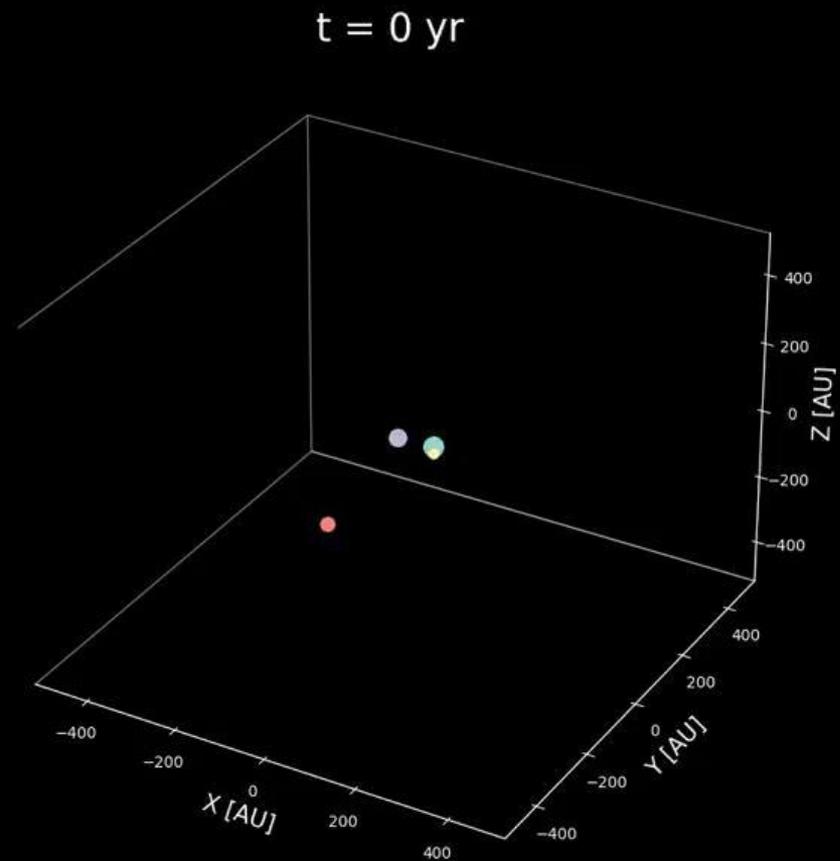
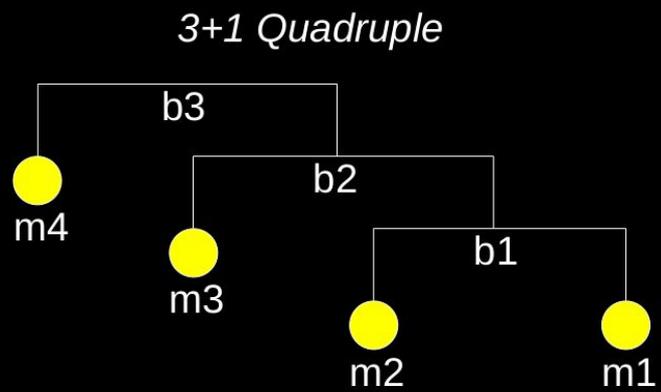


*2+2 Quadruple*



t = 0 yr



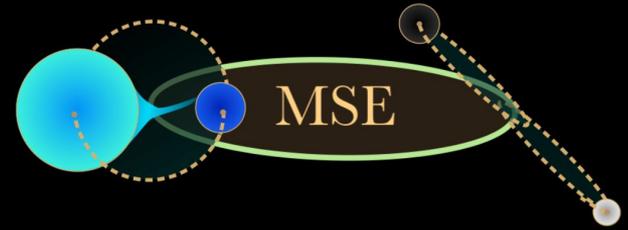


# Project outline

Refer to *Vynatheya & Hamers (2022)*  
(ApJ, 926, 195V)

- ❖ Population synthesis using MSE code (*next slide*)
  - ❖ (2+2) quadruples compared with isolated binaries (same initial conditions)
  - ❖ (3+1) quadruples
  - ❖ Look for BH-BH, BH-NS or NS-NS ‘mergers’
-

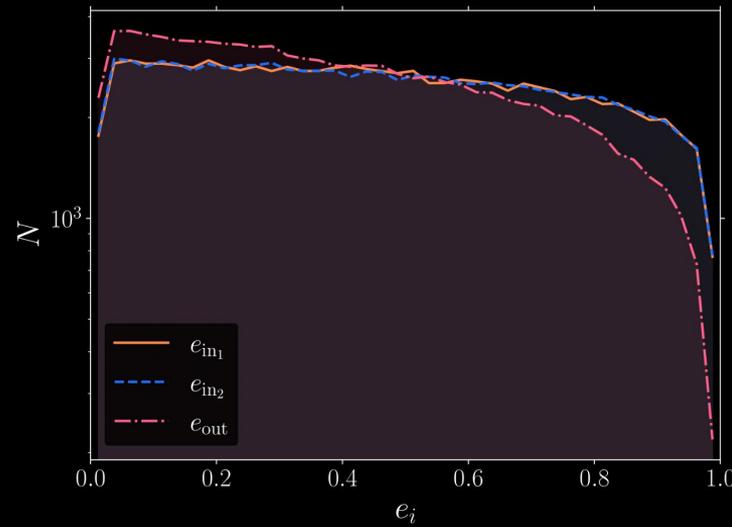
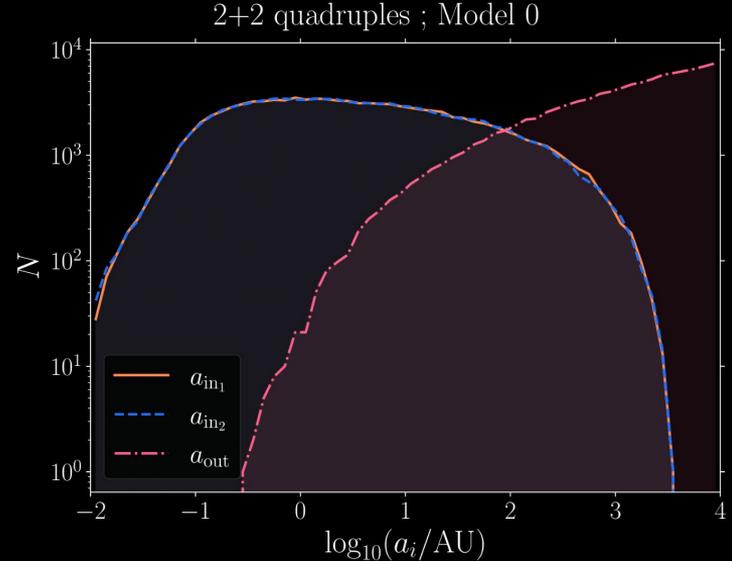
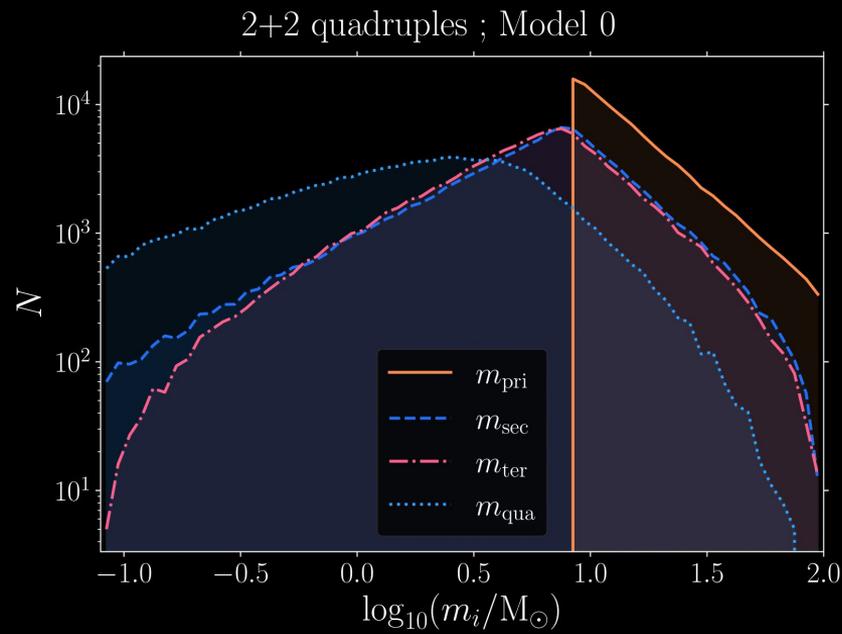
# Population synthesis : MSE code



- ‘Multiple Stellar Evolution’ by *Hamers et al. (2021)*
- **Stellar evolution + dynamics**
- Two modes - **secular** (orbit averaged) and **direct  $N$ -body** integration
- Uses SSE (*Hurley et al. 2000*) for **stellar evolution tracks**, and improves upon BSE (*Hurley et al. 2002*) for **binary events**
- Features – eccentric mass transfer, effect of flybys, triple mass transfer/CE evolution, equilibrium tides, supernova kicks

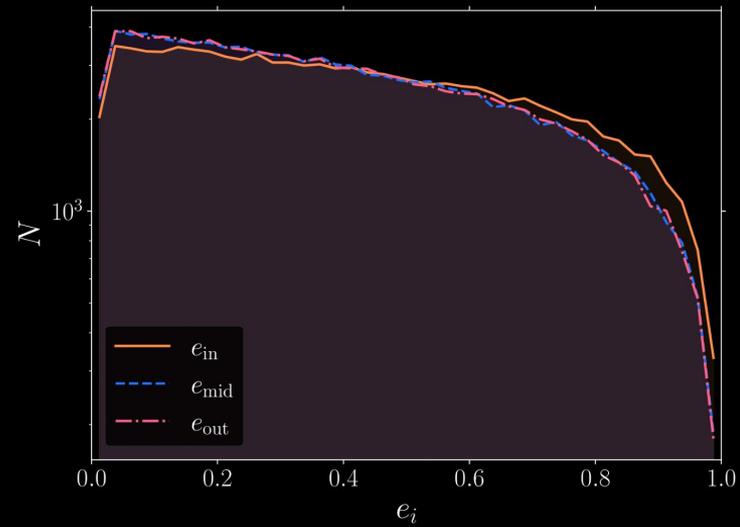
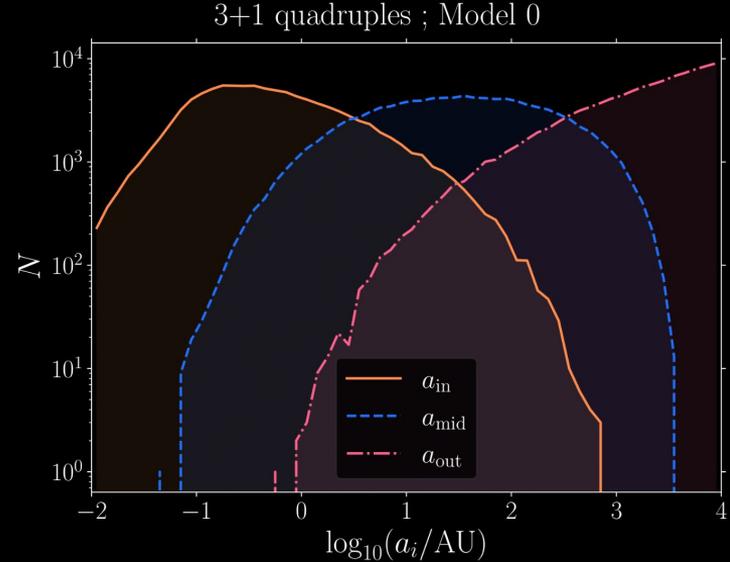
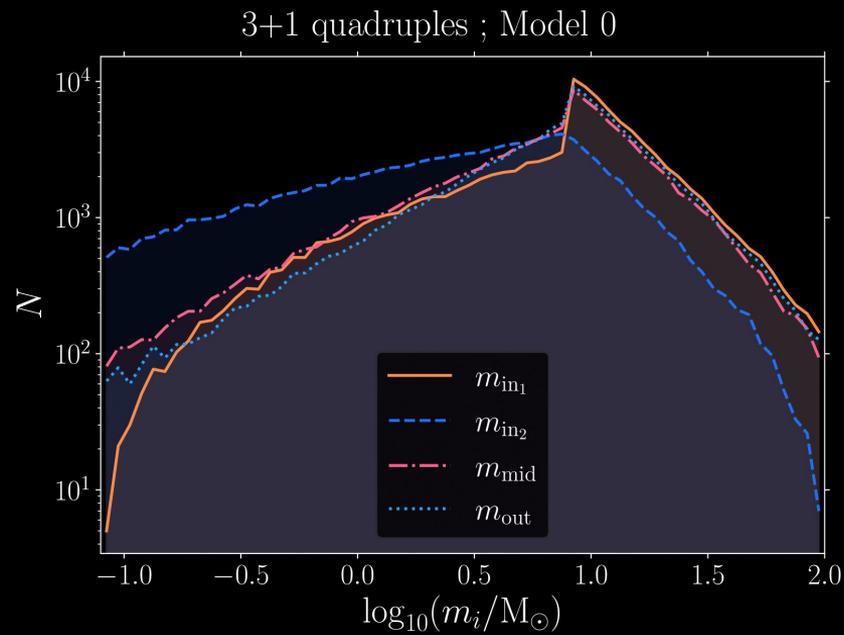
# Initial conditions: 2+2 quadruples

- 100,000 2+2 quadruples & 200,000 isolated binaries
- $m$  - Kroupa (2001);  $a$  - log flat;  $e$  - flat; isotropic



# Initial conditions: 3+1 quadruples

- 100,000 3+1 quadruples
- $m$  - Kroupa (2001);  $a$  - log flat;  $e$  - flat; isotropic

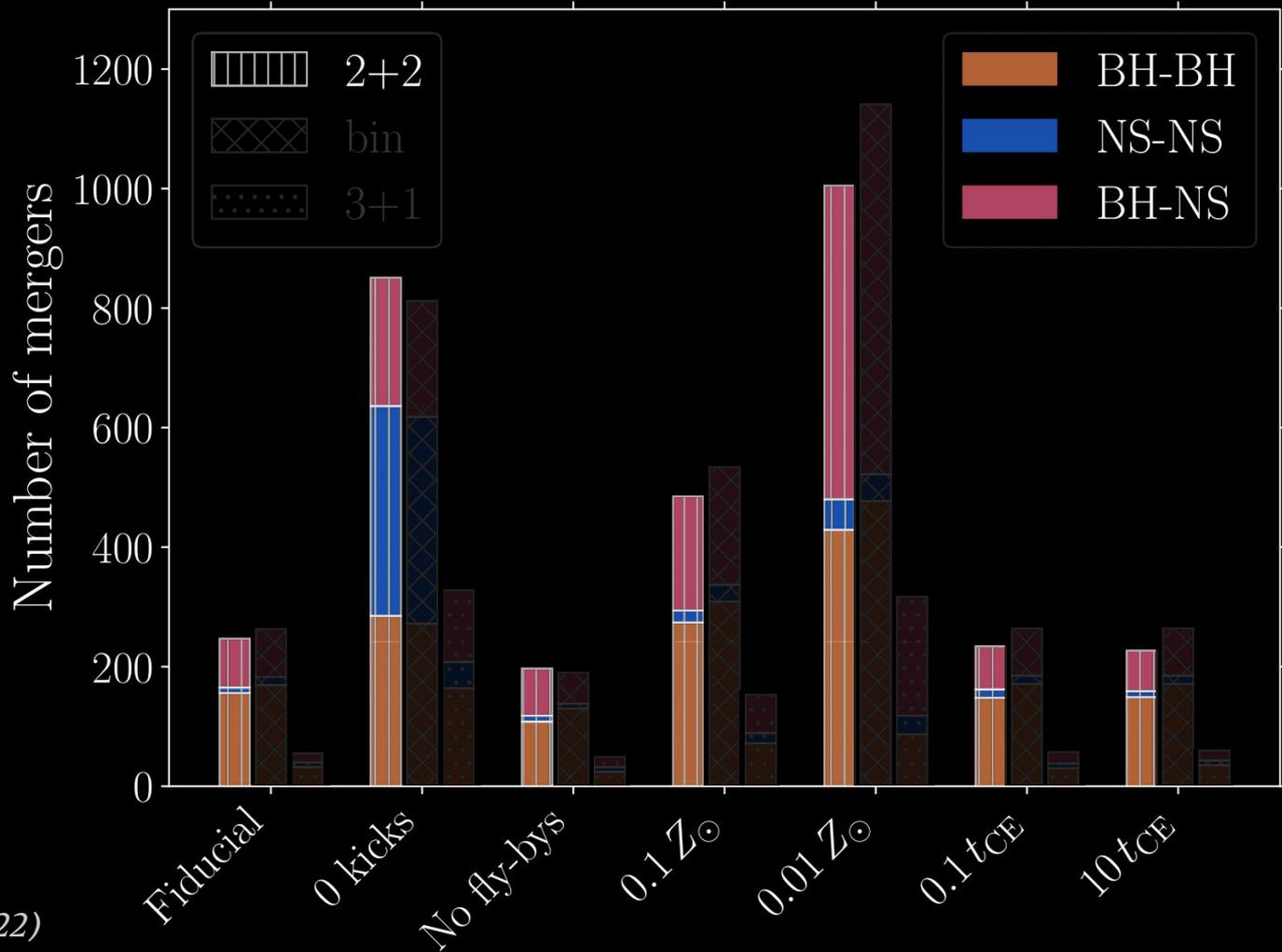


# Different models

Model	SNe kicks	fly-bys	Metallicity $Z$	CE timescale $t_{\text{CE}}$
0	non-zero	included	$2 \times 10^{-2}$	$10^3$ yr
1	<b>zero</b>	included	$2 \times 10^{-2}$	$10^3$ yr
2	non-zero	<b>excluded</b>	$2 \times 10^{-2}$	$10^3$ yr
3a	non-zero	included	<b><math>2 \times 10^{-3}</math></b>	$10^3$ yr
3b	non-zero	included	<b><math>2 \times 10^{-4}</math></b>	$10^3$ yr
4a	non-zero	included	$2 \times 10^{-2}$	<b><math>10^2</math> yr</b>
4b	non-zero	included	$2 \times 10^{-2}$	<b><math>10^4</math> yr</b>

*Vynatheya & Hamers (2022)*

# Merger numbers



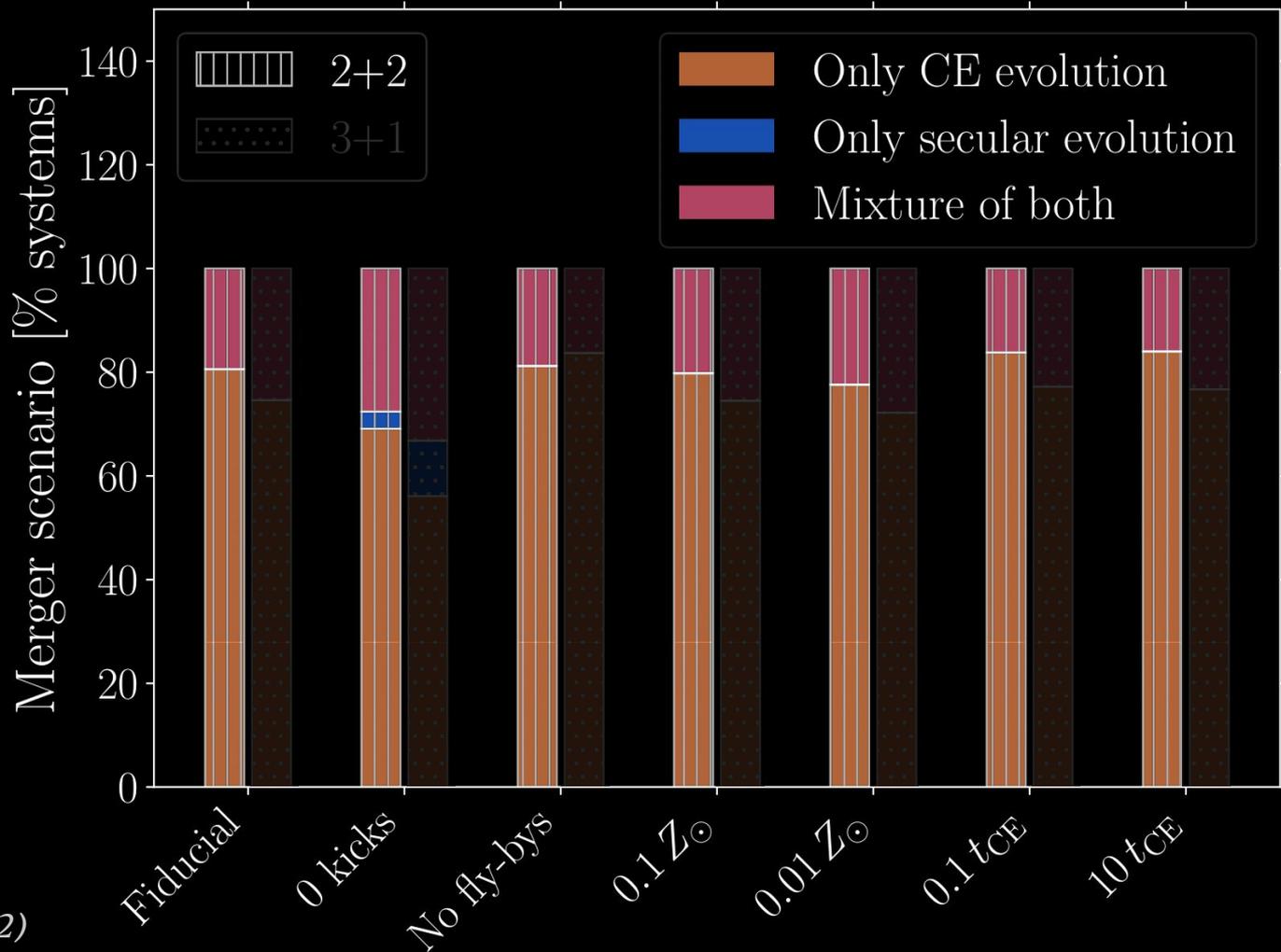
# Merger rates

For our fiducial model (in units of  $\text{Gpc}^{-3}\text{yr}^{-1}$ )

Merger type	2+2 quadruples	3+1 quadruples	<b>LIGO</b> (GWTC-3)
<b>BH-BH</b>	$10.8 \pm 0.9$	$2.9 \pm 0.5$	<b>173 – 45</b>
<b>BH-NS</b>	$5.7 \pm 0.6$	$1.4 \pm 0.4$	<b>74 – 320</b>
<b>NS-NS</b>	$0.6 \pm 0.2$	$0.7 \pm 0.3$	<b>13 – 1900</b>

*Vynatheya & Hamers (2022)*

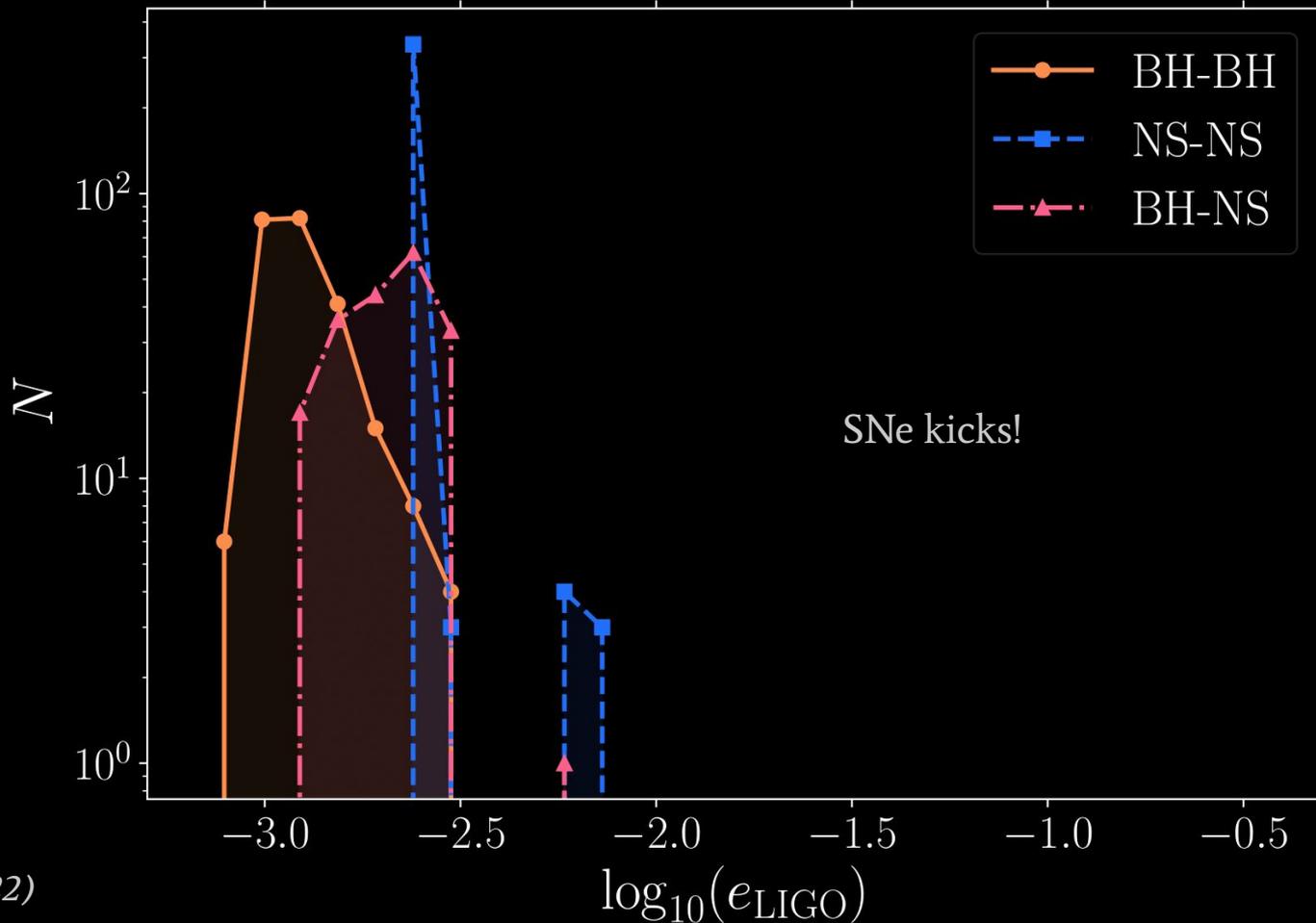
# Merger scenarios



## Binaries ; Model 1

 $e_{\text{LIGO}}$  dist.

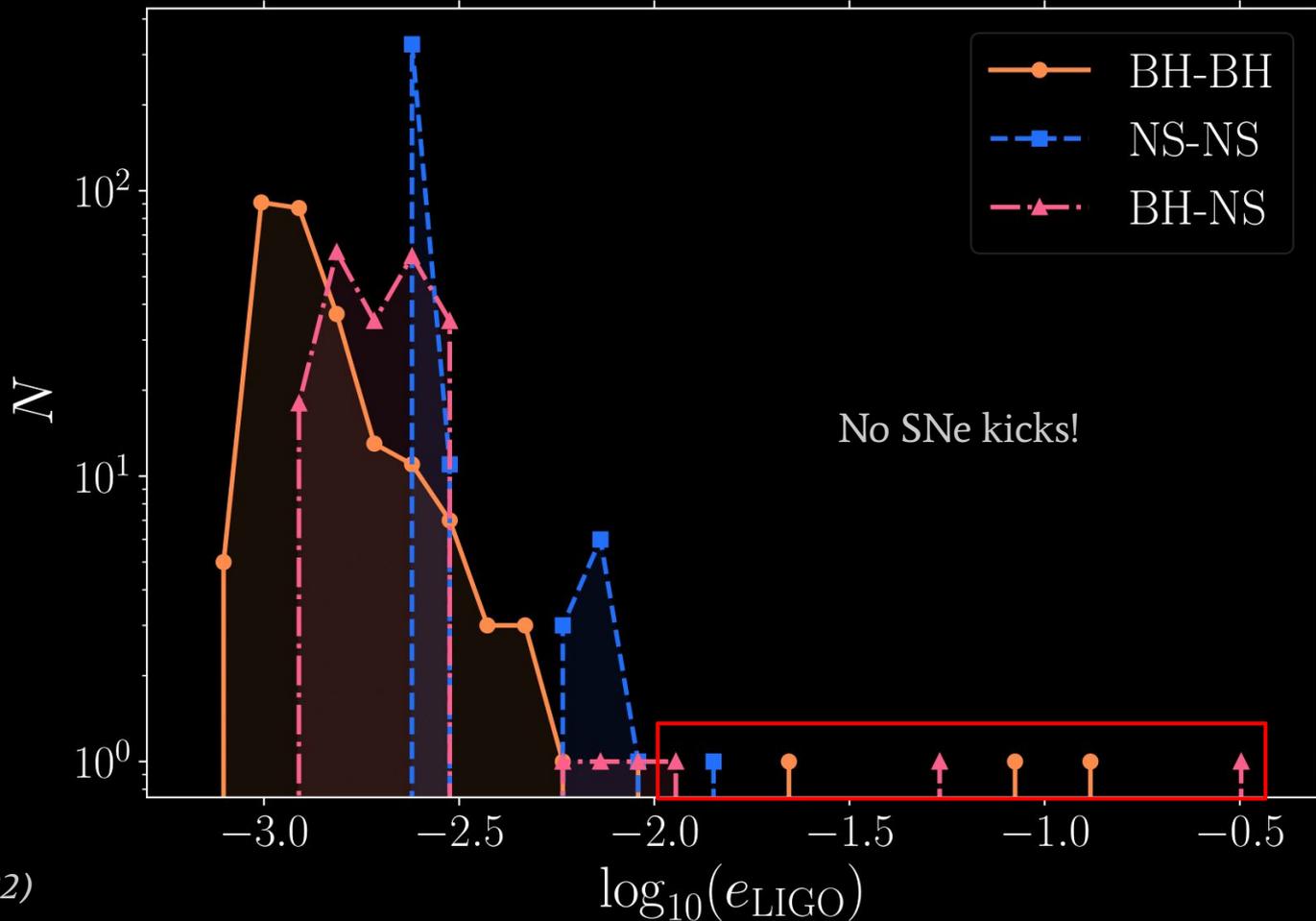
(LIGO band eccentricities)



## 2+2 quadruples ; Model 1

 $e_{\text{LIGO}}$  dist.

(LIGO band eccentricities)



## Binaries ; Model 1

$\chi_{\text{eff}}$  dist.  
(effective spin  
parameters)

$N$

$10^1$

SNe kicks!

-1.00

-0.75

-0.50

-0.25

0.00

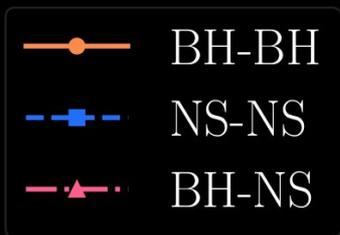
0.25

0.50

0.75

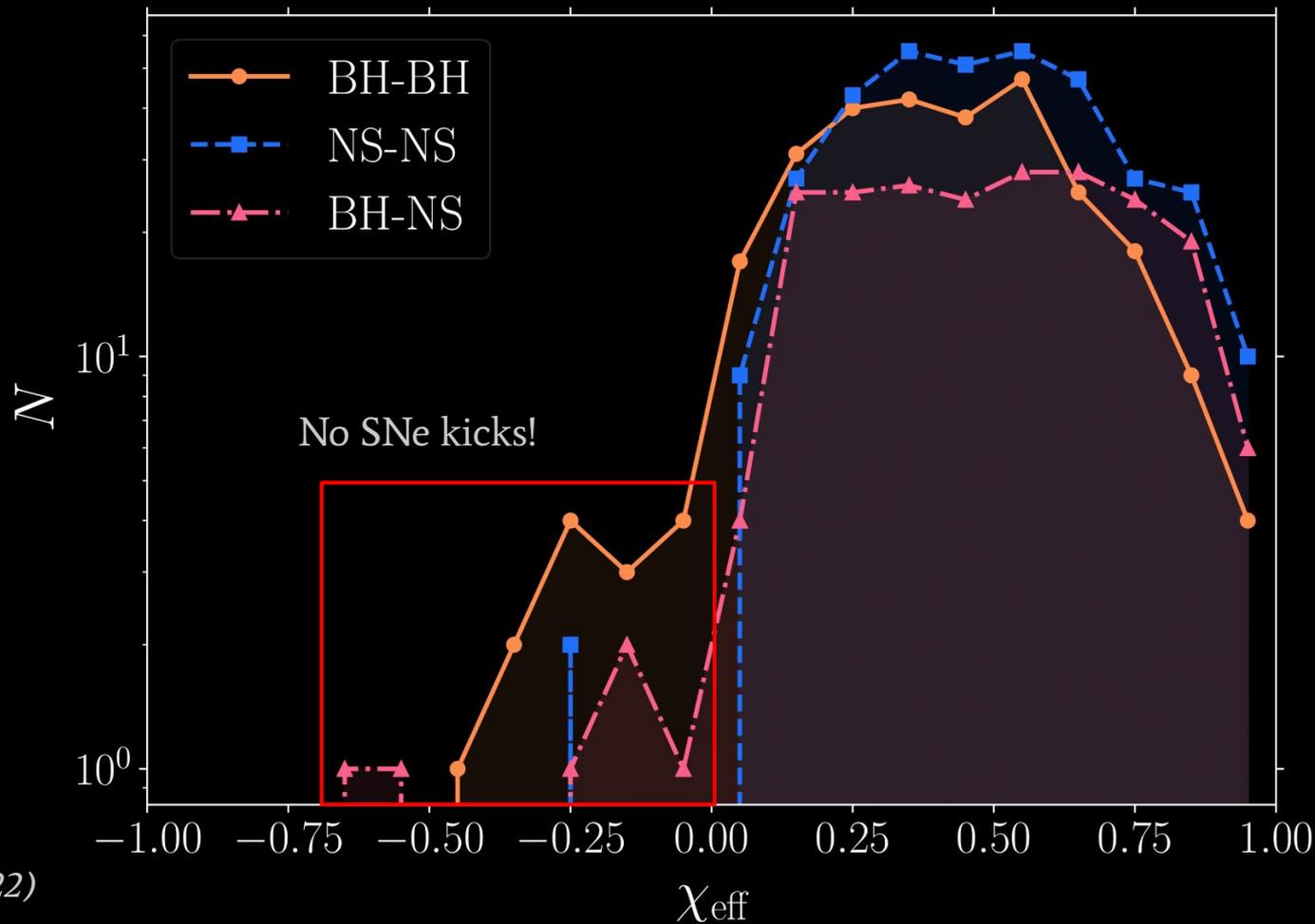
1.00

$\chi_{\text{eff}}$



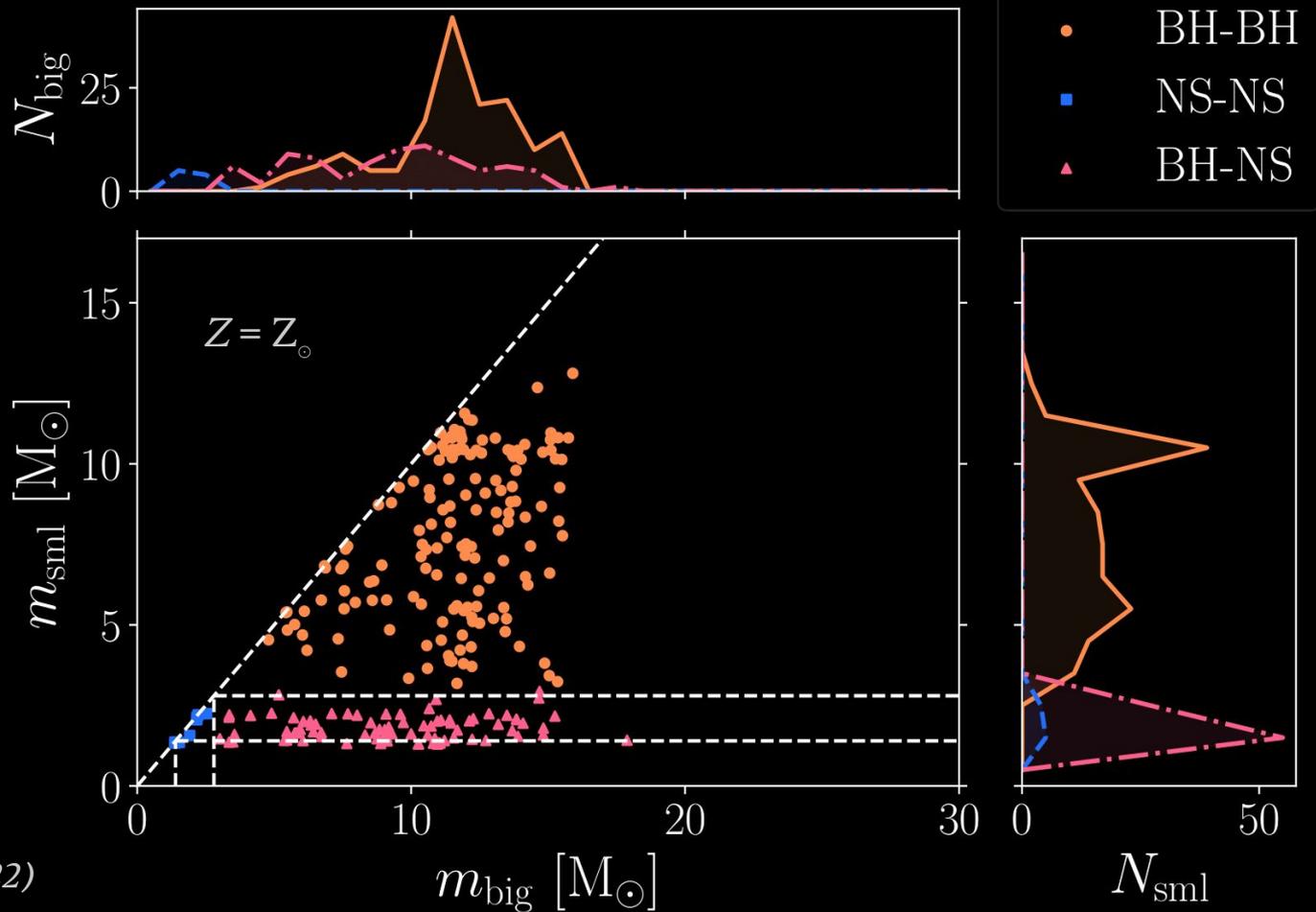
## 2+2 quadruples ; Model 1

$\chi_{\text{eff}}$  dist.  
(effective spin  
parameters)



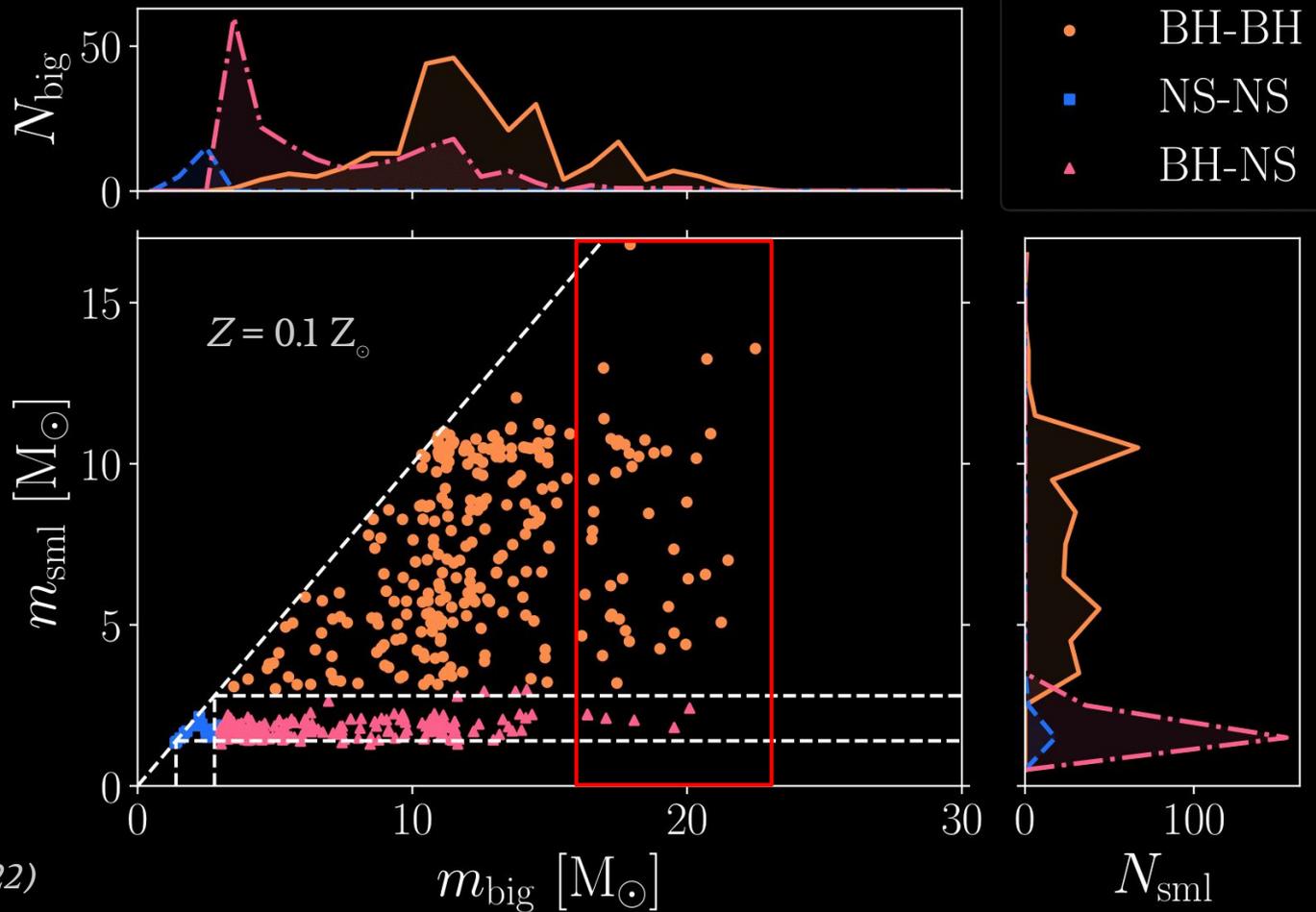
## 2+2 quadruples ; Model 0

$m_{\text{pri}}$  vs.  
 $m_{\text{sec}}$   
 (pre-merger masses)



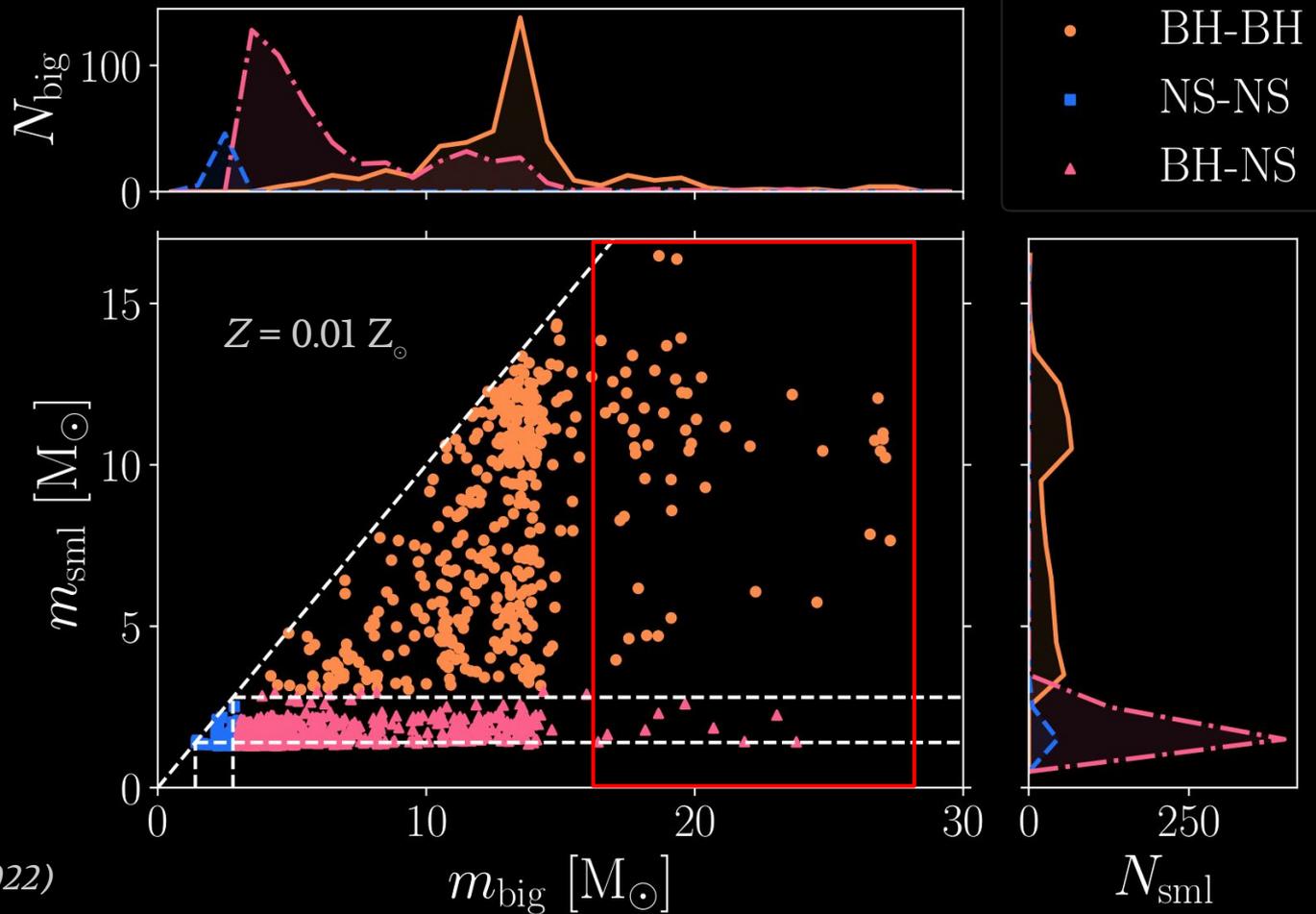
## 2+2 quadruples ; Model 3a

$m_{\text{pri}}$  vs.  
 $m_{\text{sec}}$   
 (pre-merger masses)



## 2+2 quadruples ; Model 3b

$m_{\text{pri}}$  vs.  
 $m_{\text{sec}}$   
 (pre-merger masses)



# Summary

Refer to *Vynatheya & Hamers (2022)*  
(ApJ, 926, 195V)

- ❖ BH-BH rates agree with LIGO, others fall short
  - ❖ CE evolution more important than secular evolution
  - ❖ 3+1 quadruples have lesser mergers than 2+2 quadruples
  - ❖ Zero SNe kicks  $\rightarrow$  more mergers, possible high  $e_{\text{LIGO}}$  and negative  $\chi_{\text{eff}}$
  - ❖ Low metallicities  $\rightarrow$  more mergers, higher BH masses
-

**The End**

...